

**For Online Publication**

**Internet Appendix of “Debt and Deficits: Fiscal  
Analysis with Stationary Ratios”**

**John Y. Campbell   Can Gao   Ian W. R. Martin<sup>1</sup>**

**Abstract**

This appendix presents supplementary material and results not included in the main body of the paper.

---

<sup>1</sup>John Campbell: Harvard University and NBER, <https://scholar.harvard.edu/campbell/home>.  
Can Gao: University of St. Gallen and Swiss Finance Institute, <https://sites.google.com/view/can-gao/home>. Ian Martin: London School of Economics, <https://personal.lse.ac.uk/martiniw>.

# Contents

|                                                                                 |       |
|---------------------------------------------------------------------------------|-------|
| IA.1 Data sources and descriptions . . . . .                                    | IA-1  |
| IA.1.1 The US 1841-2022 . . . . .                                               | IA-1  |
| IA.1.2 The UK 1727-2022 . . . . .                                               | IA-2  |
| IA.1.3 Canada, Japan, Switzerland, and the eurozone . . . . .                   | IA-3  |
| IA.2 Data plots . . . . .                                                       | IA-5  |
| IA.3 Measurement of real debt returns post WWII . . . . .                       | IA-21 |
| IA.4 Theoretical values . . . . .                                               | IA-26 |
| IA.5 Summary statistics for US and UK . . . . .                                 | IA-27 |
| IA.6 Unit root tests and autocorrelation coefficients . . . . .                 | IA-31 |
| IA.7 Results for US and UK . . . . .                                            | IA-40 |
| IA.7.1 Local projections . . . . .                                              | IA-40 |
| IA.7.2 VAR estimates . . . . .                                                  | IA-44 |
| IA.7.3 Variance decomposition of $fp_t$ . . . . .                               | IA-48 |
| IA.7.4 Unexpected tax and spending news . . . . .                               | IA-50 |
| IA.7.5 Sensitivity analysis of $\rho$ and $\beta$ . . . . .                     | IA-56 |
| IA.7.6 Variance decomposition of unexpected returns . . . . .                   | IA-68 |
| IA.8 Results for Canada, Japan, Switzerland and 11 Eurozone countries . . . . . | IA-70 |
| IA.8.1 VAR estimates . . . . .                                                  | IA-70 |
| IA.8.2 Variance decomposition of $fp_t$ . . . . .                               | IA-83 |
| IA.9 Other state variables . . . . .                                            | IA-91 |

## IA.1 Data sources and descriptions

### IA.1.1 The US 1841-2022

**Nominal GDP and GDP deflator** data is from the website of Louis Johnston and Samuel H. Williamson.<sup>1</sup>

The **spending, tax and interest payment** data is taken from OMB. We use the most recent observations from OMB. We use total receipts as  $T_t$ , and the difference between total outlays and interest payments as  $X_t$ .<sup>2</sup>

For interest payment data after 1940 and tax and spending data after 1901, we download directly from FRED website (series named FYFR, FYOINT and FYONET).

We hand collect interest payment data before 1940 (or 1901 for tax and spending) from the most recent digitized archive, the *Annual Report of 1980* (pages 4–14). Data are available from 1791 (end of December). In 1842, Congress changed the beginning of the fiscal year from January 1 to July 1. In 1977, it was changed again from July 1 to October 1 where it remains today. We interpolate the spending and tax data before 1842 to match the change from January to July. We do not make any adjustment for the change in 1977, which means the one-period length between 1976-1977 is effectively 1.25 years. Later, we match the observations of debt market values with fiscal years by taking end of June observations until 1976 and end of September observations thereafter.

As we treat social security taxes as taxes and social security benefit payments as outlays, we are consolidating the Social Security trust fund with the federal government, and as a result we do *not* include the nonmarketable debt held by the Social Security trust fund in our measure of government debt. Conversely, as our measures of tax receipts and expenditures do include transfers between the Federal Reserve and Treasury, we are treating the Federal Reserve as being outside the federal government. We therefore include the marketable debt held by the Federal Reserve in our measure of the debt.

For the **market value of debt**, there are two main data sources. The Dallas Fed provides the market value of marketable debt,  $V_t$ , from the 1942. The suitable series according to our definition of debt is the *market value of gross federal debts* from the

---

<sup>1</sup>See <https://www.measuringworth.com/> for details.

<sup>2</sup>Receipts include taxes and other collections from the public. See table 17.1 in [https://www.whitehouse.gov/wp-content/uploads/2023/03/ap\\_17\\_receipts\\_fy2024.pdf](https://www.whitehouse.gov/wp-content/uploads/2023/03/ap_17_receipts_fy2024.pdf) for details. Outlays are payments that liquidate obligations. Details are given in the chapter on outlays in [https://www.whitehouse.gov/wp-content/uploads/2023/03/ap\\_15\\_concepts\\_fy2024.pdf](https://www.whitehouse.gov/wp-content/uploads/2023/03/ap_15_concepts_fy2024.pdf). The US federal government also collects income from the public through market-oriented activities. Collections from these activities are subtracted from gross outlays, rather than being added to taxes and other governmental receipts. See table 18.1 in [https://www.whitehouse.gov/wp-content/uploads/2023/03/ap\\_18\\_offsetting\\_fy2024.pdf](https://www.whitehouse.gov/wp-content/uploads/2023/03/ap_18_offsetting_fy2024.pdf) for details.

spreadsheet on the Dallas Fed’s website. For long sample data, the calculation of ‘privately held debt’ from Robert Hall’s website (as used in [Hall and Sargent \(2021\)](#)) is available.

The two sources are similar to each other (see the following figure). We use Dallas Fed’s data from 1942 and connect it with Hall-Sargent’s data before 1942.

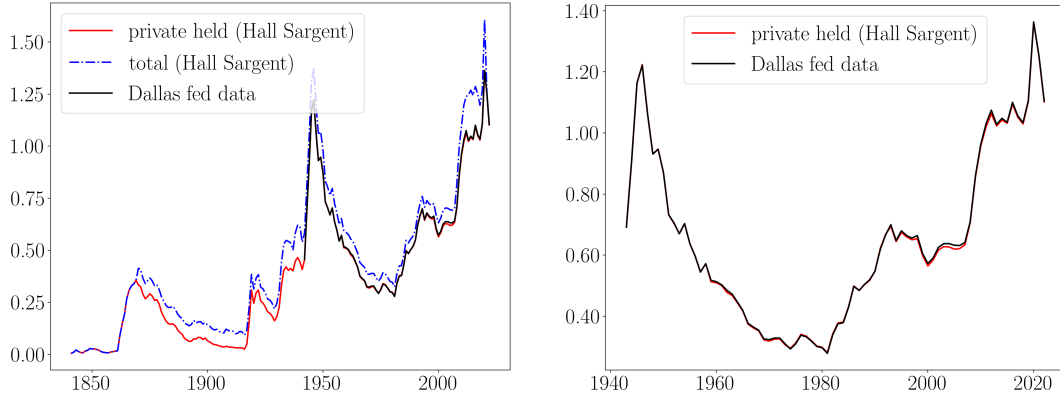


Figure IA.1: Hall-Sargent’s data vs. Dallas Fed’s ‘market value of gross federal debts’ (measured as debt-to-GDP ratio)

The US full sample range is 1790s to 2022. As there are three missing data points for the market value of debt from 1838 to 1840, we start from 1841. We match the observations of debt market values with fiscal years. To do so, we use end of June observations until 1976 and end of September observations thereafter.

We take 1 year and 10 year nominal bond yields from FRED after 1953, using variable names GS1 and GS10. Pre-1953 data is from Robert Shiller’s website. The variable  $yr_{1,t}$  is constructed by taking difference between the one-year yield and lagged inflation between  $t - 1$  and  $t$ . The variable  $spr_{1 \rightarrow 10,t}$  is the difference between the 10 and 1 year yield.

### IA.1.2 The UK 1727-2022

The public sector in UK includes central government, local government, the Bank of England and other public corporations. Our measures are of **the central government**.

The **market value of debt** data has two parts: i) For 1727-2016, we use the time series of the ‘market value of central government gross debt’ from the Bank of England’s macro dataset;<sup>3</sup> ii) For 2017-2022, we infer the market value of debt using the BIS’s

<sup>3</sup>See <https://www.bankofengland.co.uk/statistics/research-datasets>.

government debt dataset, which reports (market value of) debt to GDP ratios from 2017 to 2022, and nominal GDP and deflator data from the website of Johnston and Williamson.

The spending (central government expenditure), tax (central government receipt), interest payment data is taken from website of the UK’s Office for Budget Responsibility (*historical public finances database*).

### IA.1.3 Canada, Japan, Switzerland, and the eurozone

We merge BIS government debt market value to GDP data and IMF public finance data to construct a panel dataset.<sup>4</sup> Debt to GDP ratio series are from BIS website; expenditure and revenue to GDP data, real GDP growth, and inflation data is from IMF; short and long term interest rates data are from FRED’s website (source is OECD), monthly series.

Most countries’ fiscal year ends in December, so we take December observations as our annual observations if higher frequency data are available. For Canada and Japan, we use March/June observations from year  $N + 1$  as the year  $N$  observation, because the fiscal years of those countries do not align with calendar years. We first compute real return minus GDP growth, then back out the real debt return by adding back the real GDP growth. Similar approaches are used to compute tax, spending, or debt growth rates.

The table below summarizes the starting years for which data are available for Canada, Switzerland, and the 11 eurozone countries.

Table IA.1: Panel data, starting year by country

| Year | Countries                                                    |
|------|--------------------------------------------------------------|
| 1989 | CAN                                                          |
| 1999 | AUT, BEL, CHE, DEU, ESP, FIN<br>FRA, GRC, IRL, ITA, NLD, PRT |

**For Japan 1980-2022.** *Market value of debt* is from [Koeda and Kimura \(2025\)](#), which is measured in Yen.<sup>5</sup> We then take nominal GDP from FRED (measured in USD) and

<sup>4</sup>We exclude a number of smaller countries for which data are available (CHL, KOR, LUX, ISR, NOR, and TUR), and five EU countries that are not in the eurozone (CZE, DNK, HUN, POL, SWE) that are not in the eurozone.

<sup>5</sup>We thank the authors for sharing data with us.

convert to Japanese Yen using the exchange rate from BIS.

The other variables—real GDP growth, tax to GDP, spending to GDP and interest payment to GDP—are all from the IMF dataset.

## IA.2 Data plots

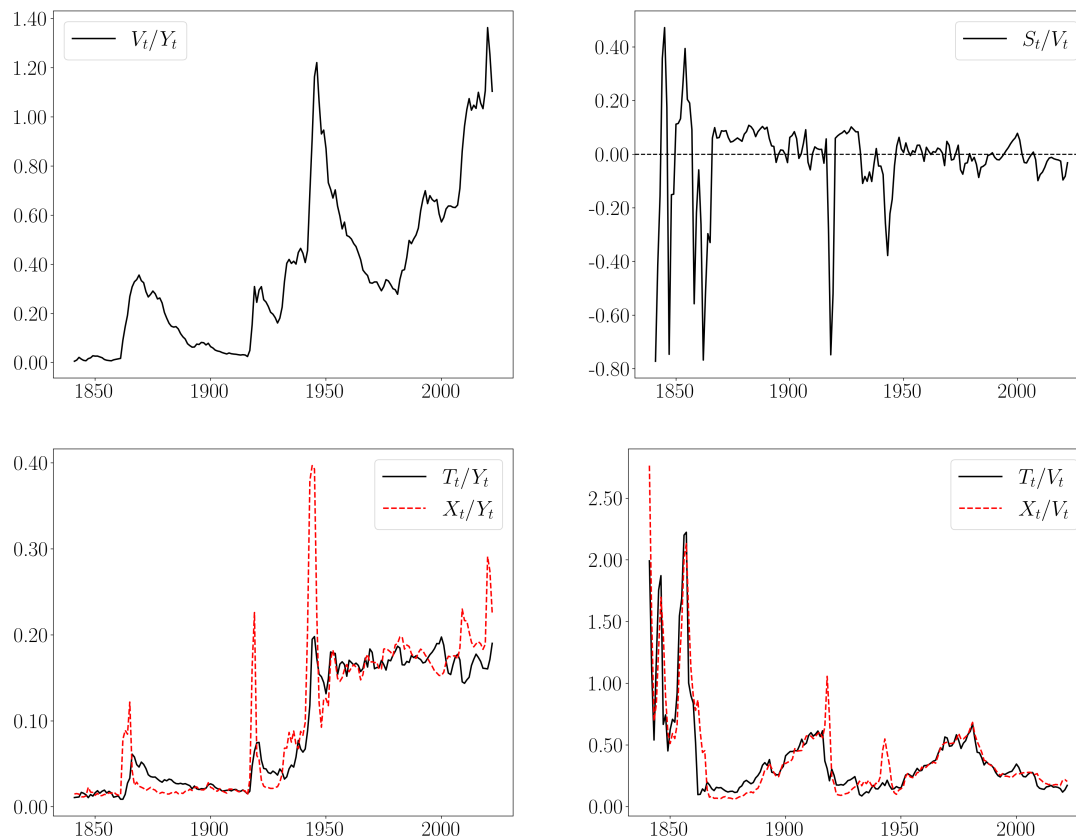


Figure IA.2: USA

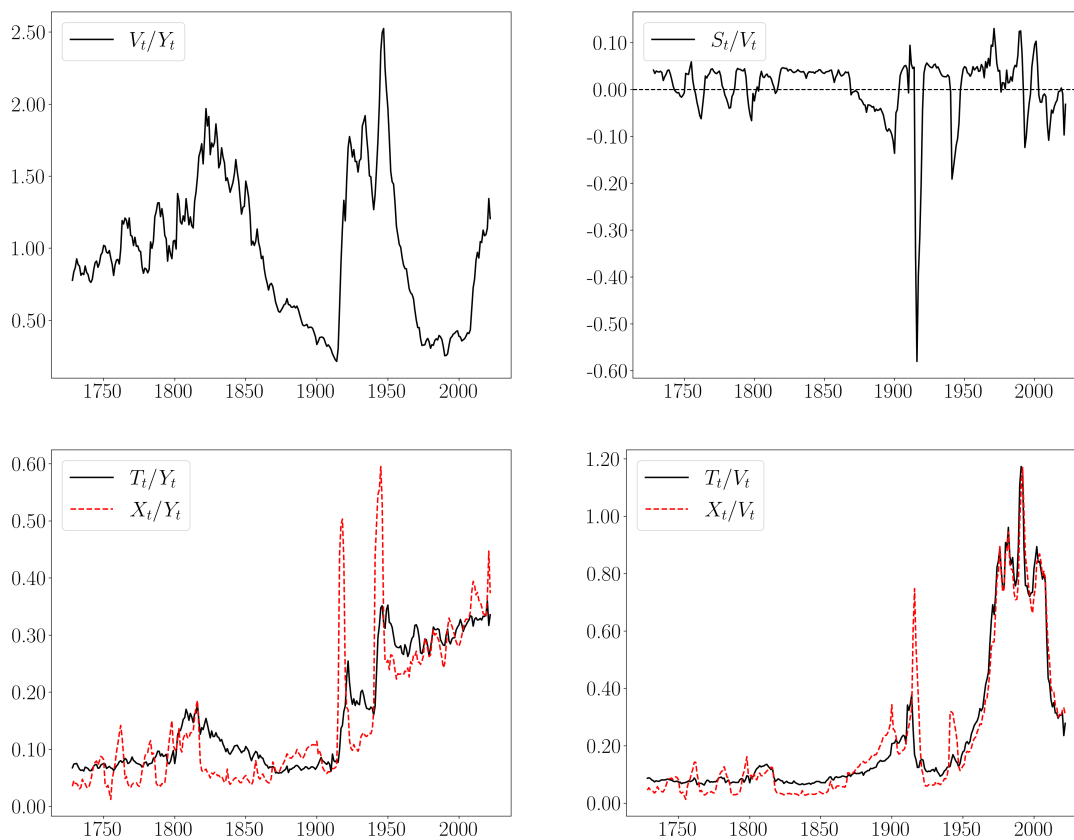


Figure IA.3: GBR

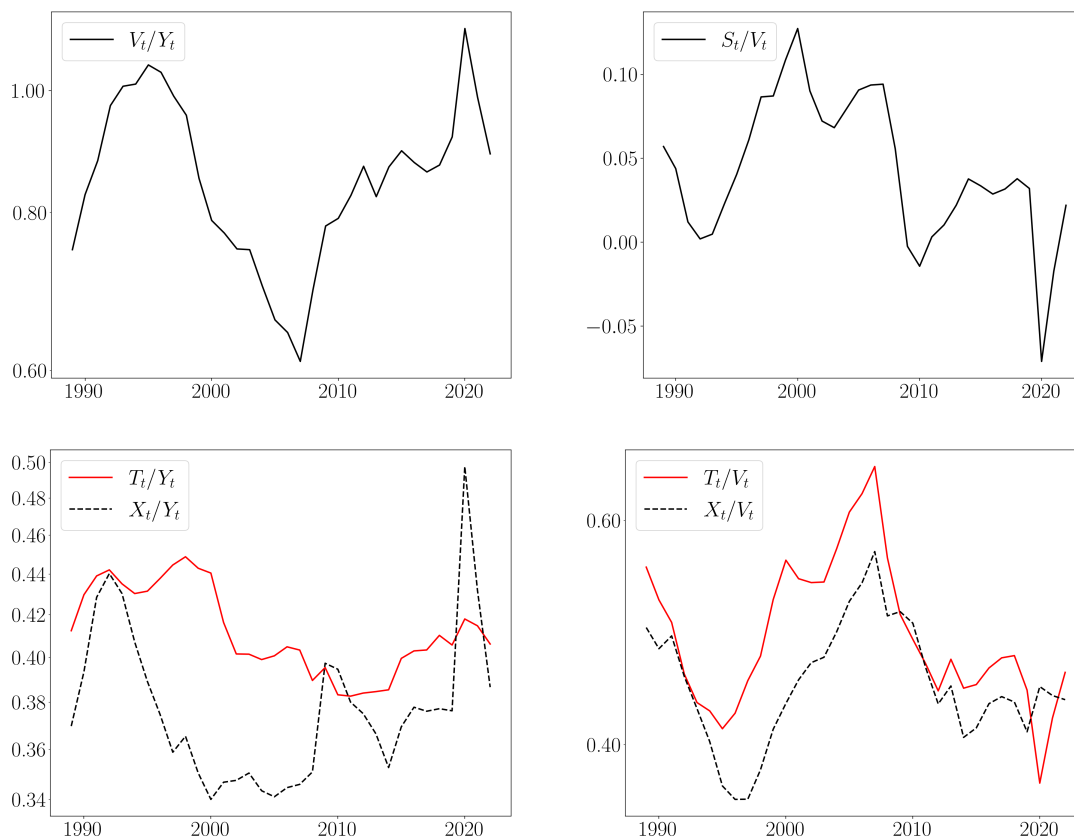


Figure IA.4: CAN

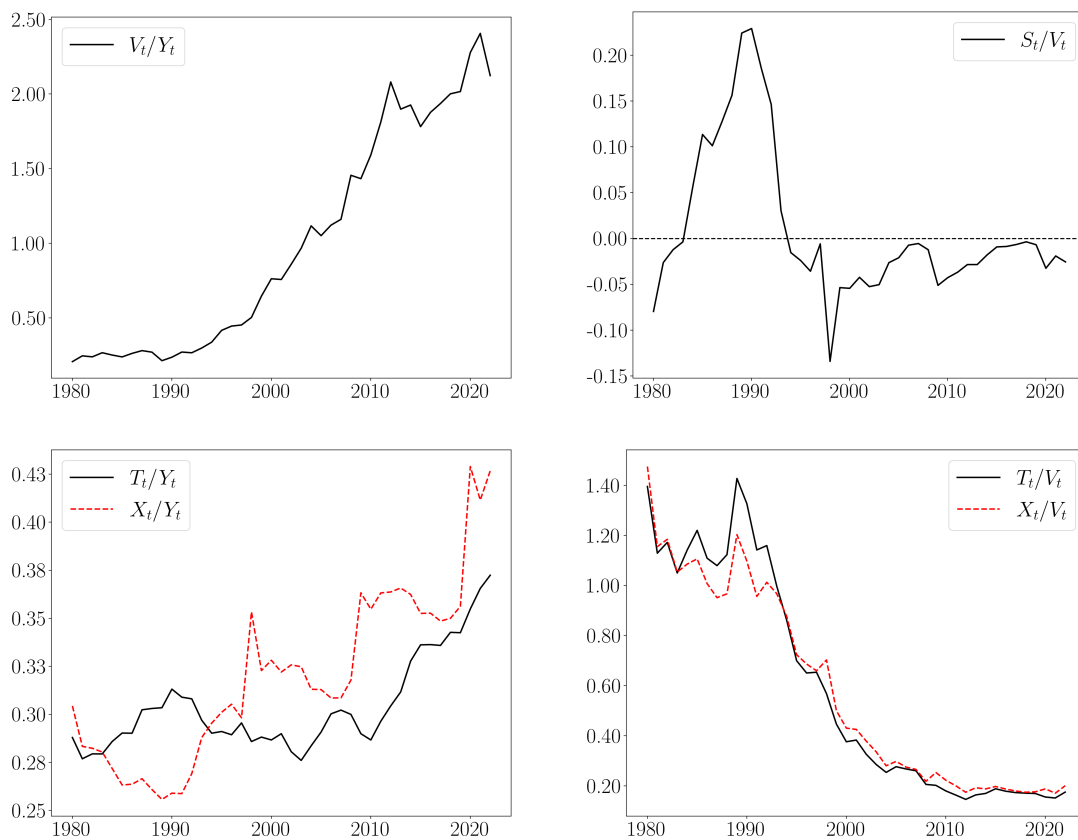


Figure IA.5: JPN



Figure IA.6: CHE

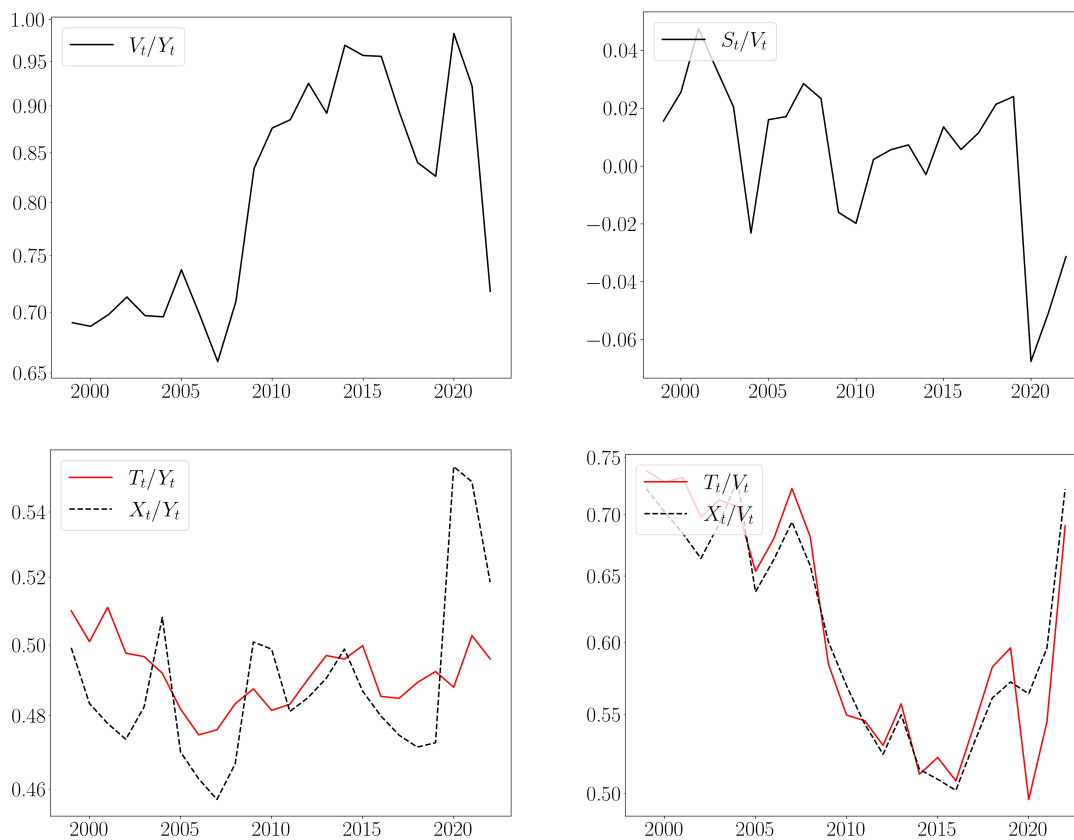


Figure IA.7: AUT



Figure IA.8: BEL

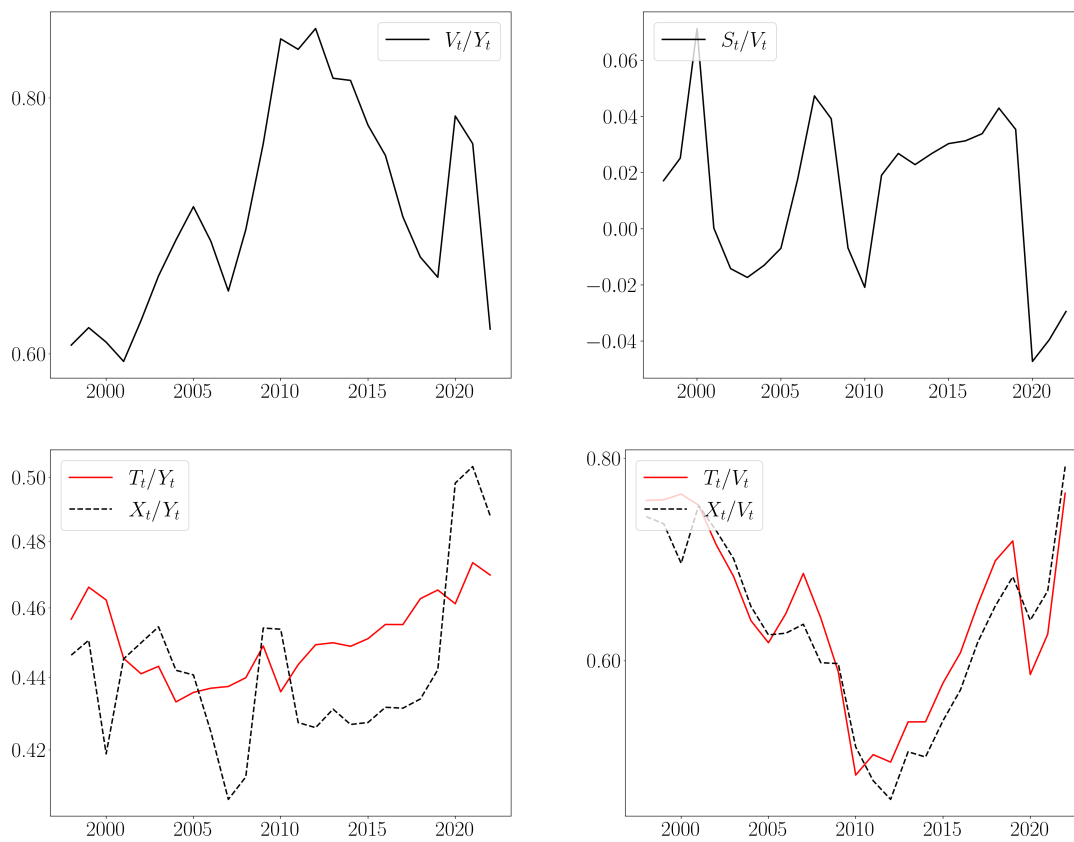


Figure IA.9: DEU

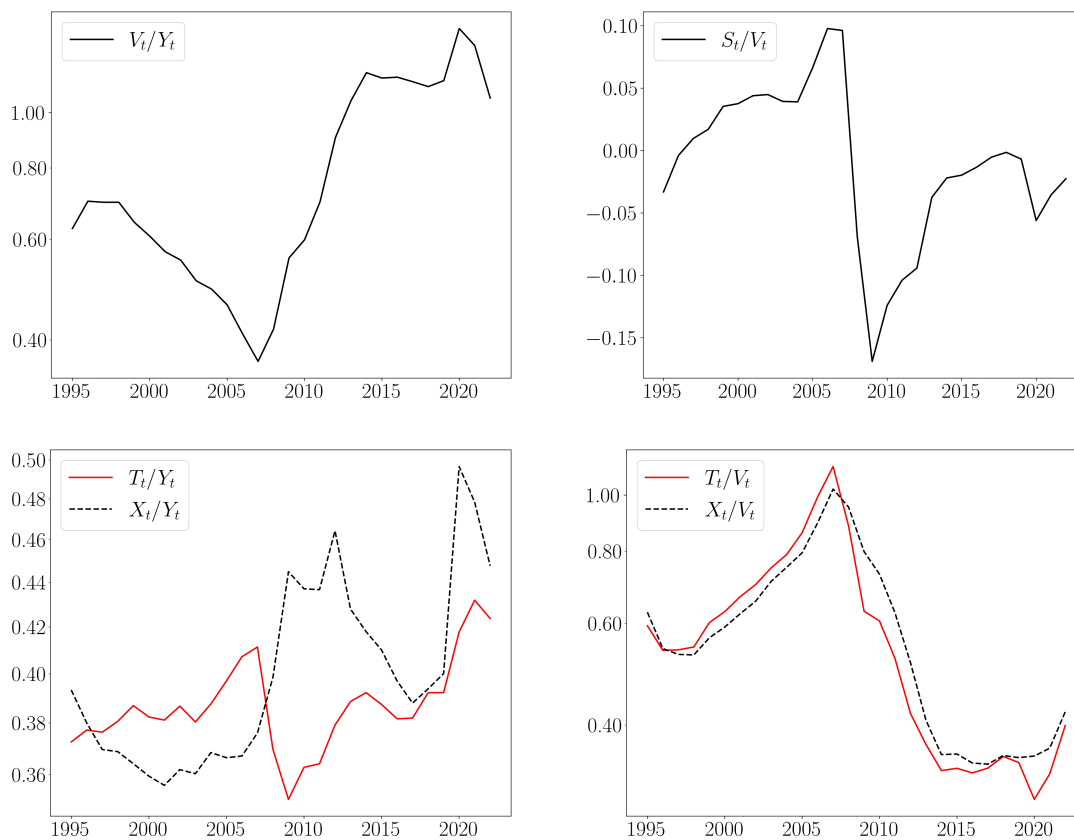


Figure IA.10: ESP

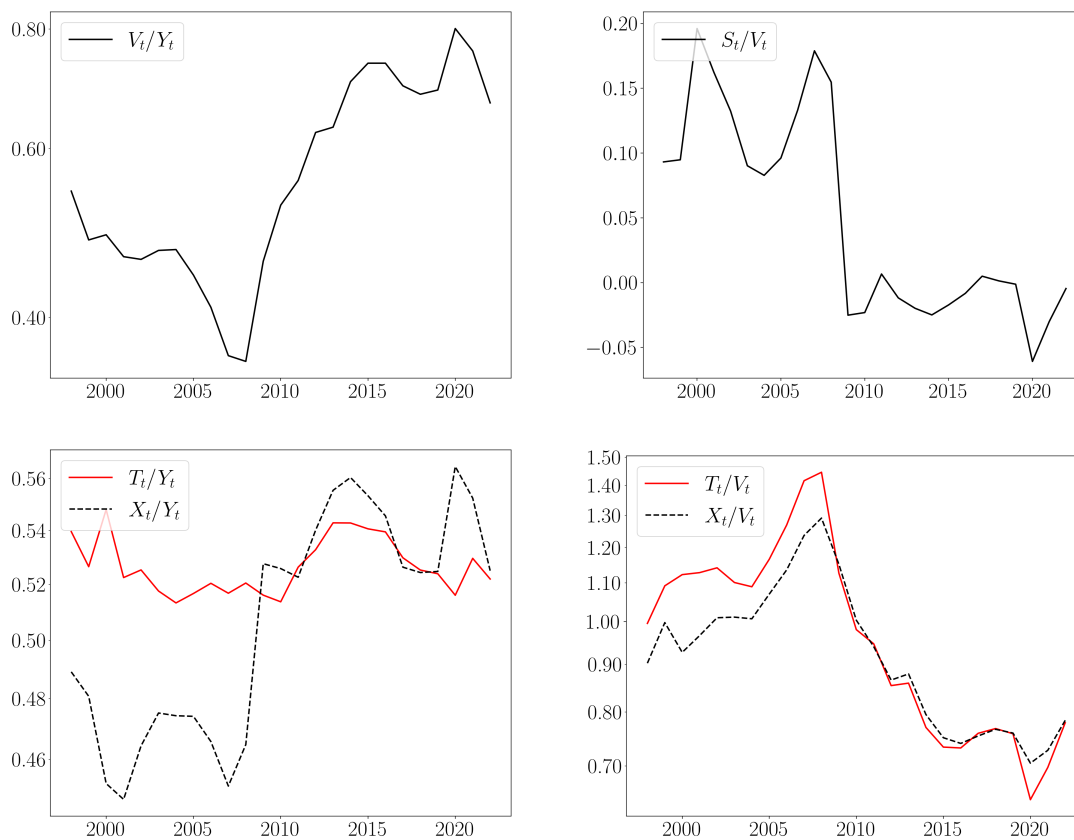


Figure IA.11: FIN

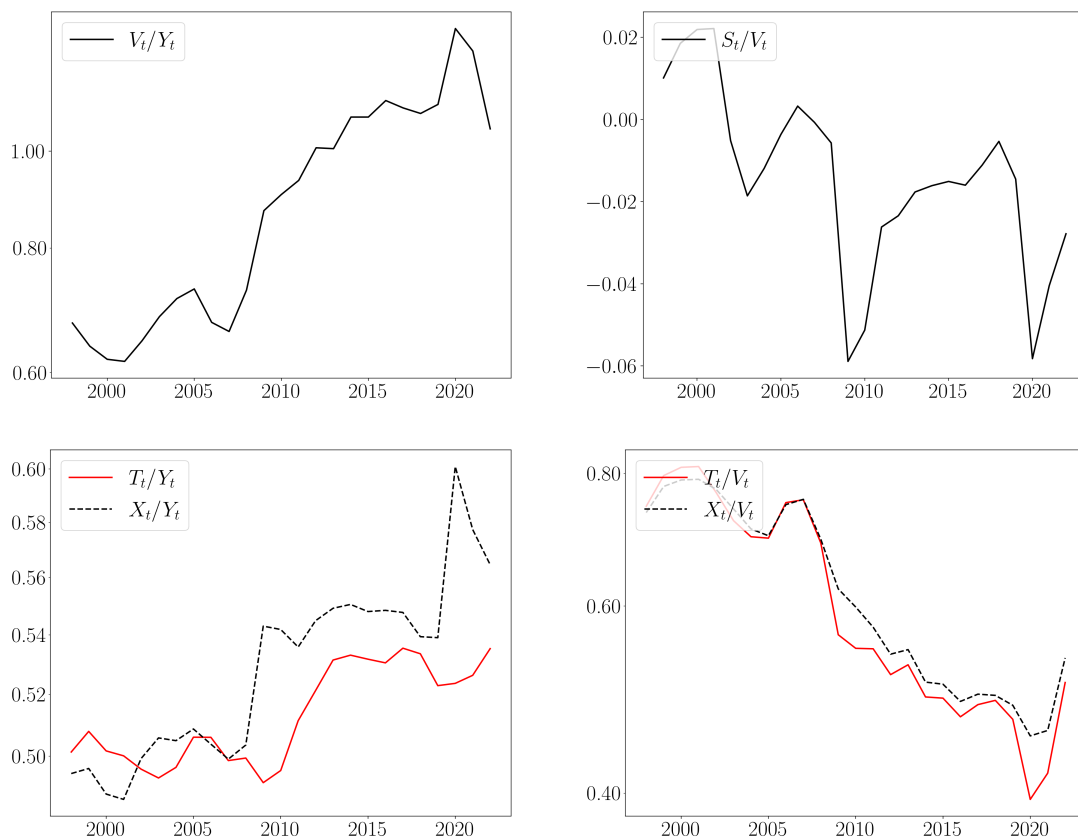


Figure IA.12: FRA

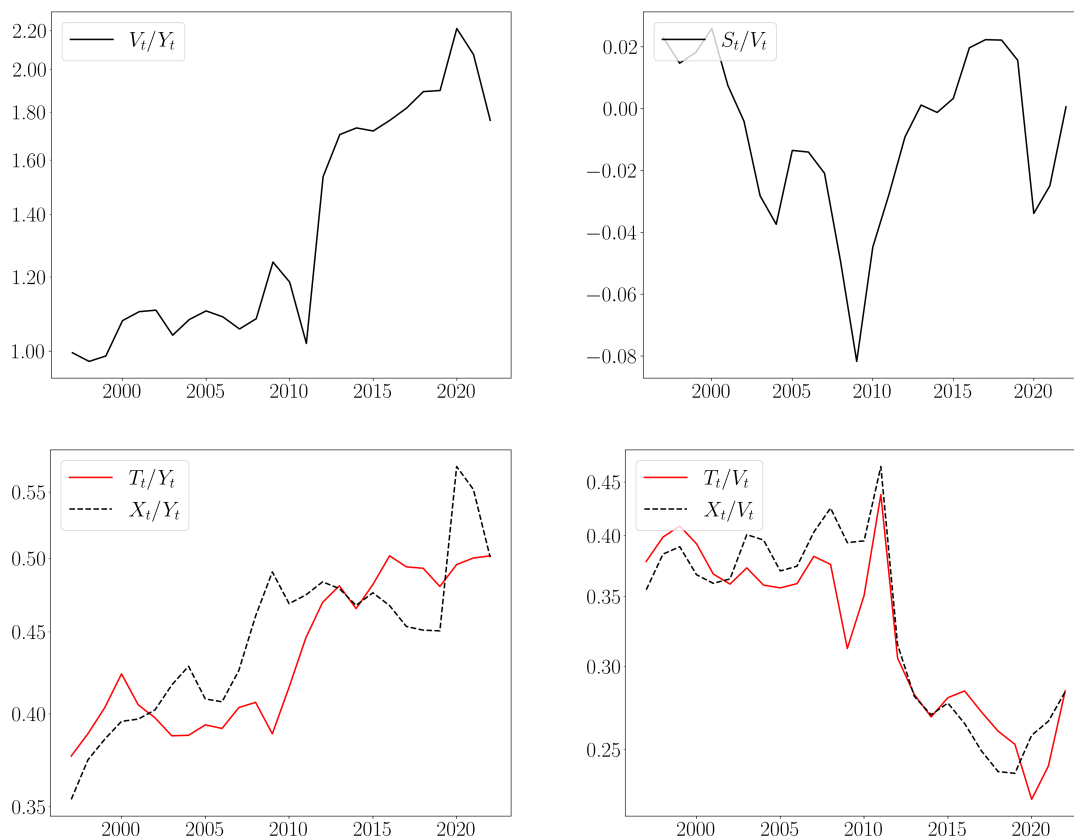


Figure IA.13: GRC

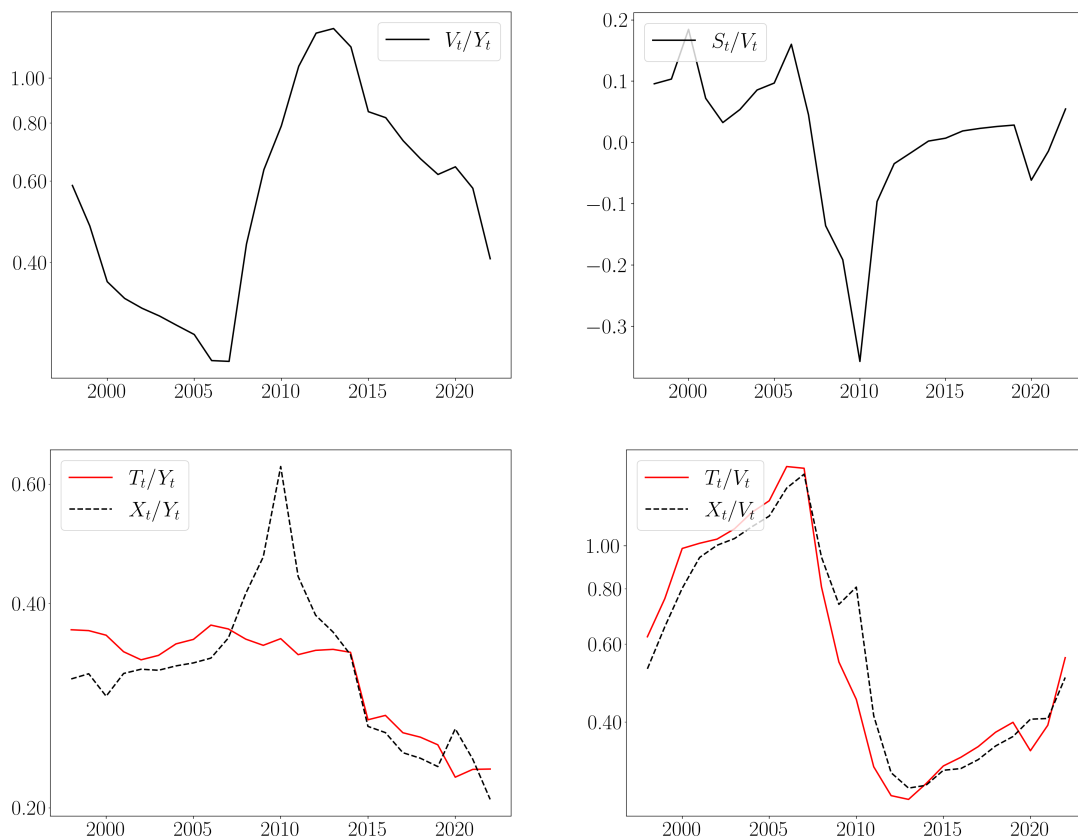


Figure IA.14: IRL

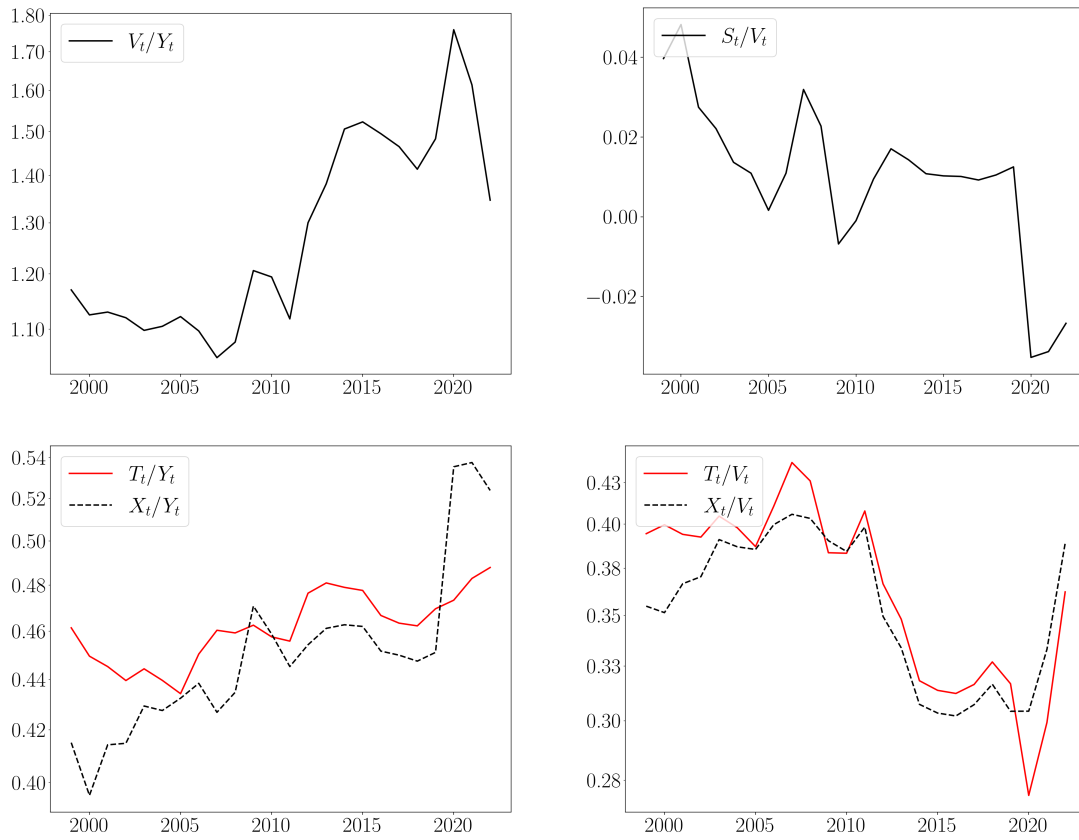


Figure IA.15: ITA

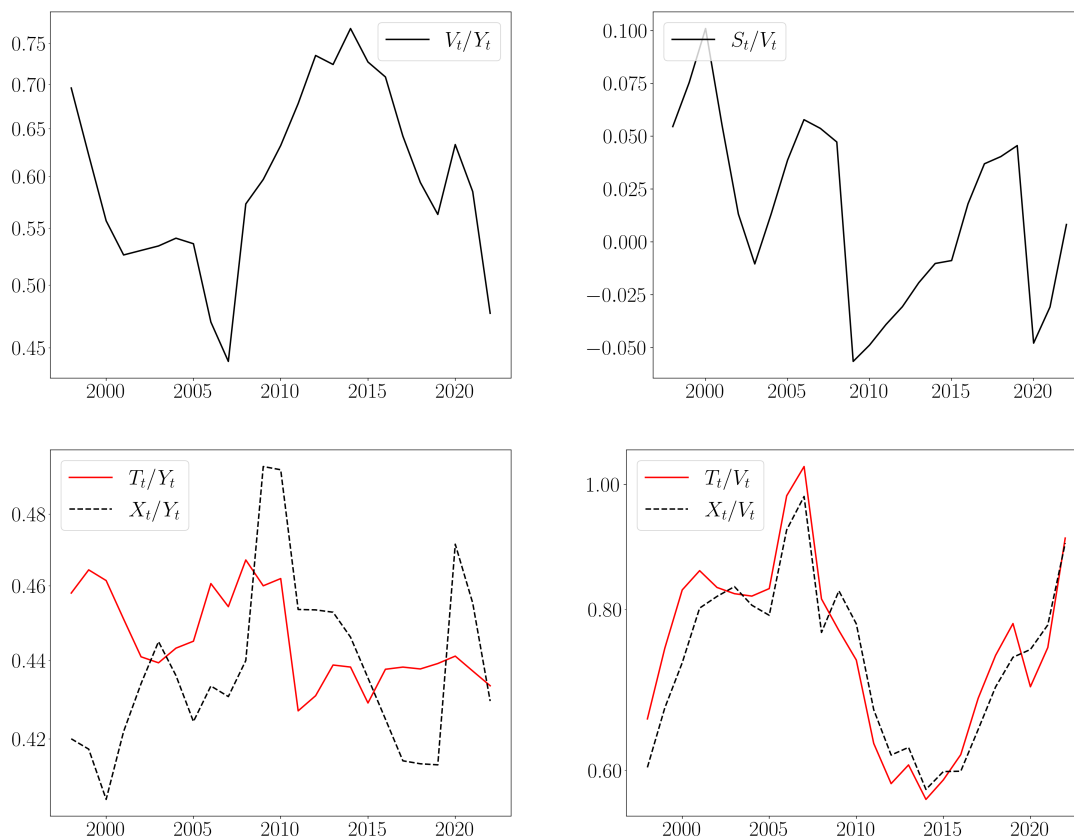


Figure IA.16: NLD

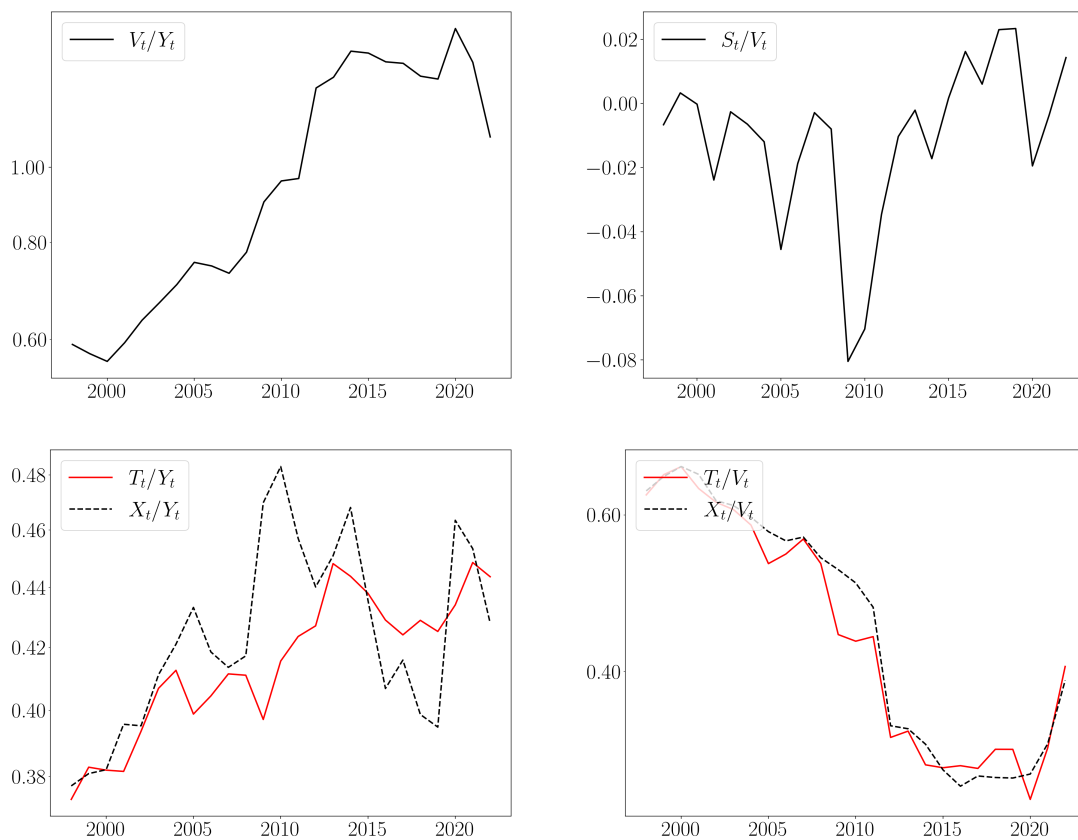


Figure IA.17: PRT

### IA.3 Measurement of real debt returns post WWII

Table IA.2: US, UK, Canada, Japan, and Switzerland (1)

The imputed real debt return is regressed on the realized short-term real interest rate, the change in the long-term nominal bond yield, or both. Standard errors are computed using a Newey-West correction with a single lag. The multiple regression equation is the following:

$$r_t = \alpha + \beta (\text{short yield}_{t-1 \rightarrow t} - \text{realised inflation}_t) + \gamma \Delta \text{long yield}_t + \varepsilon_t$$

| country | $\alpha$ | NW <sub>se</sub> | $\beta$ | NW <sub>se</sub> | $\gamma$ | NW <sub>se</sub> | $R^2$ | obs. |
|---------|----------|------------------|---------|------------------|----------|------------------|-------|------|
| USA     | 0.01     | [0.00]           | 1.42    | [0.15]           | —        | —                | 55.3% | 76   |
|         | 0.02     | [0.00]           | —       | —                | −4.09    | [0.47]           | 60.2% | 76   |
|         | 0.01     | [0.00]           | 1.01    | [0.11]           | −3.05    | [0.36]           | 84.1% | 76   |
| GBR     | 0.03     | [0.01]           | 1.80    | [0.36]           | —        | —                | 23.5% | 76   |
|         | 0.03     | [0.01]           | —       | —                | −10.27   | [1.12]           | 40.8% | 76   |
|         | 0.03     | [0.01]           | 0.97    | [0.34]           | −8.49    | [1.20]           | 46.4% | 76   |
| CAN     | 0.05     | [0.01]           | 1.06    | [0.32]           | —        | —                | 35.1% | 33   |
|         | 0.06     | [0.01]           | —       | —                | −4.43    | [1.28]           | 34.4% | 33   |
|         | 0.05     | [0.01]           | 0.78    | [0.26]           | −3.23    | [0.82]           | 51.0% | 33   |
| JPN     | 0.02     | [0.00]           | 0.73    | [0.44]           | —        | —                | 13.5% | 25   |
|         | 0.02     | [0.01]           | —       | —                | −3.62    | [1.94]           | 20.4% | 25   |
|         | 0.02     | [0.00]           | 0.68    | [0.37]           | −3.47    | [1.85]           | 32.3% | 25   |
| CHE     | 0.03     | [0.01]           | 1.50    | [0.52]           | —        | —                | 20.5% | 23   |
|         | 0.02     | [0.01]           | —       | —                | −5.85    | [0.57]           | 65.8% | 23   |
|         | 0.02     | [0.01]           | 0.02    | [0.37]           | −5.83    | [0.74]           | 65.8% | 23   |

Table IA.3: US, UK, Canada, Japan, and Switzerland (2)

The imputed real debt return is regressed on the nominal short rate, the realized inflation rate, the change in the long-term nominal bond yield, and the slope of the term structure (the yield spread between the long-term and short-term interest rate). Standard errors are computed using a Newey-West correction with a single lag.

| country | $\alpha$         | nominal short yield | inflation         | $\Delta$ long yield | slope             | $R^2$ | obs. |
|---------|------------------|---------------------|-------------------|---------------------|-------------------|-------|------|
| USA     | 0.012<br>[0.007] | 1.051<br>[0.096]    | -1.269<br>[0.123] | -2.759<br>[0.347]   | 0.587<br>[0.270]  | 86.6% | 76   |
| GBR     | 0.016<br>[0.013] | 1.451<br>[0.412]    | -1.277<br>[0.450] | -8.089<br>[1.097]   | 2.067<br>[1.164]  | 47.9% | 76   |
| CAN     | 0.096<br>[0.015] | 0.394<br>[0.180]    | -1.977<br>[0.422] | -4.115<br>[0.771]   | -0.904<br>[0.497] | 64.5% | 33   |
| JPN     | 0.008<br>[0.004] | 0.930<br>[1.163]    | -0.440<br>[0.360] | -2.868<br>[1.825]   | 1.176<br>[1.070]  | 38.3% | 25   |
| CHE     | 0.030<br>[0.008] | 0.151<br>[0.322]    | 1.128<br>[0.586]  | -7.314<br>[0.842]   | -1.653<br>[0.627] | 71.7% | 23   |

Table IA.4: Eurozone countries (1)

The imputed real debt return is regressed on the realized short-term real interest rate, the change in the long-term nominal bond yield, or both. Standard errors are computed using a Newey-West correction with a single lag. The multiple regression equation is the following:

$$r_t = \alpha + \beta (\text{short yield}_{t-1 \rightarrow t} - \text{realised inflation}_t) + \gamma \Delta \text{long yield}_t + \varepsilon_t$$

| country | $\alpha$ | NW <sub>se</sub> | $\beta$ | NW <sub>se</sub> | $\gamma$ | NW <sub>se</sub> | $R^2$ | obs. |
|---------|----------|------------------|---------|------------------|----------|------------------|-------|------|
| AUT     | 0.04     | [0.01]           | 2.18    | [0.29]           | —        | —                | 74.4% | 23   |
|         | 0.01     | [0.01]           | —       | —                | -7.76    | [1.06]           | 69.2% | 23   |
|         | 0.03     | [0.01]           | 1.42    | [0.19]           | -4.49    | [0.54]           | 88.5% | 23   |
| BEL     | 0.03     | [0.01]           | 1.70    | [0.34]           | —        | —                | 60.9% | 24   |
|         | 0.01     | [0.01]           | —       | —                | -6.11    | [1.39]           | 72.3% | 24   |
|         | 0.02     | [0.00]           | 0.99    | [0.15]           | -4.34    | [0.60]           | 86.8% | 24   |
| DEU     | 0.03     | [0.01]           | 1.63    | [0.40]           | —        | —                | 54.5% | 24   |
|         | 0.02     | [0.01]           | —       | —                | -6.29    | [2.11]           | 50.7% | 24   |
|         | 0.03     | [0.01]           | 1.10    | [0.34]           | -3.91    | [1.31]           | 68.4% | 24   |
| ESP     | 0.03     | [0.01]           | 1.48    | [0.38]           | —        | —                | 42.9% | 27   |
|         | 0.02     | [0.01]           | —       | —                | -4.68    | [0.81]           | 68.2% | 27   |
|         | 0.02     | [0.01]           | 0.42    | [0.30]           | -3.97    | [0.72]           | 70.2% | 27   |
| FIN     | 0.08     | [0.01]           | 2.18    | [0.24]           | —        | —                | 47.7% | 24   |
|         | 0.06     | [0.02]           | —       | —                | -5.98    | [1.11]           | 32.6% | 24   |
|         | 0.07     | [0.01]           | 1.71    | [0.35]           | -3.15    | [1.19]           | 54.4% | 24   |

Table IA.5: Eurozone countries (2)

The imputed real debt return is regressed on the realized short-term real interest rate, the change in the long-term nominal bond yield, or both. Standard errors are computed using a Newey-West correction with a single lag. The multiple regression equation is the following:

$$r_t = \alpha + \beta (\text{short yield}_{t-1 \rightarrow t} - \text{realised inflation}_t) + \gamma \Delta \text{long yield}_t + \varepsilon_t$$

| country | $\alpha$ | NW <sub>se</sub> | $\beta$ | NW <sub>se</sub> | $\gamma$ | NW <sub>se</sub> | $R^2$ | obs. |
|---------|----------|------------------|---------|------------------|----------|------------------|-------|------|
| FRA     | 0.02     | [0.01]           | 1.80    | [0.45]           | —        | —                | 57.0% | 24   |
|         | 0.01     | [0.01]           | —       | —                | -5.98    | [1.12]           | 71.6% | 24   |
|         | 0.02     | [0.00]           | 1.08    | [0.21]           | -4.44    | [0.52]           | 87.4% | 24   |
| GRC     | 0.01     | [0.02]           | 1.04    | [0.44]           | —        | —                | 14.2% | 25   |
|         | 0.01     | [0.01]           | —       | —                | -3.35    | [0.40]           | 79.6% | 25   |
|         | 0.01     | [0.01]           | 0.01    | [0.35]           | -3.35    | [0.46]           | 79.6% | 25   |
| IRL     | 0.04     | [0.02]           | 2.16    | [0.74]           | —        | —                | 23.4% | 24   |
|         | 0.03     | [0.02]           | —       | —                | -3.69    | [1.56]           | 17.4% | 24   |
|         | 0.04     | [0.02]           | 1.90    | [0.80]           | -3.05    | [1.66]           | 35.0% | 24   |
| ITA     | 0.03     | [0.01]           | 1.53    | [0.14]           | —        | —                | 58.6% | 23   |
|         | 0.02     | [0.01]           | —       | —                | -4.67    | [0.58]           | 85.2% | 23   |
|         | 0.02     | [0.00]           | 0.62    | [0.16]           | -3.69    | [0.53]           | 91.1% | 23   |
| NLD     | 0.03     | [0.01]           | 1.58    | [0.43]           | —        | —                | 31.8% | 24   |
|         | 0.01     | [0.01]           | —       | —                | -5.95    | [1.27]           | 33.2% | 24   |
|         | 0.02     | [0.01]           | 1.00    | [0.47]           | -3.98    | [0.90]           | 42.5% | 24   |
| PRT     | 0.03     | [0.01]           | 1.39    | [0.33]           | —        | —                | 33.8% | 24   |
|         | 0.02     | [0.01]           | —       | —                | -2.30    | [0.56]           | 60.3% | 24   |
|         | 0.03     | [0.01]           | 0.87    | [0.31]           | -1.94    | [0.55]           | 71.9% | 24   |

Table IA.6: Eurozone countries (3)

The imputed real debt return is regressed on the nominal short rate, the realized inflation rate, the change in the long-term nominal bond yield, and the slope of the term structure (the yield spread between the long-term and short-term interest rate). Standard errors are computed using a Newey-West correction with a single lag.

| country | $\alpha$          | nominal short yield | inflation         | $\Delta$ long yield | slope             | $R^2$ | obs. |
|---------|-------------------|---------------------|-------------------|---------------------|-------------------|-------|------|
| AUT     | 0.023<br>[0.012]  | 1.483<br>[0.234]    | -1.324<br>[0.323] | -4.608<br>[0.783]   | 0.100<br>[0.817]  | 88.5% | 23   |
| BEL     | 0.021<br>[0.009]  | 1.007<br>[0.235]    | -0.972<br>[0.305] | -4.344<br>[1.000]   | 0.065<br>[0.869]  | 86.8% | 24   |
| DEU     | 0.029<br>[0.018]  | 0.849<br>[0.493]    | -1.545<br>[0.436] | -2.828<br>[1.463]   | 1.220<br>[1.450]  | 71.5% | 24   |
| ESP     | -0.008<br>[0.016] | 0.867<br>[0.268]    | -0.580<br>[0.297] | -3.234<br>[0.747]   | 1.333<br>[0.659]  | 76.1% | 27   |
| FIN     | -0.020<br>[0.020] | 3.090<br>[0.316]    | 0.177<br>[0.416]  | -4.392<br>[0.897]   | 3.206<br>[1.009]  | 82.9% | 24   |
| FRA     | 0.017<br>[0.009]  | 1.076<br>[0.199]    | -0.961<br>[0.326] | -4.655<br>[0.659]   | -0.232<br>[0.351] | 87.5% | 24   |
| GRC     | -0.008<br>[0.020] | 0.163<br>[0.427]    | 0.431<br>[0.437]  | -3.418<br>[0.409]   | 0.160<br>[0.224]  | 80.4% | 25   |
| IRL     | -0.001<br>[0.032] | 3.614<br>[1.310]    | -0.954<br>[0.635] | -3.476<br>[1.386]   | -0.114<br>[1.346] | 46.6% | 24   |
| ITA     | -0.009<br>[0.006] | 1.151<br>[0.147]    | -0.804<br>[0.144] | -2.864<br>[0.359]   | 1.303<br>[0.195]  | 95.8% | 23   |
| NLD     | 0.008<br>[0.023]  | 1.768<br>[0.682]    | -0.120<br>[0.545] | -6.161<br>[1.993]   | -2.421<br>[2.273] | 55.1% | 24   |
| PRT     | -0.007<br>[0.012] | 1.506<br>[0.269]    | -0.812<br>[0.297] | -1.470<br>[0.228]   | 1.007<br>[0.263]  | 84.5% | 24   |

## IA.4 Theoretical values

Table IA.7: Parameters choices

The last three columns report the corresponding sample means.

| Country | period    | $r$   | $g$   | $\rho$ | $\beta$ | $\mathbb{E} r_t$ | $\mathbb{E} \Delta y_t$ | $\mathbb{E} \Delta v$ |
|---------|-----------|-------|-------|--------|---------|------------------|-------------------------|-----------------------|
| USA     | 1841-2022 | 0.029 | 0.035 | 1.006  | 1.014   | 0.029            | 0.035                   | 0.064                 |
|         |           | 0.055 | 0.035 | 0.980  | 0.952   | 0.029            | 0.035                   | 0.064                 |
|         | 1947-2022 | 0.020 | 0.030 | 1.010  | 1.036   | 0.021            | 0.030                   | 0.029                 |
|         |           | 0.050 | 0.030 | 0.980  | 0.931   | 0.021            | 0.030                   | 0.029                 |
| GBR     | 1727-2022 | 0.021 | 0.017 | 0.997  | 0.975   | 0.021            | 0.018                   | 0.019                 |
|         | 1947-2022 | 0.032 | 0.024 | 0.991  | 0.980   | 0.032            | 0.024                   | 0.014                 |
| CAN     | 1989-2022 | 0.067 | 0.021 | 0.955  | 0.944   | 0.067            | 0.021                   | 0.026                 |
| CHE     | 1999-2022 | 0.025 | 0.019 | 0.994  | 0.993   | 0.025            | 0.019                   | -0.005                |
| JPN     | 1980-2022 | 0.085 | 0.017 | 0.933  | 0.912   | 0.086            | 0.017                   | 0.079                 |
| AUT     | 1999-2022 | 0.020 | 0.016 | 0.996  | 0.993   | 0.020            | 0.016                   | 0.017                 |
| BEL     | 1999-2022 | 0.016 | 0.017 | 1.001  | 1.002   | 0.016            | 0.017                   | 0.004                 |
| DEU     | 1999-2022 | 0.024 | 0.012 | 0.988  | 0.984   | 0.024            | 0.012                   | 0.013                 |
| ESP     | 1999-2022 | 0.020 | 0.017 | 0.997  | 0.994   | 0.020            | 0.017                   | 0.034                 |
| FIN     | 1999-2022 | 0.067 | 0.016 | 0.950  | 0.951   | 0.067            | 0.016                   | 0.025                 |
| FRA     | 1999-2022 | 0.017 | 0.014 | 0.997  | 0.993   | 0.017            | 0.014                   | 0.032                 |
| GRC     | 1999-2022 | 0.019 | 0.005 | 0.986  | 0.965   | 0.019            | 0.005                   | 0.030                 |
| IRL     | 1999-2022 | 0.037 | 0.055 | 1.019  | 1.026   | 0.037            | 0.055                   | 0.040                 |
| ITA     | 1999-2022 | 0.018 | 0.004 | 0.986  | 0.977   | 0.018            | 0.004                   | 0.010                 |
| NLD     | 1999-2022 | 0.013 | 0.017 | 1.004  | 1.005   | 0.013            | 0.017                   | 0.002                 |
| PRT     | 1999-2022 | 0.024 | 0.010 | 0.986  | 0.973   | 0.024            | 0.010                   | 0.036                 |

## IA.5 Summary statistics for US and UK

Table IA.8: Summary statistics of US data, 1841 to 2022

| horizon                   | mean   | std   | skew   | kurt   | median | max    | min    | auto-corr |
|---------------------------|--------|-------|--------|--------|--------|--------|--------|-----------|
| $r_t$                     | 0.029  | 0.102 | -0.009 | 11.502 | 0.029  | 0.612  | -0.543 | 0.048     |
| $\Delta x_t$              | 0.049  | 0.293 | 1.644  | 17.469 | 0.024  | 1.886  | -1.339 | 0.216     |
| $\Delta \tau_t$           | 0.048  | 0.168 | 1.809  | 8.414  | 0.036  | 1.044  | -0.367 | 0.325     |
| $\Delta v_t$              | 0.064  | 0.232 | 3.633  | 20.421 | 0.017  | 1.783  | -0.422 | 0.422     |
| $\Delta y_t$              | 0.035  | 0.046 | -0.473 | 2.452  | 0.034  | 0.169  | -0.142 | 0.284     |
| $\tau v_t$                | -1.215 | 0.677 | 0.715  | 0.394  | -1.286 | 0.799  | -2.448 | 0.934     |
| $xv_t$                    | -1.223 | 0.790 | 0.150  | -0.104 | -1.284 | 1.017  | -2.817 | 0.958     |
| $\log(1 + S_t/V_t)$       | -0.043 | 0.255 | -3.923 | 17.987 | 0.007  | 0.387  | -1.479 | 0.475     |
| $S_t/V_t$                 | -0.019 | 0.169 | -2.209 | 8.142  | 0.007  | 0.472  | -0.772 | 0.590     |
| $T_t/V_t$                 | 0.387  | 0.366 | 3.055  | 10.756 | 0.276  | 2.224  | 0.086  | 0.865     |
| $X_t/V_t$                 | 0.405  | 0.389 | 2.905  | 11.097 | 0.277  | 2.765  | 0.060  | 0.899     |
| $fp_t$ ( $\rho = 1.006$ ) | 0.015  | 0.184 | -1.273 | 4.152  | 0.020  | 0.360  | -0.870 | 0.784     |
| $fp_t$ ( $\rho = 0.980$ ) | -0.039 | 0.182 | -1.489 | 4.643  | -0.028 | 0.284  | -0.936 | 0.773     |
| $\tau y_t$                | -2.811 | 0.997 | -0.189 | -1.542 | -2.881 | -1.619 | -4.728 | 0.988     |
| $xy_t$                    | -2.820 | 1.108 | -0.077 | -1.747 | -2.515 | -0.924 | -4.463 | 0.967     |
| $vy_t$                    | -1.596 | 1.362 | -0.859 | -0.267 | -1.173 | 0.310  | -5.215 | 0.985     |
| $T_t/Y_t$                 | 0.091  | 0.070 | 0.203  | -1.816 | 0.056  | 0.198  | 0.009  | 0.989     |
| $X_t/Y_t$                 | 0.100  | 0.086 | 0.723  | 0.173  | 0.081  | 0.397  | 0.012  | 0.936     |
| $S_t/Y_t$                 | -0.009 | 0.041 | -3.183 | 13.193 | 0.001  | 0.059  | -0.261 | 0.736     |
| $V_t/Y_t$                 | 0.374  | 0.325 | 0.937  | 0.198  | 0.309  | 1.364  | 0.005  | 0.985     |

Table IA.9: Summary statistics of US data, 1947 to 2022

| horizon                   | mean   | std   | skew   | kurt   | median | max    | min    | auto-corr |
|---------------------------|--------|-------|--------|--------|--------|--------|--------|-----------|
| $r_t$                     | 0.020  | 0.055 | -0.339 | 0.597  | 0.019  | 0.144  | -0.140 | 0.304     |
| $\Delta x_t$              | 0.030  | 0.119 | -1.476 | 14.762 | 0.028  | 0.412  | -0.630 | 0.195     |
| $\Delta \tau_t$           | 0.031  | 0.068 | -0.133 | 1.543  | 0.038  | 0.227  | -0.188 | 0.227     |
| $\Delta v_t$              | 0.029  | 0.069 | 0.230  | 0.226  | 0.021  | 0.186  | -0.153 | 0.443     |
| $\Delta y_t$              | 0.030  | 0.024 | -0.194 | 0.077  | 0.030  | 0.086  | -0.027 | 0.068     |
| $\tau v_t$                | -1.242 | 0.450 | -0.105 | -0.917 | -1.261 | -0.398 | -2.140 | 0.968     |
| $xv_t$                    | -1.213 | 0.433 | -0.035 | -0.431 | -1.293 | -0.381 | -2.308 | 0.975     |
| $\log(1 + S_t/V_t)$       | -0.008 | 0.038 | -0.374 | 0.167  | -0.005 | 0.075  | -0.104 | 0.671     |
| $S_t/V_t$                 | -0.008 | 0.037 | -0.262 | 0.086  | -0.005 | 0.078  | -0.098 | 0.674     |
| $T_t/V_t$                 | 0.318  | 0.139 | 0.612  | -0.507 | 0.283  | 0.672  | 0.118  | 0.963     |
| $X_t/V_t$                 | 0.326  | 0.141 | 0.746  | -0.469 | 0.274  | 0.683  | 0.100  | 0.979     |
| $fp_t$ ( $\rho = 1.010$ ) | 0.017  | 0.045 | -0.363 | 2.727  | 0.019  | 0.166  | -0.131 | 0.746     |
| $fp_t$ ( $\rho = 0.980$ ) | -0.058 | 0.048 | -1.072 | 2.749  | -0.050 | 0.07   | -0.228 | 0.761     |
| $\tau y_t$                | -1.785 | 0.074 | -0.532 | 0.723  | -1.778 | -1.622 | -2.028 | 0.661     |
| $xy_t$                    | -1.756 | 0.163 | -0.330 | 3.992  | -1.746 | -1.234 | -2.379 | 0.812     |
| $vy_t$                    | -0.544 | 0.425 | 0.032  | -0.958 | -0.492 | 0.310  | -1.280 | 0.983     |
| $T_t/Y_t$                 | 0.168  | 0.012 | -0.277 | 0.363  | 0.169  | 0.198  | 0.132  | 0.663     |
| $X_t/Y_t$                 | 0.175  | 0.029 | 1.021  | 4.938  | 0.174  | 0.291  | 0.093  | 0.799     |
| $S_t/Y_t$                 | -0.007 | 0.030 | -1.522 | 4.525  | -0.003 | 0.059  | -0.131 | 0.744     |
| $V_t/Y_t$                 | 0.634  | 0.270 | 0.707  | -0.341 | 0.612  | 1.364  | 0.278  | 0.975     |

Table IA.10: Summary statistics of UK data, 1727 to 2022

| horizon             | mean   | std   | skew   | kurt   | median | max    | min    | auto-corr |
|---------------------|--------|-------|--------|--------|--------|--------|--------|-----------|
| $r_t$               | 0.021  | 0.074 | -0.080 | 2.220  | 0.024  | 0.346  | -0.306 | 0.252     |
| $\Delta x_t$        | 0.026  | 0.204 | 1.117  | 12.107 | 0.027  | 1.337  | -0.754 | 0.307     |
| $\Delta \tau_t$     | 0.023  | 0.070 | 1.349  | 7.672  | 0.022  | 0.437  | -0.225 | 0.120     |
| $\Delta v_t$        | 0.019  | 0.091 | 2.151  | 11.892 | 0.011  | 0.689  | -0.216 | 0.402     |
| $\Delta y_t$        | 0.018  | 0.031 | -0.555 | 1.378  | 0.021  | 0.101  | -0.109 | -0.002    |
| $\tau v_t$          | -1.900 | 0.826 | 1.078  | -0.124 | -2.207 | 0.160  | -2.763 | 0.994     |
| $xv_t$              | -2.082 | 1.063 | 0.374  | -0.904 | -2.243 | 0.157  | -4.327 | 0.982     |
| $\log(1 + S_t/V_t)$ | 0.002  | 0.084 | -5.470 | 45.001 | 0.028  | 0.123  | -0.867 | 0.806     |
| $S_t/V_t$           | 0.005  | 0.070 | -3.727 | 22.722 | 0.029  | 0.130  | -0.580 | 0.837     |
| $T_t/V_t$           | 0.227  | 0.254 | 1.907  | 2.459  | 0.110  | 1.173  | 0.063  | 0.989     |
| $X_t/V_t$           | 0.222  | 0.257 | 1.683  | 1.772  | 0.106  | 1.170  | 0.013  | 0.985     |
| $fp_t$              | 0.010  | 0.055 | -0.324 | 0.720  | 0.008  | 0.195  | -0.197 | 0.899     |
| $\tau y_t$          | -2.052 | 0.612 | 0.410  | -1.442 | -2.305 | -1.023 | -2.845 | 0.992     |
| $xy_t$              | -2.234 | 0.796 | 0.253  | -1.002 | -2.360 | -0.519 | -4.398 | 0.968     |
| $vy_t$              | -0.152 | 0.559 | -0.484 | -0.713 | -0.039 | 0.926  | -1.538 | 0.986     |
| $T_t/Y_t$           | 0.156  | 0.099 | 0.744  | -1.106 | 0.100  | 0.360  | 0.058  | 0.993     |
| $X_t/Y_t$           | 0.147  | 0.122 | 1.278  | 0.972  | 0.094  | 0.595  | 0.012  | 0.962     |
| $S_t/Y_t$           | 0.009  | 0.066 | -3.032 | 12.445 | 0.020  | 0.101  | -0.361 | 0.877     |
| $V_t/Y_t$           | 0.988  | 0.487 | 0.461  | -0.284 | 0.962  | 2.525  | 0.215  | 0.982     |

Table IA.11: Summary statistics of UK data, 1947 to 2022

| horizon             | mean   | std   | skew   | kurt   | median | max    | min    | auto-corr |
|---------------------|--------|-------|--------|--------|--------|--------|--------|-----------|
| $r_t$               | 0.032  | 0.067 | -0.178 | -0.217 | 0.036  | 0.169  | -0.121 | 0.058     |
| $\Delta x_t$        | 0.019  | 0.085 | -2.973 | 19.385 | 0.020  | 0.275  | -0.502 | 0.213     |
| $\Delta \tau_t$     | 0.023  | 0.039 | -0.304 | 1.118  | 0.024  | 0.133  | -0.102 | 0.222     |
| $\Delta v_t$        | 0.014  | 0.094 | 0.349  | 0.560  | 0.012  | 0.248  | -0.216 | 0.389     |
| $\Delta y_t$        | 0.024  | 0.026 | -2.025 | 8.793  | 0.026  | 0.083  | -0.109 | 0.053     |
| $\tau v_t$          | -0.706 | 0.586 | -0.480 | -1.029 | -0.437 | 0.160  | -2.060 | 0.984     |
| $xv_t$              | -0.758 | 0.630 | -0.623 | -0.770 | -0.576 | 0.157  | -2.175 | 0.989     |
| $\log(1 + S_t/V_t)$ | 0.018  | 0.054 | -0.619 | 0.470  | 0.031  | 0.123  | -0.132 | 0.815     |
| $S_t/V_t$           | 0.020  | 0.054 | -0.457 | 0.279  | 0.031  | 0.130  | -0.123 | 0.820     |
| $T_t/V_t$           | 0.574  | 0.285 | 0.076  | -1.294 | 0.646  | 1.173  | 0.127  | 0.971     |
| $X_t/V_t$           | 0.554  | 0.283 | 0.043  | -1.275 | 0.562  | 1.170  | 0.114  | 0.975     |
| $fp_t$              | 0.008  | 0.050 | -0.590 | 0.755  | 0.012  | 0.110  | -0.162 | 0.825     |
| $\tau y_t$          | -1.192 | 0.075 | -0.108 | -0.832 | -1.173 | -1.023 | -1.338 | 0.847     |
| $xy_t$              | -1.244 | 0.160 | 0.451  | -0.544 | -1.256 | -0.805 | -1.501 | 0.922     |
| $vy_t$              | -0.486 | 0.605 | 0.512  | -0.918 | -0.746 | 0.926  | -1.370 | 0.988     |
| $T_t/Y_t$           | 0.305  | 0.023 | 0.025  | -0.766 | 0.310  | 0.360  | 0.262  | 0.842     |
| $X_t/Y_t$           | 0.292  | 0.048 | 0.771  | 0.164  | 0.285  | 0.447  | 0.223  | 0.913     |
| $S_t/Y_t$           | 0.013  | 0.038 | -0.742 | 1.840  | 0.015  | 0.097  | -0.130 | 0.806     |
| $V_t/Y_t$           | 0.746  | 0.508 | 1.495  | 2.075  | 0.475  | 2.525  | 0.254  | 0.990     |

## IA.6 Unit root tests and autocorrelation coefficients

| sample    | variable  | $r_t$ | $\Delta x_t$ | $\Delta \tau_t$ | $\Delta v_t$ | $\Delta y_t$ |
|-----------|-----------|-------|--------------|-----------------|--------------|--------------|
| 1841-2022 | t-stat    | -3.70 | -9.06        | -5.73           | -8.76        | -7.77        |
|           | p-value   | 0.004 | 0.000        | 0.000           | 0.000        | 0.000        |
|           | auto-corr | 0.05  | 0.22         | 0.32            | 0.42         | 0.28         |
| 1947-2022 | t-stat    | -6.12 | -10.95       | -5.88           | -5.51        | -8.18        |
|           | p-value   | 0.000 | 0.000        | 0.000           | 0.000        | 0.000        |
|           | auto-corr | 0.30  | 0.19         | 0.23            | 0.44         | 0.07         |

Table IA.12: ADF tests for US samples (1)

| sample    | variable  | $\tau v_t$ | $xv_t$ | $\tau y_t$ | $xy_t$ | $vy_t$ |
|-----------|-----------|------------|--------|------------|--------|--------|
| 1841-2022 | t-stat    | -3.04      | -3.10  | -1.59      | -1.35  | -2.12  |
|           | p-value   | 0.032      | 0.027  | 0.488      | 0.604  | 0.238  |
|           | auto-corr | 0.93       | 0.96   | 0.99       | 0.97   | 0.99   |
| 1947-2022 | t-stat    | -1.64      | -2.67  | -4.68      | -2.22  | -0.87  |
|           | p-value   | 0.462      | 0.079  | 0.000      | 0.199  | 0.797  |
|           | auto-corr | 0.97       | 0.98   | 0.66       | 0.81   | 0.98   |

Table IA.13: ADF tests for US samples (2)

| sample    | variable  | $S_t/V_t$ | $\log(1 + S_t/V_t)$ | $fp_t (r = \mathbb{E} r_t)$ | $fp_t (\rho = 0.980)$ |
|-----------|-----------|-----------|---------------------|-----------------------------|-----------------------|
| 1841-2022 | t-stat    | -4.19     | -2.95               | -5.02                       | -5.13                 |
|           | p-value   | 0.001     | 0.040               | 0.000                       | 0.000                 |
|           | auto-corr | 0.59      | 0.47                | 0.78                        | 0.77                  |
| 1947-2022 | t-stat    | -3.82     | -3.84               | -4.46                       | -3.87                 |
|           | p-value   | 0.003     | 0.002               | 0.000                       | 0.002                 |
|           | auto-corr | 0.67      | 0.67                | 0.75                        | 0.76                  |

Table IA.14: ADF tests for US samples (3)

| sample    | variable  | $T_t/V_t$ | $X_t/V_t$ | $T_t/Y_t$ | $X_t/Y_t$ | $S_t/Y_t$ | $V_t/Y_t$ |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1841-2022 | t-stat    | -5.62     | -4.47     | -0.61     | -1.79     | -6.46     | -1.13     |
|           | p-value   | 0.000     | 0.000     | 0.869     | 0.384     | 0.000     | 0.704     |
|           | auto-corr | 0.87      | 0.90      | 0.99      | 0.94      | 0.74      | 0.99      |
| 1947-2022 | t-stat    | -1.53     | -1.68     | -4.63     | -1.80     | -4.02     | -0.90     |
|           | p-value   | 0.519     | 0.439     | 0.000     | 0.380     | 0.001     | 0.787     |
|           | auto-corr | 0.96      | 0.98      | 0.66      | 0.80      | 0.74      | 0.98      |

Table IA.15: ADF tests for US samples (4)

| sample    | variable  | $r_t$ | $\Delta x_t$ | $\Delta \tau_t$ | $\Delta v_t$ | $\Delta y_t$ |
|-----------|-----------|-------|--------------|-----------------|--------------|--------------|
| 1728-2022 | t-stat    | -4.63 | -8.17        | -15.11          | -11.15       | -17.10       |
|           | p-value   | 0.000 | 0.000        | 0.000           | 0.000        | 0.000        |
|           | auto-corr | 0.25  | 0.31         | 0.12            | 0.40         | -0.00        |
| 1947-2022 | t-stat    | -7.85 | -10.28       | -4.61           | -5.62        | -8.19        |
|           | p-value   | 0.000 | 0.000        | 0.000           | 0.000        | 0.000        |
|           | auto-corr | 0.06  | 0.21         | 0.22            | 0.39         | 0.05         |

Table IA.16: ADF tests for UK samples (1)

| sample    | variable  | $\tau v_t$ | $xv_t$ | $\tau y_t$ | $xy_t$ | $vy_t$ |
|-----------|-----------|------------|--------|------------|--------|--------|
| 1728-2022 | t-stat    | -1.09      | -1.54  | -1.04      | -1.27  | -2.26  |
|           | p-value   | 0.719      | 0.512  | 0.739      | 0.642  | 0.184  |
|           | auto-corr | 0.99       | 0.98   | 0.99       | 0.97   | 0.99   |
| 1947-2022 | t-stat    | -2.07      | -2.47  | -2.33      | -1.03  | -1.91  |
|           | p-value   | 0.257      | 0.123  | 0.163      | 0.741  | 0.326  |
|           | auto-corr | 0.98       | 0.99   | 0.85       | 0.92   | 0.99   |

Table IA.17: ADF tests for UK samples (2)

| sample    | variable  | $S_t/V_t$ | $\log(1 + S_t/V_t)$ | $fp_t$ |
|-----------|-----------|-----------|---------------------|--------|
| 1728-2022 | t-stat    | -5.71     | -5.96               | -6.00  |
|           | p-value   | 0.000     | 0.000               | 0.000  |
|           | auto-corr | 0.84      | 0.81                | 0.90   |
| 1947-2022 | t-stat    | -3.60     | -3.60               | -2.50  |
|           | p-value   | 0.006     | 0.006               | 0.116  |
|           | auto-corr | 0.82      | 0.82                | 0.82   |

Table IA.18: ADF tests for UK samples (3)

| sample    | variable  | $T_t/V_t$ | $X_t/V_t$ | $T_t/Y_t$ | $X_t/Y_t$ | $S_t/Y_t$ | $V_t/Y_t$ |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1728-2022 | t-stat    | -2.85     | -2.25     | -0.50     | -2.03     | -7.08     | -2.56     |
|           | p-value   | 0.052     | 0.189     | 0.893     | 0.274     | 0.000     | 0.101     |
|           | auto-corr | 0.99      | 0.99      | 0.99      | 0.96      | 0.88      | 0.98      |
| 1947-2022 | t-stat    | -1.81     | -1.83     | -2.36     | -1.49     | -2.65     | -0.79     |
|           | p-value   | 0.375     | 0.364     | 0.153     | 0.540     | 0.084     | 0.821     |
|           | auto-corr | 0.97      | 0.98      | 0.84      | 0.91      | 0.81      | 0.99      |

Table IA.19: ADF tests for UK samples (4)

Table IA.20: t-tests for difference between mean growth rates, various samples

The table reports tests of differences in means of time series. The difference between two series is regressed against a constant. The test statistics are reported under the null of the intercept being zero. Standard error is Newey-West with 1 lag.

| start year |              | $\Delta\tau_t - \Delta y_t$ | $\Delta x_t - \Delta y_t$ | $\Delta\tau_t - \Delta v_t$ | $\Delta x_t - \Delta v_t$ | $\Delta v_t - \Delta y_t$ | $\Delta\tau_t - \Delta x_t$ |
|------------|--------------|-----------------------------|---------------------------|-----------------------------|---------------------------|---------------------------|-----------------------------|
| USA 1841   | t-stat       | 1.205                       | 0.650                     | -0.704                      | -0.718                    | 1.437                     | 0.038                       |
|            | p-value      | 0.228                       | 0.515                     | 0.481                       | 0.473                     | 0.151                     | 0.969                       |
|            | 1947 t-stat  | 0.384                       | 0.769                     | 0.154                       | 0.630                     | 0.051                     | -0.412                      |
|            | 1947 p-value | 0.701                       | 0.442                     | 0.878                       | 0.529                     | 0.959                     | 0.680                       |
| GBR 1727   | t-stat       | 1.171                       | 0.610                     | 0.679                       | 0.490                     | 0.228                     | -0.202                      |
|            | p-value      | 0.242                       | 0.542                     | 0.497                       | 0.624                     | 0.820                     | 0.840                       |
|            | 1947 t-stat  | 0.117                       | 0.251                     | 0.753                       | 0.899                     | -0.744                    | -0.166                      |
|            | 1947 p-value | 0.907                       | 0.802                     | 0.451                       | 0.369                     | 0.457                     | 0.868                       |

| null    | alternative | test-stat | 90%   | 95%   | 99%   |
|---------|-------------|-----------|-------|-------|-------|
| $r = 0$ | $r \geq 1$  | 40.15     | 13.43 | 15.49 | 19.93 |
| $r = 1$ | $r \geq 2$  | 8.72      | 2.71  | 3.84  | 6.63  |
| $r = 0$ | $r \geq 1$  | 31.42     | 12.30 | 14.26 | 18.52 |
| $r = 1$ | $r \geq 2$  | 8.72      | 2.71  | 3.84  | 6.63  |

Table IA.21: Johansen test for  $(\tau v_t, x v_t)$ , US 1841-2022  
Top panel is trace test and bottom panel is eigenvalue test

| null    | alternative | test-stat | 90%   | 95%   | 99%   |
|---------|-------------|-----------|-------|-------|-------|
| $r = 0$ | $r \geq 1$  | 30.03     | 13.43 | 15.49 | 19.93 |
| $r = 1$ | $r \geq 2$  | 3.57      | 2.71  | 3.84  | 6.63  |
| $r = 0$ | $r \geq 1$  | 26.46     | 12.30 | 14.26 | 18.52 |
| $r = 1$ | $r \geq 2$  | 3.57      | 2.71  | 3.84  | 6.63  |

Table IA.22: Johansen test for  $(\tau v_t, x v_t)$ , US 1947-2022  
Top panel is trace test and bottom panel is eigenvalue test

| null    | alternative | test-stat | 90%   | 95%   | 99%   |
|---------|-------------|-----------|-------|-------|-------|
| $r = 0$ | $r \geq 1$  | 32.11     | 13.43 | 15.49 | 19.93 |
| $r = 1$ | $r \geq 2$  | 1.24      | 2.71  | 3.84  | 6.63  |
| $r = 0$ | $r \geq 1$  | 30.87     | 12.3  | 14.26 | 18.52 |
| $r = 1$ | $r \geq 2$  | 1.24      | 2.71  | 3.84  | 6.63  |

Table IA.23: Johansen test for  $(\tau v_t, x v_t)$ , UK 1728-2022  
Top panel is trace test and bottom panel is eigenvalue test

| null    | alternative | test-stat | 90%   | 95%   | 99%   |
|---------|-------------|-----------|-------|-------|-------|
| $r = 0$ | $r \geq 1$  | 27.24     | 13.43 | 15.49 | 19.93 |
| $r = 1$ | $r \geq 2$  | 3.62      | 2.71  | 3.84  | 6.63  |
| $r = 0$ | $r \geq 1$  | 23.62     | 12.3  | 14.26 | 18.52 |
| $r = 1$ | $r \geq 2$  | 3.62      | 2.71  | 3.84  | 6.63  |

Table IA.24: Johansen test for  $(\tau v_t, x v_t)$ , UK 1947-2022  
Top panel is trace test and bottom panel is eigenvalue test

Table IA.25: Other 14 countries: unit-root tests for returns and growth rates

| country |         | $r_t$  | $\Delta\tau_t$ | $\Delta x_t$ | $\Delta v_t$ | $\Delta y_t$ |
|---------|---------|--------|----------------|--------------|--------------|--------------|
| AUT     | t-stat  | -0.954 | -6.306         | -4.009       | -2.804       | -4.772       |
|         | p-value | 0.770  | 0.000          | 0.001        | 0.058        | 0.000        |
| BEL     | t-stat  | -1.406 | -4.154         | -3.017       | -2.744       | -4.723       |
|         | p-value | 0.580  | 0.001          | 0.033        | 0.067        | 0.000        |
| CAN     | t-stat  | -2.878 | -3.553         | -4.720       | -2.832       | -3.956       |
|         | p-value | 0.048  | 0.007          | 0.000        | 0.054        | 0.002        |
| CHE     | t-stat  | -2.302 | -2.715         | -4.779       | -2.605       | -4.389       |
|         | p-value | 0.171  | 0.071          | 0.000        | 0.092        | 0.000        |
| DEU     | t-stat  | -1.309 | -4.202         | -3.719       | -2.726       | -4.875       |
|         | p-value | 0.625  | 0.001          | 0.004        | 0.070        | 0.000        |
| ESP     | t-stat  | -1.853 | -3.384         | -2.469       | -1.982       | -3.125       |
|         | p-value | 0.355  | 0.012          | 0.123        | 0.295        | 0.025        |
| FIN     | t-stat  | -0.516 | -4.657         | -2.667       | -2.420       | -3.919       |
|         | p-value | 0.889  | 0.000          | 0.080        | 0.136        | 0.002        |
| FRA     | t-stat  | -1.774 | -4.267         | -3.674       | -2.893       | -4.479       |
|         | p-value | 0.393  | 0.001          | 0.004        | 0.046        | 0.000        |
| GRC     | t-stat  | -3.952 | -3.326         | -2.817       | -5.092       | -1.837       |
|         | p-value | 0.002  | 0.014          | 0.056        | 0.000        | 0.362        |
| IRL     | t-stat  | -3.531 | -2.897         | -3.012       | -2.228       | -2.427       |
|         | p-value | 0.007  | 0.046          | 0.034        | 0.196        | 0.134        |
| ITA     | t-stat  | -1.858 | -4.191         | -2.434       | -3.205       | -4.212       |
|         | p-value | 0.352  | 0.001          | 0.132        | 0.020        | 0.001        |
| JPN     | t-stat  | -3.620 | -3.610         | -4.190       | -5.570       | -2.930       |
|         | p-value | 0.005  | 0.006          | 0.001        | 0.000        | 0.042        |
| NLD     | t-stat  | -3.281 | -2.691         | -3.077       | -3.077       | -3.946       |
|         | p-value | 0.016  | 0.076          | 0.028        | 0.028        | 0.002        |
| PRT     | t-stat  | -2.257 | -5.469         | -4.445       | -1.723       | -3.730       |
|         | p-value | 0.186  | 0.000          | 0.000        | 0.419        | 0.004        |

Table IA.26: Other 14 countries: autocorrelations of returns and growth rates

| country | $r_t$  | $\Delta\tau_t$ | $\Delta x_t$ | $\Delta v_t$ | $\Delta y_t$ |
|---------|--------|----------------|--------------|--------------|--------------|
| AUT     | 0.399  | -0.293         | -0.104       | 0.159        | -0.034       |
| BEL     | 0.153  | -0.044         | -0.240       | 0.103        | -0.239       |
| CAN     | 0.154  | 0.271          | -0.079       | 0.263        | 0.109        |
| CHE     | -0.061 | -0.187         | -0.073       | 0.194        | -0.110       |
| DEU     | 0.214  | -0.024         | -0.076       | 0.131        | -0.108       |
| ESP     | 0.375  | 0.199          | 0.266        | 0.579        | 0.100        |
| FIN     | 0.504  | -0.170         | 0.380        | 0.324        | 0.145        |
| FRA     | 0.264  | -0.009         | -0.027       | 0.240        | -0.225       |
| GRC     | -0.007 | 0.185          | 0.511        | -0.175       | 0.458        |
| IRL     | 0.089  | 0.190          | -0.021       | 0.577        | 0.326        |
| ITA     | 0.260  | -0.182         | 0.212        | 0.081        | -0.103       |
| JPN     | 0.210  | 0.390          | -0.370       | 0.050        | 0.420        |
| NLD     | -0.110 | 0.002          | 0.274        | 0.085        | 0.061        |
| PRT     | -0.003 | -0.224         | 0.197        | 0.093        | 0.031        |

Table IA.27: Other 14 countries: unit-root tests for ratios

| country |         | $vy_t$ | $\tau y_t$ | $xy_t$ | $\tau v_t$ | $xv_t$ | $fp_t$ |
|---------|---------|--------|------------|--------|------------|--------|--------|
| AUT     | t-stat  | -1.840 | -1.936     | -2.948 | -1.790     | -1.276 | -2.634 |
|         | p-value | 0.361  | 0.315      | 0.040  | 0.386      | 0.640  | 0.086  |
| BEL     | t-stat  | -2.214 | -1.908     | -1.549 | -2.777     | -1.775 | -1.600 |
|         | p-value | 0.201  | 0.328      | 0.509  | 0.062      | 0.393  | 0.484  |
| CAN     | t-stat  | -1.92  | -1.546     | -2.405 | -2.195     | -1.766 | -2.294 |
|         | p-value | 0.323  | 0.511      | 0.14   | 0.208      | 0.397  | 0.174  |
| CHE     | t-stat  | -0.669 | -1.899     | -3.338 | -0.786     | -0.574 | -3.012 |
|         | p-value | 0.855  | 0.333      | 0.013  | 0.823      | 0.877  | 0.034  |
| DEU     | t-stat  | -2.063 | -0.913     | -2.037 | -1.965     | -0.695 | -3.508 |
|         | p-value | 0.259  | 0.784      | 0.271  | 0.302      | 0.848  | 0.008  |
| ESP     | t-stat  | -1.461 | -2.423     | -1.650 | -1.461     | -2.123 | -2.138 |
|         | p-value | 0.553  | 0.135      | 0.457  | 0.553      | 0.235  | 0.230  |
| FIN     | t-stat  | -1.365 | -2.062     | -1.855 | -1.316     | -1.331 | -2.101 |
|         | p-value | 0.599  | 0.260      | 0.354  | 0.622      | 0.615  | 0.244  |
| FRA     | t-stat  | -1.521 | -1.143     | -1.313 | -1.688     | -1.588 | -2.810 |
|         | p-value | 0.523  | 0.697      | 0.623  | 0.437      | 0.490  | 0.057  |
| GRC     | t-stat  | -0.903 | -0.37      | -1.811 | -1.580     | -1.091 | -3.072 |
|         | p-value | 0.787  | 0.915      | 0.375  | 0.494      | 0.719  | 0.029  |
| IRL     | t-stat  | -1.893 | 0.189      | -0.833 | -1.870     | -1.269 | -2.447 |
|         | p-value | 0.335  | 0.972      | 0.809  | 0.346      | 0.643  | 0.129  |
| ITA     | t-stat  | -1.545 | -1.121     | -1.176 | -1.781     | -1.541 | -2.267 |
|         | p-value | 0.511  | 0.707      | 0.684  | 0.390      | 0.513  | 0.183  |
| JPN     | t-stat  | -0.420 | 0.120      | 0.150  | -0.660     | -0.830 | -0.990 |
|         | p-value | 0.906  | 0.967      | 0.969  | 0.856      | 0.811  | 0.757  |
| NLD     | t-stat  | -1.491 | -2.244     | -3.145 | -1.639     | -1.317 | -3.342 |
|         | p-value | 0.538  | 0.191      | 0.023  | 0.463      | 0.621  | 0.013  |
| PRT     | t-stat  | -1.765 | -1.667     | -2.891 | -1.634     | -1.529 | -2.828 |
|         | p-value | 0.398  | 0.448      | 0.046  | 0.465      | 0.519  | 0.054  |

Table IA.28: Other 14 countries: autocorrelations of ratios

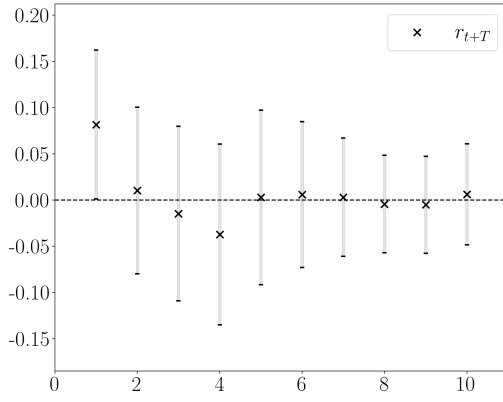
| country | $vy_t$ | $\tau y_t$ | $xy_t$ | $\tau v_t$ | $xv_t$ | $fp_t$ |
|---------|--------|------------|--------|------------|--------|--------|
| AUT     | 0.807  | 0.675      | 0.534  | 0.806      | 0.851  | 0.469  |
| BEL     | 0.670  | 0.778      | 0.847  | 0.573      | 0.804  | 0.814  |
| CAN     | 0.879  | 0.916      | 0.687  | 0.860      | 0.882  | 0.748  |
| CHE     | 0.946  | 0.678      | 0.407  | 0.938      | 0.959  | 0.435  |
| DEU     | 0.774  | 0.819      | 0.662  | 0.772      | 0.861  | 0.498  |
| ESP     | 0.956  | 0.743      | 0.812  | 0.950      | 0.961  | 0.792  |
| FIN     | 0.935  | 0.578      | 0.874  | 0.929      | 0.936  | 0.833  |
| FRA     | 0.954  | 0.913      | 0.846  | 0.939      | 0.962  | 0.635  |
| GRC     | 0.914  | 0.944      | 0.804  | 0.803      | 0.877  | 0.619  |
| IRL     | 0.920  | 0.943      | 0.858  | 0.937      | 0.932  | 0.697  |
| ITA     | 0.878  | 0.855      | 0.822  | 0.838      | 0.869  | 0.697  |
| JPN     | 0.990  | 0.960      | 0.930  | 0.990      | 0.990  | 0.940  |
| NLD     | 0.788  | 0.639      | 0.583  | 0.819      | 0.798  | 0.649  |
| PRT     | 0.963  | 0.889      | 0.662  | 0.948      | 0.968  | 0.454  |

## IA.7 Results for US and UK

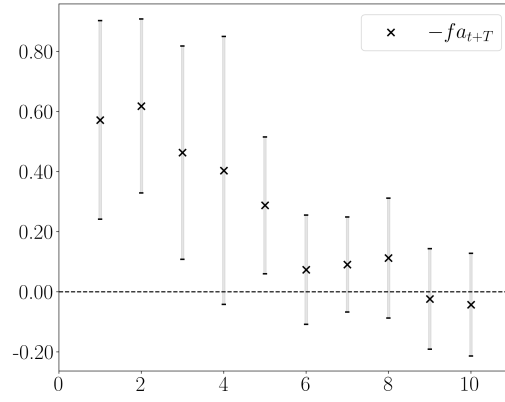
### IA.7.1 Local projections

Figure IA.18: What does the US fiscal position predict?

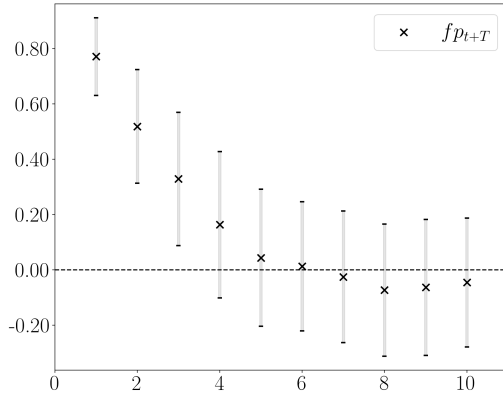
This figure plots estimated slope coefficients (with  $\pm 2$  Newey–West standard error bands) from regressions  $\theta_{t+T} = \alpha + \beta_{\theta,T} fp_t + \varepsilon_{\theta,t+T}$ , for  $T = 1, \dots, 10$ , where the variables  $\theta_{t+T}$  are indicated in the legend of each subfigure. US data 1841–2022,  $\rho = 0.980$ ,  $\beta = 0.952$ .



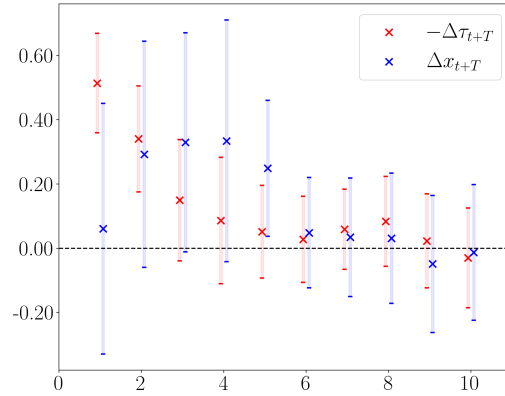
(a) Return



(b) Fiscal Adjustment

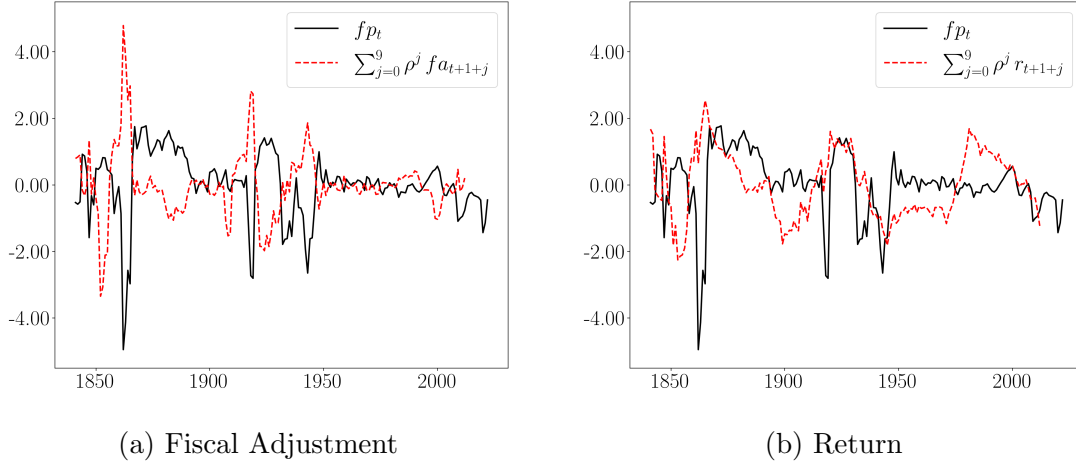


(c) Future  $fp$



(d) Tax and spending growth

Figure IA.19: The fiscal position and subsequent fiscal adjustment and returns. US data 1841–2022,  $\rho = 0.980$ ,  $\beta = 0.952$ .



Newey–West standard errors reported in the main text set lags equal to 2, 5, and 15, respectively, for  $T = 1, 3$  and 10. The standard error for the spending ratio is computed via the delta method using the Newey–West standard errors of  $\beta_{\tau,T}$  and  $\beta_{x,T}$ :

$$\text{s.e. of spending ratio} = \left| \frac{\beta_{\tau,T} \times \text{s.e. of spending}}{(\beta_{x,T} + \beta_{\tau,T})^2} \right| + \left| \frac{\beta_{x,T} \times \text{s.e. of tax}}{(\beta_{x,T} + \beta_{\tau,T})^2} \right|$$

| horizon | return       | fiscal adjustment | future fp      | spending ratio |
|---------|--------------|-------------------|----------------|----------------|
| 1       | 0.2<br>[0.1] | 23.6<br>[10.1]    | 75.7<br>[6.5]  | 11.0<br>[27.5] |
| 3       | 0.2<br>[0.2] | 63.7<br>[20.4]    | 33.3<br>[11.0] | 37.9<br>[16.8] |
| 10      | 0.2<br>[0.5] | 100.4<br>[31.3]   | -3.3<br>[13.5] | 47.2<br>[15.8] |

Table IA.29: Local projection for US data, 1841 to 2022,  $\rho = 0.980$ ,  $\beta = 0.952$

| horizon | return        | fiscal adjustment | future fp      | spending ratio |
|---------|---------------|-------------------|----------------|----------------|
| 1       | -0.2<br>[0.2] | 26.5<br>[11.9]    | 73.9<br>[7.2]  | 69.4<br>[20.9] |
| 3       | -0.1<br>[0.4] | 57.3<br>[24.3]    | 43.2<br>[10.3] | 74.3<br>[22.2] |
| 10      | 1.0<br>[1.6]  | 78.9<br>[45.5]    | 20.7<br>[24.7] | 80.5<br>[29.8] |

Table IA.30: Local projection for US data, 1947 to 2022,  $\rho = 1.010$ ,  $\beta = 1.036$

| horizon | return        | fiscal adjustment | future fp      | spending ratio |
|---------|---------------|-------------------|----------------|----------------|
| 1       | 0.6<br>[0.4]  | 24.6<br>[10.7]    | 74.3<br>[7.5]  | 63.8<br>[20.7] |
| 3       | 0.1<br>[0.9]  | 56.1<br>[24.4]    | 41.7<br>[10.1] | 72.2<br>[23.1] |
| 10      | -1.7<br>[3.0] | 75.2<br>[41.9]    | 20.9<br>[22.4] | 80.1<br>[29.9] |

Table IA.31: Local projection for US data, 1947 to 2022,  $\rho = 0.980$ ,  $\beta = 0.931$

| horizon | return        | fiscal adjustment | future fp      | spending ratio |
|---------|---------------|-------------------|----------------|----------------|
| 1       | -0.1<br>[0.2] | 17.4<br>[8.4]     | 82.6<br>[6.4]  | 85.0<br>[22.1] |
| 3       | -0.8<br>[0.3] | 39.6<br>[16.7]    | 61.0<br>[10.2] | 77.3<br>[22.5] |
| 10      | -2.0<br>[0.8] | 51.6<br>[37.9]    | 49.3<br>[10.8] | 90.1<br>[41.4] |

Table IA.32: Local projection for UK data, 1947 to 2022,  $\rho = 0.991$ ,  $\beta = 0.980$

Table IA.33: More details of covariance between  $fp_t$  and returns, US data

This table reports the components of the product

$$\frac{\text{cov}(\sum_{j=0}^{T-1} \rho^j r_{t+1+j}, fp_t)}{\text{var } fp_t} = \underbrace{\frac{\text{std}(r_t)}{\text{std}(fp_t)}}_{(1)} \times \underbrace{\frac{\text{std}(\sum_{j=0}^{T-1} \rho^j r_{t+1+j})}{\text{std}(r_t)}}_{(2)} \times \underbrace{\text{corr}\left(\sum_{j=0}^{T-1} \rho^j r_{t+1+j}, fp_t\right)}_{(3)}.$$

| Period    | $\rho$ | $\beta$ | $T$ | (1)   | (2)   | (3)    |
|-----------|--------|---------|-----|-------|-------|--------|
| 1841-2022 | 1.006  | 1.014   | 1   | 0.561 | 0.997 | 0.171  |
|           | 1.006  | 1.014   | 3   | 0.561 | 1.705 | 0.105  |
|           | 1.006  | 1.014   | 10  | 0.561 | 3.079 | 0.049  |
|           | 0.980  | 0.952   | 1   | 0.567 | 0.997 | 0.163  |
|           | 0.980  | 0.952   | 3   | 0.567 | 1.664 | 0.088  |
|           | 0.980  | 0.952   | 10  | 0.567 | 2.758 | 0.033  |
|           | 1.010  | 1.036   | 1   | 1.223 | 0.954 | 0.215  |
|           | 1.010  | 1.036   | 3   | 1.223 | 1.857 | 0.029  |
|           | 1.010  | 1.036   | 10  | 1.223 | 4.806 | -0.157 |
| 1947-2022 | 0.980  | 0.931   | 1   | 1.139 | 0.954 | 0.251  |
|           | 0.980  | 0.931   | 3   | 1.139 | 1.797 | 0.090  |
|           | 0.980  | 0.931   | 10  | 1.139 | 4.202 | -0.053 |
|           |        |         |     |       |       |        |

Table IA.34: More details of covariance between  $fp_t$  and returns, UK data

This table reports the components of the product

$$\frac{\text{cov}(\sum_{j=0}^{T-1} \rho^j r_{t+1+j}, fp_t)}{\text{var } fp_t} = \underbrace{\frac{\text{std}(r_t)}{\text{std}(fp_t)}}_{(1)} \times \underbrace{\frac{\text{std}(\sum_{j=0}^{T-1} \rho^j r_{t+1+j})}{\text{std}(r_t)}}_{(2)} \times \underbrace{\text{corr}\left(\sum_{j=0}^{T-1} \rho^j r_{t+1+j}, fp_t\right)}_{(3)}.$$

| Period    | $\rho$ | $\beta$ | $T$ | (1)   | (2)   | (3)    |
|-----------|--------|---------|-----|-------|-------|--------|
| 1727-2022 | 0.997  | 0.975   | 1   | 1.355 | 0.998 | 0.314  |
|           | 0.997  | 0.975   | 3   | 1.355 | 2.064 | 0.368  |
|           | 0.997  | 0.975   | 10  | 1.355 | 4.910 | 0.253  |
| 1947-2022 | 0.991  | 0.980   | 1   | 1.321 | 0.998 | -0.095 |
|           | 0.991  | 0.980   | 3   | 1.321 | 1.755 | -0.346 |
|           | 0.991  | 0.980   | 10  | 1.321 | 3.095 | -0.485 |

### IA.7.2 VAR estimates

Table IA.35: VAR(1) coefficients for US data, 1841 to 2022,  $\rho = 0.980$ ,  $\beta = 0.952$

OLS standard errors are reported in square brackets. The last two columns show imputed coefficients for spending growth and for  $fa_{t+1} = \Delta\tau_{t+1} - \beta\Delta x_{t+1}$

|                | $r_{t+1}$ | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$ | $fp_{t+1}$ | $\Delta x_{t+1}$ | $fa_{t+1}$ |
|----------------|-----------|--------------------|------------------|------------|------------------|------------|
| $r_t$          | 0.095     | 0.201              | 0.037            | 0.080      | 0.013            | 0.189      |
|                | [0.075]   | [0.090]            | [0.033]          | [0.085]    | [0.213]          | [0.200]    |
| $\Delta\tau_t$ | -0.042    | 0.103              | -0.020           | -0.034     | 0.190            | -0.078     |
|                | [0.061]   | [0.074]            | [0.027]          | [0.069]    | [0.174]          | [0.163]    |
| $\Delta y_t$   | 0.119     | 1.171              | 0.305            | 0.175      | 0.793            | 0.415      |
|                | [0.180]   | [0.217]            | [0.078]          | [0.203]    | [0.510]          | [0.480]    |
| $fp_t$         | 0.227     | -0.577             | -0.028           | 0.944      | -0.431           | -0.166     |
|                | [0.067]   | [0.080]            | [0.029]          | [0.075]    | [0.189]          | [0.178]    |
| $fp_{t-1}$     | -0.153    | 0.155              | 0.031            | -0.211     | 0.675            | -0.488     |
|                | [0.079]   | [0.095]            | [0.034]          | [0.089]    | [0.223]          | [0.210]    |
| $R^2$          | 11.02%    | 46.59%             | 10.52%           | 64.81%     | 8.41%            | 15.1%      |

Table IA.36: VAR(1) coefficients for US data, 1947 to 2022,  $\rho = 1.010$ ,  $\beta = 1.036$

OLS standard errors are reported in square brackets. The last two columns show imputed coefficients for spending growth and for  $fa_{t+1} = \Delta\tau_{t+1} - \beta\Delta x_{t+1}$

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.313<br>[0.123]  | -0.103<br>[0.118]  | 0.091<br>[0.054]  | -0.040<br>[0.063] | 0.060<br>[0.202]  | -0.165<br>[0.246] |
| $\Delta\tau_t$ | -0.105<br>[0.115] | 0.177<br>[0.110]   | 0.019<br>[0.050]  | 0.005<br>[0.058]  | 0.151<br>[0.187]  | 0.021<br>[0.229]  |
| $\Delta y_t$   | 0.056<br>[0.279]  | 1.918<br>[0.268]   | 0.267<br>[0.122]  | 0.591<br>[0.141]  | -0.316<br>[0.456] | 2.246<br>[0.557]  |
| $fp_t$         | 0.499<br>[0.252]  | -0.937<br>[0.242]  | -0.282<br>[0.110] | 0.582<br>[0.128]  | 0.617<br>[0.411]  | -1.576<br>[0.503] |
| $fp_{t-1}$     | -0.272<br>[0.242] | 0.587<br>[0.232]   | 0.295<br>[0.106]  | 0.111<br>[0.123]  | 0.155<br>[0.395]  | 0.426<br>[0.483]  |
| $R^2$          | 16.08%            | 52.15%             | 16.84%            | 73.65%            | 21.53%            | 37.13%            |

Table IA.37: VAR(1) coefficients for US data, 1947 to 2022,  $\rho = 0.980$ ,  $\beta = 0.931$

OLS standard errors are reported in square brackets. The last two columns show imputed coefficients for spending growth and for  $fa_{t+1} = \Delta\tau_{t+1} - \beta\Delta x_{t+1}$

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.311<br>[0.121]  | -0.043<br>[0.122]  | 0.074<br>[0.053]  | -0.001<br>[0.074] | -0.068<br>[0.222] | 0.020<br>[0.261]  |
| $\Delta\tau_t$ | -0.105<br>[0.118] | 0.173<br>[0.120]   | 0.033<br>[0.052]  | 0.004<br>[0.072]  | 0.179<br>[0.217]  | 0.006<br>[0.256]  |
| $\Delta y_t$   | 0.053<br>[0.275]  | 1.869<br>[0.279]   | 0.272<br>[0.122]  | 0.600<br>[0.169]  | -0.187<br>[0.506] | 2.042<br>[0.596]  |
| $fp_t$         | 0.476<br>[0.239]  | -0.713<br>[0.242]  | -0.312<br>[0.106] | 0.762<br>[0.147]  | 0.114<br>[0.439]  | -0.819<br>[0.517] |
| $fp_{t-1}$     | -0.227<br>[0.250] | 0.602<br>[0.254]   | 0.309<br>[0.111]  | 0.190<br>[0.154]  | -0.041<br>[0.460] | 0.640<br>[0.542]  |
| $R^2$          | 34.65%            | 47.64%             | 16.49%            | 90.56%            | 2.77%             | 17.57%            |

Table IA.38: VAR(1) coefficients for UK data, 1947 to 2022,  $\rho = 0.991$ ,  $\beta = 0.980$

OLS standard errors are reported in square brackets. The last two columns show imputed coefficients for spending growth and for  $fa_{t+1} = \Delta\tau_{t+1} - \beta\Delta x_{t+1}$

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.097<br>[0.110]  | -0.134<br>[0.066]  | 0.132<br>[0.048]  | -0.092<br>[0.035] | 0.082<br>[0.071]  | -0.214<br>[0.086] |
| $\Delta\tau_t$ | 0.731<br>[0.216]  | 0.241<br>[0.130]   | 0.026<br>[0.095]  | 0.122<br>[0.069]  | -0.060<br>[0.140] | 0.300<br>[0.168]  |
| $\Delta y_t$   | -1.147<br>[0.266] | 0.371<br>[0.161]   | -0.075<br>[0.117] | 0.815<br>[0.085]  | -1.550<br>[0.173] | 1.890<br>[0.208]  |
| $fp_t$         | -0.127<br>[0.286] | -0.097<br>[0.173]  | 0.045<br>[0.126]  | 0.780<br>[0.092]  | 0.451<br>[0.186]  | -0.539<br>[0.223] |
| $fp_{t-1}$     | -0.070<br>[0.290] | -0.123<br>[0.175]  | 0.094<br>[0.128]  | -0.056<br>[0.093] | 0.009<br>[0.189]  | -0.132<br>[0.226] |
| $R^2$          | 32.27%            | 15.90%             | 12.26%            | 87.67%            | 59.08%            | 60.13%            |

### IA.7.3 Variance decomposition of $fp_t$

Table IA.39: Variance decomposition for US data, 1841 to 2022,  $\rho = 0.980$ ,  $\beta = 0.952$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return             | fiscal adjustment      | future fp            | spending ratio       |
|----------|--------------------|------------------------|----------------------|----------------------|
| 1        | 0.3<br>[0.1, 0.4]  | 22.0<br>[15.6, 29.6]   | 78.3<br>[70.7, 84.8] | 5.9<br>[-43.5, 30.9] |
| 3        | 0.4<br>[0.1, 0.8]  | 63.6<br>[50.0, 80.0]   | 36.6<br>[20.3, 50.1] | 33.4<br>[0.4, 57.3]  |
| 10       | 0.5<br>[-0.1, 1.3] | 98.4<br>[91.0, 100.9]  | 1.7<br>[-0.7, 8.6]   | 44.4<br>[14.0, 72.9] |
| $\infty$ | 0.5<br>[-0.1, 1.4] | 100.1<br>[99.2, 100.6] | 0.0<br>[0.0, 0.0]    | 44.8<br>[14.7, 72.8] |

Table IA.40: Variance decomposition for US data, 1947 to 2022,  $\rho = 1.010$ ,  $\beta = 1.036$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return              | fiscal adjustment       | future fp            | spending ratio         |
|----------|---------------------|-------------------------|----------------------|------------------------|
| 1        | -0.3<br>[-0.5, 0.0] | 25.4<br>[17.2, 36.5]    | 76.2<br>[65.1, 84.3] | 81.0<br>[64.6, 103.6]  |
| 3        | -0.6<br>[-1.2, 0.1] | 56.3<br>[32.6, 82.2]    | 45.6<br>[20.3, 69.0] | 85.5<br>[53.6, 123.6]  |
| 10       | -1.1<br>[-2.6, 0.3] | 89.7<br>[56.8, 102.1]   | 12.8<br>[0.9, 44.7]  | 101.5<br>[52.0, 174.2] |
| $\infty$ | -1.3<br>[-4.8, 0.5] | 102.6<br>[100.9, 106.1] | 0.0<br>[0.0, 0.0]    | 104.3<br>[52.2, 208.5] |

Table IA.41: Variance decomposition for US data, 1947 to 2022,  $\rho = 0.980$ ,  $\beta = 0.931$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return              | fiscal adjustment    | future fp             | spending ratio           |
|----------|---------------------|----------------------|-----------------------|--------------------------|
| 1        | 0.6<br>[0.3, 0.8]   | 3.4<br>[-1.0, 11.0]  | 97.4<br>[89.8, 101.8] | 124.5<br>[-602.8, 701.8] |
| 3        | 1.8<br>[1.1, 2.7]   | 14.4<br>[6.8, 31.9]  | 85.1<br>[67.1, 92.7]  | 58.2<br>[-61.8, 128.9]   |
| 10       | 5.7<br>[3.2, 9.0]   | 31.4<br>[16.3, 66.9] | 64.2<br>[29.2, 77.0]  | 59.4<br>[-97.7, 155.7]   |
| $\infty$ | 17.6<br>[6.3, 37.8] | 83.7<br>[63.6, 95.0] | 0.0<br>[0.0, 0.0]     | 60.3<br>[-128.6, 185.6]  |

Table IA.42: Variance decomposition for UK data, 1947 to 2022,  $\rho = 0.991$ ,  $\beta = 0.98$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return               | fiscal adjustment       | future fp            | spending ratio        |
|----------|----------------------|-------------------------|----------------------|-----------------------|
| 1        | -0.1<br>[-0.3, 0.0]  | 18.1<br>[10.1, 25.4]    | 83.4<br>[76.0, 91.4] | 77.9<br>[53.4, 122.6] |
| 3        | -0.8<br>[-1.3, -0.2] | 46.9<br>[22.8, 72.9]    | 55.2<br>[29.3, 79.2] | 64.4<br>[37.7, 115.3] |
| 10       | -1.8<br>[-2.9, -0.6] | 91.6<br>[50.9, 106.4]   | 11.5<br>[-3.5, 53.4] | 63.2<br>[28.0, 125.4] |
| $\infty$ | -2.1<br>[-6.0, -0.6] | 103.4<br>[102.0, 107.3] | 0.0<br>[0.0, 0.0]    | 63.0<br>[27.1, 127.6] |

#### IA.7.4 Unexpected tax and spending news

Table IA.43: Variance decomposition for short-run tax news, US data, 1841 to 2022,  $\rho = 0.980$ ,  $\beta = 0.952$

| horizon  | return                | surplus                  | future fp               | spending ratio             |
|----------|-----------------------|--------------------------|-------------------------|----------------------------|
| 1        | 0.58<br>[0.48, 0.67]  | 54.80<br>[49.52, 58.99]  | 41.40<br>[37.00, 47.05] | 100.00<br>[100.00, 100.00] |
| 3        | 0.71<br>[0.08, 1.43]  | 70.67<br>[34.69, 103.28] | 25.40<br>[-7.17, 61.39] | 116.00<br>[88.26, 153.27]  |
| 10       | 0.74<br>[-0.06, 1.72] | 94.89<br>[86.33, 97.85]  | 1.14<br>[-1.27, 9.46]   | 102.10<br>[65.06, 142.32]  |
| $\infty$ | 0.74<br>[-0.07, 1.74] | 96.03<br>[95.10, 96.89]  | 0.00<br>[0.00, 0.00]    | 101.69<br>[62.77, 142.32]  |

Table IA.44: Variance decomposition for short-run spending news, US data, 1841 to 2022,  $\rho = 0.980$ ,  $\beta = 0.952$

| horizon  | return                   | surplus                   | future fp                | spending ratio             |
|----------|--------------------------|---------------------------|--------------------------|----------------------------|
| 1        | -0.19<br>[-0.23, -0.13 ] | 11.86<br>[10.81, 12.91 ]  | 89.61<br>[88.51, 90.64 ] | 0.00<br>[0.00, 0.00 ]      |
| 3        | 0.39<br>[0.05, 0.77 ]    | 40.62<br>[21.21, 55.22 ]  | 60.28<br>[45.61, 79.94 ] | -40.92<br>[-187.06, 3.51 ] |
| 10       | 0.56<br>[-0.11, 1.41 ]   | 97.63<br>[85.13, 102.62 ] | 3.1<br>[-1.92, 15.11 ]   | 16.45<br>[-24.49, 40.07 ]  |
| $\infty$ | 0.56<br>[-0.12, 1.53 ]   | 100.73<br>[99.77, 101.4 ] | 0.00<br>[0.00, 0.00]     | 18.02<br>[-19.78, 40.79 ]  |

Table IA.45: Variance decomposition for short-run tax news, US data, 1947 to 2022,  $\rho = 1.010$ ,  $\beta = 1.036$

| horizon  | return                | surplus                   | future fp                 | spending ratio                |
|----------|-----------------------|---------------------------|---------------------------|-------------------------------|
| 1        | 1.30<br>[1.09, 1.51]  | -3.48<br>[-16.03, 7.16]   | 103.47<br>[93.28, 115.45] | 100.00<br>[100.00, 100.00]    |
| 3        | 1.50<br>[0.42, 2.87]  | 24.68<br>[-36.57, 71.22]  | 75.12<br>[28.74, 134.88]  | 207.10<br>[-1335.81, 1265.93] |
| 10       | 0.85<br>[-1.37, 3.64] | 81.81<br>[33.4, 98.71]    | 18.64<br>[1.51, 65.52]    | 139.17<br>[87.51, 381.87]     |
| $\infty$ | 0.58<br>[-3.89, 4.07] | 100.72<br>[97.28, 105.01] | 0.00<br>[0.00, 0.00]      | 136.31<br>[86.33, 300.78]     |

Table IA.46: Variance decomposition for short-run spending news, US data, 1947 to 2022,  $\rho = 1.010$ ,  $\beta = 1.036$

| horizon  | return                  | surplus                     | future fp                  | spending ratio            |
|----------|-------------------------|-----------------------------|----------------------------|---------------------------|
| 1        | 0.18<br>[0.05, 0.32 ]   | -1.12<br>[-4.91, 2.43 ]     | 102.43<br>[98.96, 106.13 ] | 0.00<br>[0.00, 0.00 ]     |
| 3        | -0.54<br>[-1.25, 0.18 ] | 62.19<br>[31.98, 87.24 ]    | 39.84<br>[15.04, 69.70 ]   | 52.87<br>[20.71, 79.73 ]  |
| 10       | -1.10<br>[-2.76, 0.17 ] | 89.9<br>[60.08, 101.69 ]    | 12.68<br>[1.4, 42.47 ]     | 79.33<br>[42.39, 130.12 ] |
| $\infty$ | -1.28<br>[-4.48, 0.43 ] | 102.77<br>[101.04, 105.94 ] | 0.00<br>[0.00, 0.00]       | 84.90<br>[45.09, 186.86 ] |

Table IA.47: Variance decomposition for short-run tax news, US data, 1947 to 2022,  $\rho = 0.980$ ,  $\beta = 0.931$

| horizon  | return                  | surplus                    | future fp                  | spending ratio               |
|----------|-------------------------|----------------------------|----------------------------|------------------------------|
| 1        | -2.18<br>[-2.61, -1.76] | -22.03<br>[-29.43, -10.28] | 127.38<br>[114.64, 135.28] | 100.00<br>[100.00, 100.00]   |
| 3        | -1.82<br>[-4.17, 0.14]  | -7.71<br>[-50.19, 39.15]   | 112.70<br>[64.41, 156.18]  | -97.49<br>[-1258.11, 958.55] |
| 10       | 3.07<br>[-1.06, 6.93]   | 17.52<br>[-16.18, 66.03]   | 82.58<br>[35.10, 116.87]   | 111.55<br>[-701.91, 629.16]  |
| $\infty$ | 18.38<br>[2.10, 40.44]  | 84.79<br>[62.7, 100.65]    | 0.00<br>[0.00, 0.00]       | 71.30<br>[-132.18, 264.67]   |

Table IA.48: Variance decomposition for short-run spending news, US data, 1947 to 2022,  $\rho = 0.980$ ,  $\beta = 0.931$

| horizon  | return                  | surplus                   | future fp                   | spending ratio              |
|----------|-------------------------|---------------------------|-----------------------------|-----------------------------|
| 1        | -0.37<br>[-0.67, -0.1 ] | -9.02<br>[-12.19, -4.55 ] | 110.57<br>[105.93, 113.83 ] | 0.00<br>[0.00, 0.00]        |
| 3        | 1.24<br>[-0.29, 2.62 ]  | 27.42<br>[-5.06, 55.23 ]  | 72.52<br>[44.13, 105.63 ]   | 24.72<br>[-191.22, 165.53 ] |
| 10       | 4.78<br>[2.14, 7.86 ]   | 40.32<br>[15.99, 74.53 ]  | 56.08<br>[22.14, 79.51 ]    | 30.84<br>[-112.55, 102.49 ] |
| $\infty$ | 15.18<br>[4.44, 30.79 ] | 86.00<br>[70.42, 96.6 ]   | 0.00<br>[0.00, 0.00]        | 46.76<br>[-82.8, 166.83 ]   |

Table IA.49: Variance decomposition for short-run tax news, UK data, 1947 to 2022,  $\rho = 0.991$ ,  $\beta = 0.980$

| horizon  | return                 | surplus                   | future fp                | spending ratio                |
|----------|------------------------|---------------------------|--------------------------|-------------------------------|
| 1        | 0.01<br>[-0.17, 0.20]  | 22.98<br>[17.89, 28.55]   | 77.92<br>[72.15, 83.08]  | 100.00<br>[100.00, 100.00]    |
| 3        | 1.27<br>[0.33, 2.32]   | 6.75<br>[-41.7, 48.84]    | 92.89<br>[51.39, 141.49] | 389.05<br>[-1646.35, 1112.76] |
| 10       | -0.84<br>[-2.55, 0.7]  | 77.64<br>[16.38, 107.1]   | 24.11<br>[-4.94, 85.0]   | 83.06<br>[34.74, 241.37]      |
| $\infty$ | -1.39<br>[-7.42, 0.58] | 102.3<br>[100.37, 108.31] | 0.00<br>[0.00, 0.00]     | 77.77<br>[35.3, 166.53]       |

Table IA.50: Variance decomposition for short-run spending news, UK data, 1947 to 2022,  
 $\rho = 0.991$ ,  $\beta = 0.980$

| horizon  | return                   | surplus                     | future fp                | spending ratio           |
|----------|--------------------------|-----------------------------|--------------------------|--------------------------|
| 1        | -0.14<br>[-0.35, 0.06 ]  | 23.06<br>[17.26, 28.75 ]    | 78.32<br>[72.61, 84.13 ] | 0.00<br>[0.00, 0.00 ]    |
| 3        | -0.61<br>[-1.17, 0.01 ]  | 80.33<br>[51.20, 109.63 ]   | 21.52<br>[-7.82, 50.19 ] | 47.65<br>[27.12, 62.43 ] |
| 10       | -1.11<br>[-1.95, -0.43 ] | 97.87<br>[78.92, 106.04 ]   | 4.48<br>[-3.90, 23.81 ]  | 50.09<br>[27.59, 67.34 ] |
| $\infty$ | -1.22<br>[-2.86, -0.46 ] | 102.46<br>[101.69, 104.14 ] | 0.00<br>[0.00, 0.00 ]    | 50.57<br>[26.9, 75.15 ]  |



### IA.7.5 Sensitivity analysis of $\rho$ and $\beta$

Table IA.51: Sensitivity analysis for variance decomposition of  $fp_t$ , using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1841 to 2022.

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.025 | 1.025   | 6.69          | 0.652           | -0.1   | 100.7             | 52.6           |
| 1.010  | 0.025 | 1.004   | 134.20        | 0.604           | 0.0    | 100.6             | 49.4           |
| 1.010  | 0.025 | 1.114   | 10.41         | 0.894           | -1.0   | 101.6             | 67.5           |
| 1.005  | 0.030 | 1.013   | 6.45          | 0.623           | 0.0    | 100.6             | 51.3           |
| 1.005  | 0.030 | 1.002   | 132.01        | 0.602           | 0.0    | 100.6             | 49.7           |
| 1.005  | 0.030 | 1.058   | 10.07         | 0.790           | -0.2   | 100.8             | 59.7           |
| 0.999  | 0.036 | 0.997   | 6.22          | 0.596           | 0.0    | 100.5             | 49.6           |
| 0.999  | 0.036 | 1.000   | 129.42        | 0.599           | 0.0    | 100.6             | 50.0           |
| 0.999  | 0.036 | 0.988   | 9.81          | 0.597           | 0.0    | 100.5             | 47.7           |
| 0.995  | 0.040 | 0.988   | 6.11          | 0.591           | 0.1    | 100.5             | 48.5           |
| 0.995  | 0.040 | 0.998   | 127.70        | 0.597           | 0.0    | 100.5             | 50.1           |
| 0.995  | 0.040 | 0.942   | 9.74          | 0.765           | 0.6    | 100.0             | 38.6           |
| 0.990  | 0.045 | 0.975   | 6.01          | 0.601           | 0.1    | 100.4             | 47.1           |
| 0.990  | 0.045 | 0.995   | 125.58        | 0.595           | 0.0    | 100.5             | 50.3           |
| 0.990  | 0.045 | 0.883   | 9.76          | 0.905           | 2.6    | 98.0              | 28.0           |
| 0.980  | 0.055 | 0.952   | 5.94          | 0.654           | 0.5    | 100.1             | 44.7           |
| 0.980  | 0.055 | 0.991   | 121.41        | 0.588           | 0.0    | 100.5             | 50.7           |
| 0.980  | 0.055 | 0.764   | 10.23         | 0.978           | 11.6   | 88.9              | 25.1           |
| 0.970  | 0.065 | 0.931   | 6.05          | 0.713           | 1.2    | 99.3              | 42.8           |
| 0.970  | 0.065 | 0.986   | 117.34        | 0.579           | 0.0    | 100.5             | 51.1           |
| 0.970  | 0.065 | 0.642   | 11.32         | 0.993           | 18.5   | 82.1              | 44.4           |
| 0.960  | 0.076 | 0.912   | 6.31          | 0.761           | 2.3    | 98.2              | 41.7           |
| 0.960  | 0.076 | 0.981   | 113.36        | 0.565           | 0.1    | 100.5             | 51.4           |
| 0.960  | 0.076 | 0.518   | 13.12         | 0.997           | 20.8   | 79.8              | 62.0           |

Table IA.52: Sensitivity analysis for variance decomposition of  $fp_t$ , using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1947 to 2022.

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.020 | 1.038   | 0.07          | 0.825           | -1.4   | 102.7             | 104.6          |
| 1.010  | 0.020 | 1.015   | 0.48          | 0.789           | -0.6   | 102.0             | 99.2           |
| 1.010  | 0.020 | 1.084   | 0.14          | 0.929           | -2.6   | 104.0             | 112.5          |
| 1.005  | 0.025 | 1.021   | 0.03          | 0.796           | -0.7   | 102.1             | 101.0          |
| 1.005  | 0.025 | 1.007   | 0.47          | 0.796           | -0.3   | 101.7             | 97.0           |
| 1.005  | 0.025 | 1.042   | 0.06          | 0.857           | -1.0   | 102.3             | 105.9          |
| 0.999  | 0.031 | 0.995   | 0.01          | 0.827           | 0.3    | 101.1             | 92.7           |
| 0.999  | 0.031 | 0.999   | 0.48          | 0.816           | 0.1    | 101.3             | 94.1           |
| 0.999  | 0.031 | 0.991   | 0.03          | 0.844           | 0.5    | 100.8             | 91.0           |
| 0.995  | 0.035 | 0.976   | 0.02          | 0.9             | 2.2    | 99.1              | 83.7           |
| 0.995  | 0.035 | 0.993   | 0.49          | 0.833           | 0.4    | 100.9             | 91.9           |
| 0.995  | 0.035 | 0.957   | 0.04          | 0.958           | 6.6    | 94.7              | 67.5           |
| 0.990  | 0.040 | 0.956   | 0.07          | 0.951           | 7.1    | 94.2              | 71.4           |
| 0.990  | 0.040 | 0.985   | 0.51          | 0.858           | 1.1    | 100.2             | 89.0           |
| 0.990  | 0.040 | 0.914   | 0.10          | 0.995           | 29.6   | 71.7              | 14.6           |
| 0.980  | 0.050 | 0.931   | 0.22          | 0.98            | 17.5   | 83.8              | 60.5           |
| 0.980  | 0.050 | 0.97    | 0.59          | 0.907           | 3.8    | 97.5              | 82.7           |
| 0.980  | 0.050 | 0.827   | 0.36          | 1.004           | 40.2   | 61.2              | 53.9           |
| 0.970  | 0.061 | 0.917   | 0.45          | 0.987           | 23.3   | 78.0              | 62.4           |
| 0.970  | 0.061 | 0.954   | 0.71          | 0.943           | 8.8    | 92.5              | 76.7           |
| 0.970  | 0.061 | 0.737   | 0.82          | 1.003           | 32.6   | 68.8              | 84.2           |
| 0.960  | 0.071 | 0.907   | 0.72          | 0.991           | 26.3   | 75.0              | 66.8           |
| 0.960  | 0.071 | 0.938   | 0.88          | 0.967           | 15.4   | 86.0              | 72.6           |
| 0.960  | 0.071 | 0.646   | 1.52          | 1.002           | 28.8   | 72.6              | 92.3           |

Table IA.53: Sensitivity analysis for variance decomposition of  $fp_t$ , using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1727 to 2022.

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.008 | 1.11    | 2.25          | 0.950           | -5.9   | 106.2             | 96.4           |
| 1.010  | 0.008 | 1.008   | 85.44         | 0.823           | -0.3   | 100.6             | 88.0           |
| 1.010  | 0.008 | 1.157   | 2.32          | 0.968           | -10.9  | 111.2             | 100.3          |
| 1.005  | 0.013 | 1.051   | 1.59          | 0.906           | -1.7   | 102.0             | 92.3           |
| 1.005  | 0.013 | 1.004   | 82.17         | 0.817           | -0.1   | 100.5             | 88.0           |
| 1.005  | 0.013 | 1.079   | 1.67          | 0.936           | -2.8   | 103.1             | 94.8           |
| 0.999  | 0.019 | 0.992   | 1.15          | 0.789           | 0.2    | 100.1             | 87.3           |
| 0.999  | 0.019 | 0.999   | 78.37         | 0.809           | 0.0    | 100.3             | 88.0           |
| 0.999  | 0.019 | 0.984   | 1.36          | 0.766           | 0.4    | 100.0             | 86.3           |
| 0.995  | 0.023 | 0.963   | 1.04          | 0.733           | 0.8    | 99.5              | 84.6           |
| 0.995  | 0.023 | 0.996   | 75.91         | 0.804           | 0.1    | 100.3             | 88.0           |
| 0.995  | 0.023 | 0.920   | 1.45          | 0.854           | 2.1    | 98.3              | 78.4           |
| 0.990  | 0.028 | 0.938   | 1.06          | 0.763           | 1.6    | 98.7              | 82.2           |
| 0.990  | 0.028 | 0.991   | 72.93         | 0.797           | 0.2    | 100.2             | 87.9           |
| 0.990  | 0.028 | 0.84    | 1.90          | 0.967           | 6.6    | 93.7              | 69.8           |
| 0.980  | 0.038 | 0.907   | 1.50          | 0.837           | 3.5    | 96.8              | 79.9           |
| 0.980  | 0.038 | 0.983   | 67.24         | 0.782           | 0.2    | 100.1             | 87.7           |
| 0.980  | 0.038 | 0.676   | 4.06          | 0.995           | 15.4   | 85.0              | 78.4           |
| 0.970  | 0.048 | 0.887   | 2.36          | 0.871           | 5.7    | 94.7              | 79.5           |
| 0.970  | 0.048 | 0.974   | 61.95         | 0.765           | 0.3    | 100.0             | 87.5           |
| 0.970  | 0.048 | 0.510   | 8.08          | 0.998           | 16.4   | 83.9              | 89.8           |
| 0.960  | 0.058 | 0.873   | 3.53          | 0.889           | 7.8    | 92.5              | 79.8           |
| 0.960  | 0.058 | 0.964   | 57.05         | 0.746           | 0.4    | 100.0             | 87.2           |
| 0.960  | 0.058 | 0.339   | 14.34         | 0.999           | 15.8   | 84.5              | 95.3           |

Table IA.54: Sensitivity analysis for variance decomposition of  $fp_t$ , using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1947 to 2022.

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.014 | 1.032   | 0.10          | 0.925           | -0.6   | 102.0             | 81.2           |
| 1.010  | 0.014 | 1.008   | 1.11          | 0.865           | 0.4    | 101.0             | 70.8           |
| 1.010  | 0.014 | 1.078   | 0.15          | 0.971           | -12.0  | 113.4             | 97.8           |
| 1.005  | 0.019 | 1.015   | 0.08          | 0.893           | 0.6    | 100.8             | 76.2           |
| 1.005  | 0.019 | 1.004   | 1.04          | 0.857           | 0.3    | 101.1             | 70.8           |
| 1.005  | 0.019 | 1.039   | 0.13          | 0.946           | -0.8   | 102.1             | 87.7           |
| 0.999  | 0.025 | 0.997   | 0.06          | 0.842           | -0.2   | 101.6             | 69.6           |
| 0.999  | 0.025 | 0.999   | 0.97          | 0.848           | -0.1   | 101.4             | 70.6           |
| 0.999  | 0.025 | 0.992   | 0.14          | 0.821           | -0.7   | 102.1             | 66.1           |
| 0.995  | 0.029 | 0.987   | 0.06          | 0.816           | -1.2   | 102.6             | 65.9           |
| 0.995  | 0.029 | 0.996   | 0.92          | 0.842           | -0.4   | 101.7             | 70.4           |
| 0.995  | 0.029 | 0.961   | 0.18          | 0.907           | -5.7   | 107.1             | 45.4           |
| 0.990  | 0.034 | 0.977   | 0.07          | 0.804           | -2.3   | 103.7             | 62.1           |
| 0.990  | 0.034 | 0.991   | 0.86          | 0.834           | -0.8   | 102.2             | 70.1           |
| 0.990  | 0.034 | 0.921   | 0.25          | 0.982           | -6.9   | 108.3             | 35.7           |
| 0.980  | 0.044 | 0.962   | 0.09          | 0.821           | -3.0   | 104.4             | 57.8           |
| 0.980  | 0.044 | 0.983   | 0.76          | 0.818           | -1.9   | 103.2             | 69.0           |
| 0.980  | 0.044 | 0.840   | 0.51          | 0.997           | 10.8   | 90.5              | 73.1           |
| 0.970  | 0.054 | 0.950   | 0.13          | 0.849           | -1.6   | 103.0             | 56.2           |
| 0.970  | 0.054 | 0.974   | 0.67          | 0.802           | -2.8   | 104.2             | 67.7           |
| 0.970  | 0.054 | 0.757   | 0.92          | 0.998           | 17.4   | 84.0              | 88.9           |
| 0.960  | 0.065 | 0.940   | 0.17          | 0.870           | 1.2    | 100.1             | 56.2           |
| 0.960  | 0.065 | 0.964   | 0.60          | 0.790           | -3.3   | 104.6             | 66.1           |
| 0.960  | 0.065 | 0.673   | 1.51          | 0.998           | 19.7   | 81.7              | 94.0           |

Table IA.55: Sensitivity analysis for variance decomposition of short term tax news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1841 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.025 | 1.025   | 6.69          | 0.652           | -0.3   | 102.9             | 107.2          |
| 1.010  | 0.025 | 1.004   | 134.20        | 0.604           | -0.1   | 101.3             | 105.4          |
| 1.010  | 0.025 | 1.114   | 10.41         | 0.894           | -2.1   | 110.2             | 109.7          |
| 1.005  | 0.030 | 1.013   | 6.45          | 0.623           | -0.1   | 101.7             | 106.5          |
| 1.005  | 0.030 | 1.002   | 132.01        | 0.602           | 0.0    | 100.9             | 105.6          |
| 1.005  | 0.030 | 1.058   | 10.07         | 0.790           | -0.6   | 105.1             | 109.0          |
| 0.999  | 0.036 | 0.997   | 6.22          | 0.596           | 0.0    | 100.3             | 105.5          |
| 0.999  | 0.036 | 1.000   | 129.42        | 0.599           | 0.0    | 100.5             | 105.7          |
| 0.999  | 0.036 | 0.988   | 9.81          | 0.597           | 0.1    | 99.7              | 104.0          |
| 0.995  | 0.040 | 0.988   | 6.11          | 0.591           | 0.1    | 99.4              | 104.7          |
| 0.995  | 0.040 | 0.998   | 127.70        | 0.597           | 0.0    | 100.2             | 105.7          |
| 0.995  | 0.040 | 0.942   | 9.74          | 0.765           | 1.0    | 95.7              | 94.2           |
| 0.990  | 0.045 | 0.975   | 6.01          | 0.601           | 0.3    | 98.3              | 103.6          |
| 0.990  | 0.045 | 0.995   | 125.58        | 0.595           | 0.0    | 99.8              | 105.8          |
| 0.990  | 0.045 | 0.883   | 9.76          | 0.905           | 3.6    | 90.1              | 73.2           |
| 0.980  | 0.055 | 0.952   | 5.94          | 0.654           | 0.8    | 96.0              | 101.6          |
| 0.980  | 0.055 | 0.991   | 121.41        | 0.588           | 0.1    | 99.1              | 106.0          |
| 0.980  | 0.055 | 0.764   | 10.23         | 0.978           | 14.5   | 74.8              | 66.0           |
| 0.970  | 0.065 | 0.931   | 6.05          | 0.713           | 1.6    | 93.6              | 99.6           |
| 0.970  | 0.065 | 0.986   | 117.34        | 0.579           | 0.1    | 98.3              | 106.1          |
| 0.970  | 0.065 | 0.642   | 11.32         | 0.993           | 22.6   | 63.1              | 96.2           |
| 0.960  | 0.076 | 0.912   | 6.31          | 0.761           | 2.8    | 91.1              | 97.8           |
| 0.960  | 0.076 | 0.981   | 113.36        | 0.565           | 0.1    | 97.5              | 106.1          |
| 0.960  | 0.076 | 0.518   | 13.12         | 0.997           | 25.3   | 57.6              | 121.4          |

Table IA.56: Sensitivity analysis for variance decomposition of short term tax news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.020 | 1.038   | 0.074         | 0.825           | 0.6    | 100.7             | 136.3          |
| 1.010  | 0.020 | 1.015   | 0.488         | 0.789           | 0.1    | 101.9             | 132.8          |
| 1.010  | 0.020 | 1.084   | 0.141         | 0.929           | 1.8    | 97.4              | 133.6          |
| 1.005  | 0.025 | 1.021   | 0.034         | 0.796           | 0.4    | 100.9             | 134.8          |
| 1.005  | 0.025 | 1.007   | 0.478         | 0.796           | 0.1    | 101.6             | 130.5          |
| 1.005  | 0.025 | 1.042   | 0.068         | 0.857           | 1.4    | 99.4              | 134.9          |
| 0.999  | 0.031 | 0.995   | 0.018         | 0.827           | 0.0    | 101.4             | 125.4          |
| 0.999  | 0.031 | 0.999   | 0.481         | 0.816           | 0.0    | 101.3             | 127.3          |
| 0.999  | 0.031 | 0.991   | 0.035         | 0.844           | 0.1    | 101.4             | 122.7          |
| 0.995  | 0.035 | 0.976   | 0.029         | 0.900           | 1.4    | 100.3             | 109.9          |
| 0.995  | 0.035 | 0.993   | 0.491         | 0.833           | 0.1    | 101.0             | 124.6          |
| 0.995  | 0.035 | 0.957   | 0.048         | 0.958           | 6.0    | 96.5              | 81.8           |
| 0.990  | 0.040 | 0.956   | 0.071         | 0.951           | 6.4    | 95.9              | 88.6           |
| 0.990  | 0.040 | 0.985   | 0.513         | 0.858           | 0.4    | 100.5             | 120.3          |
| 0.990  | 0.040 | 0.914   | 0.104         | 0.995           | 33.8   | 70.4              | 7.2            |
| 0.980  | 0.050 | 0.931   | 0.228         | 0.980           | 18.2   | 84.9              | 71.6           |
| 0.980  | 0.050 | 0.970   | 0.590         | 0.907           | 2.7    | 98.1              | 109.7          |
| 0.980  | 0.050 | 0.827   | 0.361         | 1.004           | 44.2   | 62.6              | 58.2           |
| 0.970  | 0.061 | 0.917   | 0.455         | 0.987           | 24.6   | 78.9              | 73.5           |
| 0.970  | 0.061 | 0.954   | 0.713         | 0.943           | 7.9    | 93.2              | 99.1           |
| 0.970  | 0.061 | 0.737   | 0.825         | 1.003           | 30.5   | 78.2              | 95.7           |
| 0.960  | 0.071 | 0.907   | 0.728         | 0.991           | 27.6   | 75.9              | 79.0           |
| 0.960  | 0.071 | 0.938   | 0.885         | 0.967           | 15.0   | 86.5              | 91.6           |
| 0.960  | 0.071 | 0.646   | 1.521         | 1.002           | 21.6   | 88.5              | 104.7          |

Table IA.57: Sensitivity analysis for variance decomposition of short term tax news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1727 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.008 | 1.110   | 2.25          | 0.950           | -6.8   | 115.5             | 105.4          |
| 1.010  | 0.008 | 1.008   | 85.44         | 0.823           | -0.4   | 101.3             | 105.0          |
| 1.010  | 0.008 | 1.157   | 2.32          | 0.968           | -10.9  | 123.7             | 106.5          |
| 1.005  | 0.013 | 1.051   | 1.59          | 0.906           | -2.6   | 107.0             | 105.0          |
| 1.005  | 0.013 | 1.004   | 82.17         | 0.817           | -0.2   | 100.9             | 104.9          |
| 1.005  | 0.013 | 1.079   | 1.67          | 0.936           | -4.1   | 110.7             | 105.3          |
| 0.999  | 0.019 | 0.992   | 1.15          | 0.789           | 0.4    | 99.3              | 104.8          |
| 0.999  | 0.019 | 0.999   | 78.37         | 0.809           | 0.0    | 100.2             | 104.8          |
| 0.999  | 0.019 | 0.984   | 1.36          | 0.766           | 0.7    | 98.3              | 104.7          |
| 0.995  | 0.023 | 0.963   | 1.04          | 0.733           | 1.7    | 95.7              | 104.3          |
| 0.995  | 0.023 | 0.996   | 75.91         | 0.804           | 0.2    | 99.8              | 104.7          |
| 0.995  | 0.023 | 0.920   | 1.45          | 0.854           | 3.8    | 90.6              | 102.6          |
| 0.990  | 0.028 | 0.938   | 1.06          | 0.763           | 2.9    | 92.5              | 103.6          |
| 0.990  | 0.028 | 0.991   | 72.93         | 0.797           | 0.4    | 99.2              | 104.6          |
| 0.990  | 0.028 | 0.840   | 1.90          | 0.967           | 8.5    | 81.5              | 96.7           |
| 0.980  | 0.038 | 0.907   | 1.50          | 0.837           | 4.8    | 88.4              | 102.3          |
| 0.980  | 0.038 | 0.983   | 67.24         | 0.782           | 0.8    | 97.8              | 104.3          |
| 0.980  | 0.038 | 0.676   | 4.06          | 0.995           | 18.4   | 65.1              | 99.9           |
| 0.970  | 0.048 | 0.887   | 2.36          | 0.871           | 6.5    | 85.7              | 101.2          |
| 0.970  | 0.048 | 0.974   | 61.95         | 0.765           | 1.1    | 96.4              | 103.9          |
| 0.970  | 0.048 | 0.510   | 8.08          | 0.998           | 26.0   | 54.6              | 104.7          |
| 0.960  | 0.058 | 0.873   | 3.53          | 0.889           | 8.2    | 83.4              | 100.4          |
| 0.960  | 0.058 | 0.964   | 57.05         | 0.746           | 1.6    | 94.8              | 103.5          |
| 0.960  | 0.058 | 0.339   | 14.34         | 0.999           | 35.1   | 47.6              | 104.3          |

Table IA.58: Sensitivity analysis for variance decomposition of short term tax news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.014 | 1.032   | 0.10          | 0.925           | -3.4   | 105.0             | 98.8           |
| 1.010  | 0.014 | 1.008   | 1.11          | 0.865           | -0.1   | 102.0             | 87.2           |
| 1.010  | 0.014 | 1.078   | 0.15          | 0.971           | -22.9  | 124.3             | 116.2          |
| 1.005  | 0.019 | 1.015   | 0.08          | 0.893           | -0.4   | 101.9             | 93.7           |
| 1.005  | 0.019 | 1.004   | 1.04          | 0.857           | 0.0    | 101.6             | 87.5           |
| 1.005  | 0.019 | 1.039   | 0.13          | 0.946           | -4.0   | 105.5             | 106.6          |
| 0.999  | 0.025 | 0.997   | 0.06          | 0.842           | -0.1   | 101.4             | 86.3           |
| 0.999  | 0.025 | 0.999   | 0.97          | 0.848           | 0.0    | 101.3             | 87.5           |
| 0.999  | 0.025 | 0.992   | 0.14          | 0.821           | -0.5   | 101.8             | 81.8           |
| 0.995  | 0.029 | 0.987   | 0.06          | 0.816           | -0.8   | 101.9             | 81.6           |
| 0.995  | 0.029 | 0.996   | 0.92          | 0.842           | -0.2   | 101.3             | 87.4           |
| 0.995  | 0.029 | 0.961   | 0.18          | 0.907           | -4.9   | 106.2             | 53.1           |
| 0.990  | 0.034 | 0.977   | 0.07          | 0.804           | -1.6   | 102.4             | 76.7           |
| 0.990  | 0.034 | 0.991   | 0.86          | 0.834           | -0.5   | 101.3             | 87.0           |
| 0.990  | 0.034 | 0.921   | 0.25          | 0.982           | -3.7   | 105.1             | 36.1           |
| 0.980  | 0.044 | 0.962   | 0.09          | 0.821           | -1.4   | 101.7             | 71.0           |
| 0.980  | 0.044 | 0.983   | 0.76          | 0.818           | -1.3   | 101.3             | 85.6           |
| 0.980  | 0.044 | 0.840   | 0.51          | 0.997           | 24.3   | 77.2              | 89.5           |
| 0.970  | 0.054 | 0.950   | 0.13          | 0.849           | 1.4    | 98.5              | 68.4           |
| 0.970  | 0.054 | 0.974   | 0.67          | 0.802           | -1.7   | 101.0             | 83.8           |
| 0.970  | 0.054 | 0.757   | 0.92          | 0.998           | 37.6   | 63.9              | 119.0          |
| 0.960  | 0.065 | 0.940   | 0.17          | 0.870           | 6.1    | 93.4              | 68.1           |
| 0.960  | 0.065 | 0.964   | 0.60          | 0.790           | -1.4   | 100.0             | 81.7           |
| 0.960  | 0.065 | 0.673   | 1.51          | 0.998           | 45.2   | 56.6              | 131.2          |

Table IA.59: Sensitivity analysis for variance decomposition of short term spending news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1841 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.025 | 1.025   | 6.69          | 0.652           | -0.2   | 100.4             | 24.9           |
| 1.010  | 0.025 | 1.004   | 134.20        | 0.604           | 0.0    | 101.2             | 21.9           |
| 1.010  | 0.025 | 1.114   | 10.41         | 0.894           | -1.2   | 97.5              | 39.6           |
| 1.005  | 0.030 | 1.013   | 6.45          | 0.623           | -0.1   | 100.4             | 23.7           |
| 1.005  | 0.030 | 1.002   | 132.01        | 0.602           | 0.0    | 100.9             | 22.2           |
| 1.005  | 0.030 | 1.058   | 10.07         | 0.790           | -0.3   | 98.6              | 31.6           |
| 0.999  | 0.036 | 0.997   | 6.22          | 0.596           | 0.0    | 100.6             | 22.2           |
| 0.999  | 0.036 | 1.000   | 129.42        | 0.599           | 0.0    | 100.5             | 22.5           |
| 0.999  | 0.036 | 0.988   | 9.81          | 0.597           | 0.1    | 101.0             | 20.6           |
| 0.995  | 0.040 | 0.988   | 6.11          | 0.591           | 0.1    | 100.7             | 21.3           |
| 0.995  | 0.040 | 0.998   | 127.70        | 0.597           | 0.0    | 100.2             | 22.8           |
| 0.995  | 0.040 | 0.942   | 9.74          | 0.765           | 0.6    | 102.5             | 12.7           |
| 0.990  | 0.045 | 0.975   | 6.01          | 0.601           | 0.2    | 100.8             | 20.1           |
| 0.990  | 0.045 | 0.995   | 125.58        | 0.595           | 0.0    | 99.9              | 23.0           |
| 0.990  | 0.045 | 0.883   | 9.76          | 0.905           | 2.6    | 103.3             | 3.6            |
| 0.980  | 0.055 | 0.952   | 5.94          | 0.654           | 0.6    | 100.7             | 18.0           |
| 0.980  | 0.055 | 0.991   | 121.41        | 0.588           | 0.1    | 99.1              | 23.5           |
| 0.980  | 0.055 | 0.764   | 10.23         | 0.978           | 10.9   | 101.5             | -2.5           |
| 0.970  | 0.065 | 0.931   | 6.05          | 0.713           | 1.2    | 100.4             | 16.3           |
| 0.970  | 0.065 | 0.986   | 117.34        | 0.579           | 0.1    | 98.4              | 24.0           |
| 0.970  | 0.065 | 0.642   | 11.32         | 0.993           | 17.6   | 102.8             | 5.0            |
| 0.960  | 0.076 | 0.912   | 6.31          | 0.761           | 2.2    | 99.6              | 15.3           |
| 0.960  | 0.076 | 0.981   | 113.36        | 0.565           | 0.1    | 97.6              | 24.4           |
| 0.960  | 0.076 | 0.518   | 13.12         | 0.997           | 20.1   | 108.1             | 7.3            |

Table IA.60: Sensitivity analysis for variance decomposition of short term spending news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.020 | 1.038   | 0.07          | 0.825           | -1.3   | 102.8             | 85.2           |
| 1.010  | 0.020 | 1.015   | 0.48          | 0.789           | -0.6   | 102.6             | 79.7           |
| 1.010  | 0.020 | 1.084   | 0.14          | 0.929           | -2.3   | 103.1             | 95.8           |
| 1.005  | 0.025 | 1.021   | 0.03          | 0.796           | -0.7   | 102.1             | 81.4           |
| 1.005  | 0.025 | 1.007   | 0.47          | 0.796           | -0.3   | 102.0             | 77.6           |
| 1.005  | 0.025 | 1.042   | 0.06          | 0.857           | -1.0   | 102.0             | 87.0           |
| 0.999  | 0.031 | 0.995   | 0.01          | 0.827           | 0.3    | 101.1             | 73.8           |
| 0.999  | 0.031 | 0.999   | 0.48          | 0.816           | 0.1    | 101.2             | 74.9           |
| 0.999  | 0.031 | 0.991   | 0.03          | 0.844           | 0.5    | 101.0             | 72.3           |
| 0.995  | 0.035 | 0.976   | 0.02          | 0.9             | 2.1    | 99.3              | 66.4           |
| 0.995  | 0.035 | 0.993   | 0.49          | 0.833           | 0.4    | 100.6             | 73.0           |
| 0.995  | 0.035 | 0.957   | 0.04          | 0.958           | 5.8    | 95.8              | 53.5           |
| 0.990  | 0.040 | 0.956   | 0.07          | 0.951           | 6.3    | 95.1              | 56.5           |
| 0.990  | 0.040 | 0.985   | 0.51          | 0.858           | 1.1    | 99.7              | 70.5           |
| 0.990  | 0.040 | 0.914   | 0.10          | 0.995           | 24.9   | 76.9              | 10.3           |
| 0.980  | 0.050 | 0.931   | 0.22          | 0.98            | 15.1   | 86.1              | 46.9           |
| 0.980  | 0.050 | 0.970   | 0.59          | 0.907           | 3.6    | 96.7              | 65.1           |
| 0.980  | 0.050 | 0.827   | 0.36          | 1.004           | 32.3   | 70.1              | 40.0           |
| 0.970  | 0.061 | 0.917   | 0.45          | 0.987           | 20.0   | 80.8              | 47.9           |
| 0.970  | 0.061 | 0.954   | 0.71          | 0.943           | 8.0    | 91.9              | 59.8           |
| 0.970  | 0.061 | 0.737   | 0.82          | 1.003           | 25.0   | 77.8              | 60.1           |
| 0.960  | 0.071 | 0.907   | 0.72          | 0.991           | 22.5   | 77.7              | 50.9           |
| 0.960  | 0.071 | 0.938   | 0.88          | 0.967           | 13.7   | 85.7              | 55.9           |
| 0.960  | 0.071 | 0.646   | 1.52          | 1.002           | 21.2   | 81.7              | 61.1           |

Table IA.61: Sensitivity analysis for variance decomposition of short term spending news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1727 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.008 | 1.110   | 2.25          | 0.950           | -7.9   | 107.7             | 80.8           |
| 1.010  | 0.008 | 1.008   | 85.44         | 0.823           | -0.4   | 101.4             | 66.8           |
| 1.010  | 0.008 | 1.157   | 2.32          | 0.968           | -14.3  | 113.7             | 87.3           |
| 1.005  | 0.013 | 1.051   | 1.59          | 0.906           | -2.4   | 102.4             | 73.7           |
| 1.005  | 0.013 | 1.004   | 82.17         | 0.817           | -0.2   | 100.9             | 66.7           |
| 1.005  | 0.013 | 1.079   | 1.67          | 0.936           | -3.9   | 103.7             | 77.7           |
| 0.999  | 0.019 | 0.992   | 1.15          | 0.789           | 0.3    | 100.1             | 65.5           |
| 0.999  | 0.019 | 0.999   | 78.37         | 0.809           | 0.0    | 100.2             | 66.6           |
| 0.999  | 0.019 | 0.984   | 1.36          | 0.766           | 0.6    | 99.9              | 64.1           |
| 0.995  | 0.023 | 0.963   | 1.04          | 0.733           | 1.3    | 99.2              | 61.5           |
| 0.995  | 0.023 | 0.996   | 75.91         | 0.804           | 0.1    | 99.8              | 66.5           |
| 0.995  | 0.023 | 0.920   | 1.45          | 0.854           | 3.2    | 97.9              | 53.4           |
| 0.990  | 0.028 | 0.938   | 1.06          | 0.763           | 2.5    | 98.0              | 58.1           |
| 0.990  | 0.028 | 0.991   | 72.93         | 0.797           | 0.3    | 99.3              | 66.4           |
| 0.990  | 0.028 | 0.840   | 1.90          | 0.967           | 9.2    | 92.6              | 41.5           |
| 0.980  | 0.038 | 0.907   | 1.50          | 0.837           | 5.0    | 95.3              | 54.5           |
| 0.980  | 0.038 | 0.983   | 67.24         | 0.782           | 0.4    | 98.3              | 66.1           |
| 0.980  | 0.038 | 0.676   | 4.06          | 0.995           | 21.7   | 81.3              | 39.8           |
| 0.970  | 0.048 | 0.887   | 2.36          | 0.871           | 7.6    | 92.2              | 53.1           |
| 0.970  | 0.048 | 0.974   | 61.95         | 0.765           | 0.6    | 97.2              | 65.8           |
| 0.970  | 0.048 | 0.510   | 8.08          | 0.998           | 28.3   | 73.5              | 30.2           |
| 0.960  | 0.058 | 0.873   | 3.53          | 0.889           | 10.1   | 89.2              | 52.6           |
| 0.960  | 0.058 | 0.964   | 57.05         | 0.746           | 0.7    | 96.1              | 65.4           |
| 0.960  | 0.058 | 0.339   | 14.34         | 0.999           | 34.3   | 49.1              | -19.2          |

Table IA.62: Sensitivity analysis for variance decomposition of short term spending news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return. Two boundary values of  $\beta$  are considered by setting  $a$  to reflect the maximum and minimum of  $T_t/V_t$  in-sample and imputing the value of  $b$  given  $\rho$  using  $b = 1 + a - \rho^{-1}$ ; then computing  $\beta = b/a$ .

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment | spending ratio |
|--------|-------|---------|---------------|-----------------|--------|-------------------|----------------|
| 1.010  | 0.014 | 1.032   | 0.10          | 0.925           | -0.6   | 102.2             | 68.3           |
| 1.010  | 0.014 | 1.008   | 1.11          | 0.865           | 0.2    | 101.6             | 58.0           |
| 1.010  | 0.014 | 1.078   | 0.15          | 0.971           | -8.9   | 110.8             | 84.6           |
| 1.005  | 0.019 | 1.015   | 0.08          | 0.893           | 0.4    | 101.1             | 62.1           |
| 1.005  | 0.019 | 1.004   | 1.04          | 0.857           | 0.2    | 101.4             | 57.1           |
| 1.005  | 0.019 | 1.039   | 0.13          | 0.946           | -0.8   | 102.3             | 73.7           |
| 0.999  | 0.025 | 0.997   | 0.06          | 0.842           | -0.1   | 101.5             | 55.2           |
| 0.999  | 0.025 | 0.999   | 0.97          | 0.848           | 0.0    | 101.4             | 56.0           |
| 0.999  | 0.025 | 0.992   | 0.14          | 0.821           | -0.5   | 101.9             | 52.9           |
| 0.995  | 0.029 | 0.987   | 0.06          | 0.816           | -0.7   | 102.0             | 52.4           |
| 0.995  | 0.029 | 0.996   | 0.92          | 0.842           | -0.2   | 101.3             | 55.2           |
| 0.995  | 0.029 | 0.961   | 0.18          | 0.907           | -2.9   | 104.2             | 46.0           |
| 0.990  | 0.034 | 0.977   | 0.07          | 0.804           | -1.4   | 102.6             | 50.0           |
| 0.990  | 0.034 | 0.991   | 0.86          | 0.834           | -0.5   | 101.3             | 54.4           |
| 0.990  | 0.034 | 0.921   | 0.25          | 0.982           | -2.7   | 103.2             | 45.5           |
| 0.980  | 0.044 | 0.962   | 0.09          | 0.821           | -1.6   | 102.7             | 47.6           |
| 0.980  | 0.044 | 0.983   | 0.76          | 0.818           | -1.1   | 101.1             | 52.8           |
| 0.980  | 0.044 | 0.840   | 0.51          | 0.997           | 7.4    | 91.4              | 64.8           |
| 0.970  | 0.054 | 0.950   | 0.13          | 0.849           | -0.4   | 101.4             | 47.3           |
| 0.970  | 0.054 | 0.974   | 0.67          | 0.802           | -1.4   | 100.7             | 51.2           |
| 0.970  | 0.054 | 0.757   | 0.92          | 0.998           | 10.2   | 84.6              | 67.0           |
| 0.960  | 0.065 | 0.940   | 0.17          | 0.870           | 2.0    | 98.8              | 47.6           |
| 0.960  | 0.065 | 0.964   | 0.60          | 0.790           | -1.3   | 99.9              | 49.7           |
| 0.960  | 0.065 | 0.673   | 1.51          | 0.998           | 9.6    | 75.1              | 60.8           |

### IA.7.6 Variance decomposition of unexpected returns

Table IA.63: Variance decomposition of unexpected return news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1841 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return.

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment |
|--------|-------|---------|---------------|-----------------|--------|-------------------|
| 1.010  | 0.025 | 1.025   | 6.69          | 0.652           | -3.7   | 71.4              |
| 1.005  | 0.030 | 1.013   | 6.45          | 0.623           | -3.5   | 71.1              |
| 0.999  | 0.036 | 0.997   | 6.22          | 0.596           | -3.8   | 71.0              |
| 0.995  | 0.040 | 0.988   | 6.11          | 0.591           | -4.3   | 70.8              |
| 0.990  | 0.045 | 0.975   | 6.01          | 0.601           | -5.4   | 70.9              |
| 0.980  | 0.055 | 0.952   | 5.94          | 0.654           | -9.0   | 71.6              |
| 0.970  | 0.065 | 0.931   | 6.05          | 0.713           | -14.7  | 73.8              |
| 0.960  | 0.076 | 0.912   | 6.31          | 0.761           | -22.4  | 78.1              |

Table IA.64: Variance decomposition of unexpected return news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , US data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return.

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment |
|--------|-------|---------|---------------|-----------------|--------|-------------------|
| 1.010  | 0.020 | 1.038   | 0.07          | 0.825           | -29.0  | 131.9             |
| 1.005  | 0.025 | 1.021   | 0.03          | 0.796           | -30.2  | 133.9             |
| 0.999  | 0.031 | 0.995   | 0.01          | 0.827           | -21.1  | 125.6             |
| 0.995  | 0.035 | 0.976   | 0.02          | 0.900           | -0.6   | 104.9             |
| 0.990  | 0.040 | 0.956   | 0.07          | 0.951           | 37.8   | 65.7              |
| 0.980  | 0.050 | 0.931   | 0.22          | 0.98            | 81.7   | 18.5              |
| 0.970  | 0.061 | 0.917   | 0.45          | 0.987           | 76.8   | 18.4              |
| 0.960  | 0.071 | 0.907   | 0.72          | 0.991           | 54.4   | 34.4              |

Table IA.65: Variance decomposition of unexpected return news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1727 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return.

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment |
|--------|-------|---------|---------------|-----------------|--------|-------------------|
| 1.010  | 0.008 | 1.110   | 2.25          | 0.950           | -44.8  | 126.8             |
| 1.005  | 0.013 | 1.051   | 1.59          | 0.906           | -37.4  | 120.4             |
| 0.999  | 0.019 | 0.992   | 1.15          | 0.789           | -34.9  | 119.9             |
| 0.995  | 0.023 | 0.963   | 1.04          | 0.733           | -34.7  | 120.7             |
| 0.990  | 0.028 | 0.938   | 1.06          | 0.763           | -36.1  | 123.5             |
| 0.980  | 0.038 | 0.907   | 1.50          | 0.837           | -42.3  | 132.2             |
| 0.970  | 0.048 | 0.887   | 2.36          | 0.871           | -52.0  | 142.2             |
| 0.960  | 0.058 | 0.873   | 3.53          | 0.889           | -64.3  | 152.5             |

Table IA.66: Variance decomposition of unexpected return news, using system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$ , UK data 1947 to 2022

Infinite horizon results using different values of  $\rho$ . We report the sum of squared approximation errors, maximum eigenvalue of the VAR(1) coefficient matrix and implied theoretical mean of return.

| $\rho$ | $r$   | $\beta$ | approx. error | $\lambda_{max}$ | return | fiscal adjustment |
|--------|-------|---------|---------------|-----------------|--------|-------------------|
| 1.010  | 0.014 | 1.032   | 0.10          | 0.925           | -4.4   | 104.3             |
| 1.005  | 0.019 | 1.015   | 0.08          | 0.893           | 18.1   | 82.3              |
| 0.999  | 0.025 | 0.997   | 0.06          | 0.842           | 33.3   | 67.0              |
| 0.995  | 0.029 | 0.987   | 0.06          | 0.816           | 37.5   | 62.9              |
| 0.990  | 0.034 | 0.977   | 0.07          | 0.804           | 38.1   | 62.5              |
| 0.980  | 0.044 | 0.962   | 0.09          | 0.821           | 29.0   | 70.8              |
| 0.970  | 0.054 | 0.950   | 0.13          | 0.849           | 9.7    | 88.0              |
| 0.960  | 0.065 | 0.940   | 0.17          | 0.870           | -16.7  | 111.9             |

## IA.8 Results for Canada, Japan, Switzerland and 11 Eurozone countries

### IA.8.1 VAR estimates

Table IA.67: VAR coefficient estimates. AUT data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$        | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.433<br>[0.268] | -0.164<br>[0.116]  | -0.175<br>[0.101] | 0.008<br>[0.126]  | -0.181<br>[0.152] | 0.016<br>[0.224]  |
| $\Delta\tau_t$ | 0.833<br>[0.840] | -0.883<br>[0.364]  | -0.788<br>[0.316] | -0.552<br>[0.396] | -0.030<br>[0.475] | -0.852<br>[0.702] |
| $\Delta y_t$   | 0.049<br>[0.904] | 0.649<br>[0.392]   | 0.437<br>[0.341]  | 0.916<br>[0.426]  | -0.781<br>[0.511] | 1.425<br>[0.756]  |
| $fp_t$         | 0.363<br>[0.712] | -0.281<br>[0.309]  | -0.048<br>[0.268] | 0.378<br>[0.336]  | 0.695<br>[0.403]  | -0.971<br>[0.595] |
| $fp_{t-1}$     | 1.681<br>[0.768] | -0.268<br>[0.333]  | -0.470<br>[0.289] | -0.133<br>[0.362] | -0.073<br>[0.434] | -0.195<br>[0.642] |
| $R^2$          | 53.62%           | 44.32%             | 43.21%            | 42.05%            | 30.21%            | 39.96%            |

Table IA.68: VAR coefficient estimates. BEL data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$ | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$ | $fp_{t+1}$ | $\Delta x_{t+1}$ | $fa_{t+1}$ |
|----------------|-----------|--------------------|------------------|------------|------------------|------------|
| $r_t$          | -0.040    | -0.214             | -0.280           | -0.157     | 0.183            | -0.396     |
|                | [0.320]   | [0.136]            | [0.105]          | [0.081]    | [0.177]          | [0.232]    |
| $\Delta\tau_t$ | 0.238     | 0.241              | 0.119            | 0.270      | -0.44            | 0.682      |
|                | [0.676]   | [0.288]            | [0.222]          | [0.171]    | [0.374]          | [0.490]    |
| $\Delta y_t$   | -1.491    | -0.410             | -0.527           | -0.289     | 0.316            | -0.727     |
|                | [0.960]   | [0.408]            | [0.315]          | [0.243]    | [0.531]          | [0.695]    |
| $fp_t$         | 1.729     | -0.316             | -0.030           | 0.586      | 0.730            | -1.047     |
|                | [1.238]   | [0.527]            | [0.407]          | [0.314]    | [0.684]          | [0.897]    |
| $fp_{t-1}$     | -0.631    | 0.293              | 0.123            | 0.283      | -0.421           | 0.715      |
|                | [1.117]   | [0.475]            | [0.367]          | [0.283]    | [0.618]          | [0.809]    |
| $R^2$          | 31.00%    | 16.25%             | 28.67%           | 78.12%     | 24.30%           | 32.70%     |

Table IA.69: VAR coefficient estimates. CAN data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.184<br>[0.172]  | -0.120<br>[0.087]  | -0.280<br>[0.073] | -0.474<br>[0.164] | 0.504<br>[0.188]  | -0.598<br>[0.227] |
| $\Delta\tau_t$ | -0.626<br>[0.461] | 0.388<br>[0.232]   | 0.328<br>[0.194]  | 0.760<br>[0.438]  | -0.576<br>[0.502] | 0.934<br>[0.606]  |
| $\Delta y_t$   | 0.023<br>[0.681]  | 0.021<br>[0.343]   | 0.428<br>[0.287]  | 0.444<br>[0.649]  | -0.560<br>[0.743] | 0.552<br>[0.896]  |
| $fp_t$         | 0.711<br>[0.383]  | -0.135<br>[0.193]  | -0.366<br>[0.161] | 0.330<br>[0.365]  | 0.745<br>[0.418]  | -0.841<br>[0.504] |
| $fp_{t-1}$     | -0.423<br>[0.346] | 0.085<br>[0.174]   | 0.378<br>[0.146]  | 0.452<br>[0.329]  | -0.488<br>[0.377] | 0.548<br>[0.455]  |
| $R^2$          | 34.75%            | 17.95%             | 38.80%            | 70.27%            | 37.22%            | 37.05%            |

Table IA.70: VAR coefficient estimates. CHE data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.145<br>[0.199]  | -0.132<br>[0.119]  | -0.204<br>[0.060] | -0.310<br>[0.132] | 0.171<br>[0.161]  | -0.297<br>[0.147] |
| $\Delta\tau_t$ | -0.661<br>[0.381] | -0.054<br>[0.227]  | 0.042<br>[0.114]  | 0.091<br>[0.252]  | -0.128<br>[0.308] | 0.070<br>[0.281]  |
| $\Delta y_t$   | 1.887<br>[0.903]  | -0.213<br>[0.539]  | -0.150<br>[0.271] | 0.724<br>[0.597]  | -1.007<br>[0.729] | 0.763<br>[0.666]  |
| $fp_t$         | -0.440<br>[0.442] | -0.148<br>[0.264]  | -0.122<br>[0.132] | 0.305<br>[0.292]  | 0.589<br>[0.356]  | -0.720<br>[0.326] |
| $fp_{t-1}$     | 1.030<br>[0.456]  | 0.017<br>[0.272]   | -0.087<br>[0.137] | 0.121<br>[0.302]  | -0.137<br>[0.368] | 0.150<br>[0.337]  |
| $R^2$          | 55.69%            | 24.11%             | 60.20%            | 48.64%            | 37.23%            | 51.77%            |

Table IA.71: VAR coefficient estimates. DEU data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.257<br>[0.263]  | 0.018<br>[0.113]   | -0.063<br>[0.104] | -0.034<br>[0.132] | 0.061<br>[0.122]  | -0.042<br>[0.199] |
| $\Delta\tau_t$ | -1.506<br>[0.964] | 0.151<br>[0.414]   | -0.026<br>[0.380] | 0.293<br>[0.485]  | -0.213<br>[0.448] | 0.361<br>[0.729]  |
| $\Delta y_t$   | -0.228<br>[0.832] | 0.115<br>[0.357]   | -0.109<br>[0.327] | 0.348<br>[0.418]  | -0.349<br>[0.386] | 0.458<br>[0.629]  |
| $fp_t$         | 1.419<br>[0.590]  | -0.385<br>[0.253]  | -0.121<br>[0.232] | 0.363<br>[0.297]  | 0.454<br>[0.274]  | -0.832<br>[0.446] |
| $fp_{t-1}$     | -0.449<br>[0.641] | 0.053<br>[0.275]   | -0.180<br>[0.252] | -0.046<br>[0.322] | 0.123<br>[0.297]  | -0.068<br>[0.484] |
| $R^2$          | 36.61%            | 19.03%             | 15.64%            | 45.38%            | 42.51%            | 38.76%            |

Table IA.72: VAR coefficient estimates. ESP data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.396<br>[0.214]  | 0.035<br>[0.172]   | 0.005<br>[0.145]  | 0.047<br>[0.143]  | -0.043<br>[0.148] | 0.079<br>[0.260]  |
| $\Delta\tau_t$ | -0.863<br>[0.442] | 0.678<br>[0.355]   | 0.534<br>[0.300]  | 0.370<br>[0.295]  | 0.078<br>[0.306]  | 0.601<br>[0.537]  |
| $\Delta y_t$   | -0.136<br>[0.426] | -0.699<br>[0.342]  | -0.359<br>[0.289] | -0.588<br>[0.284] | 0.267<br>[0.294]  | -0.964<br>[0.518] |
| $fp_t$         | 1.223<br>[0.516]  | -0.030<br>[0.413]  | -0.029<br>[0.350] | 1.125<br>[0.343]  | -0.239<br>[0.356] | 0.207<br>[0.626]  |
| $fp_{t-1}$     | -0.970<br>[0.447] | 0.068<br>[0.358]   | 0.157<br>[0.303]  | -0.236<br>[0.298] | 0.465<br>[0.309]  | -0.394<br>[0.543] |
| $R^2$          | 31.73%            | 22.48%             | 20.46%            | 77.19%            | 34.40%            | 30.37%            |

Table IA.73: VAR coefficient estimates. FIN data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.028<br>[0.223]  | -0.043<br>[0.140]  | 0.005<br>[0.124]  | -0.134<br>[0.191] | 0.084<br>[0.070]  | -0.123<br>[0.203] |
| $\Delta\tau_t$ | -0.031<br>[1.033] | -0.297<br>[0.650]  | -0.297<br>[0.573] | -0.145<br>[0.886] | -0.169<br>[0.326] | -0.137<br>[0.943] |
| $\Delta y_t$   | 0.182<br>[0.801]  | 1.184<br>[0.504]   | 0.673<br>[0.445]  | 1.067<br>[0.687]  | 0.202<br>[0.253]  | 0.992<br>[0.732]  |
| $fp_t$         | 0.076<br>[0.702]  | -0.589<br>[0.442]  | -0.159<br>[0.390] | 0.470<br>[0.603]  | -0.063<br>[0.222] | -0.529<br>[0.642] |
| $fp_{t-1}$     | 0.648<br>[0.703]  | 0.501<br>[0.442]   | 0.122<br>[0.390]  | 0.331<br>[0.603]  | 0.172<br>[0.222]  | 0.337<br>[0.642]  |
| $R^2$          | 60.75%            | 29.05%             | 11.07%            | 76.09%            | 54.81%            | 22.27%            |

Table IA.74: VAR coefficient estimates. FRA data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.506<br>[0.326]  | -0.271<br>[0.161]  | -0.326<br>[0.140] | -0.213<br>[0.095] | 0.173<br>[0.074]  | -0.443<br>[0.223] |
| $\Delta\tau_t$ | -0.822<br>[1.391] | 1.616<br>[0.688]   | 1.532<br>[0.597]  | 0.784<br>[0.403]  | -0.020<br>[0.313] | 1.636<br>[0.951]  |
| $\Delta y_t$   | -0.126<br>[0.999] | -1.211<br>[0.494]  | -1.114<br>[0.429] | -0.593<br>[0.289] | 0.032<br>[0.225]  | -1.243<br>[0.683] |
| $fp_t$         | 2.036<br>[1.986]  | -1.619<br>[0.982]  | -1.627<br>[0.853] | 0.217<br>[0.575]  | 0.013<br>[0.448]  | -1.631<br>[1.357] |
| $fp_{t-1}$     | -1.327<br>[2.157] | 1.535<br>[1.066]   | 1.811<br>[0.926]  | 0.748<br>[0.625]  | -0.024<br>[0.486] | 1.558<br>[1.474]  |
| $R^2$          | 33.44%            | 37.95%             | 34.97%            | 80.30%            | 28.88%            | 31.85%            |

Table IA.75: VAR coefficient estimates. GRC data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | -0.047<br>[0.201] | 0.014<br>[0.081]   | 0.077<br>[0.076]  | 0.003<br>[0.052]  | 0.009<br>[0.111]  | 0.005<br>[0.143]  |
| $\Delta\tau_t$ | 1.266<br>[0.779]  | 0.445<br>[0.316]   | 0.543<br>[0.293]  | -0.040<br>[0.203] | 0.521<br>[0.432]  | -0.059<br>[0.554] |
| $\Delta y_t$   | -1.269<br>[0.686] | -0.025<br>[0.278]  | 0.061<br>[0.258]  | -0.088<br>[0.179] | 0.238<br>[0.380]  | -0.255<br>[0.488] |
| $fp_t$         | -0.227<br>[0.910] | -0.780<br>[0.369]  | -0.816<br>[0.343] | 1.109<br>[0.237]  | -1.056<br>[0.504] | 0.241<br>[0.648]  |
| $fp_{t-1}$     | 1.003<br>[1.029]  | 0.710<br>[0.417]   | 0.998<br>[0.387]  | -0.214<br>[0.268] | 1.242<br>[0.570]  | -0.490<br>[0.732] |
| $R^2$          | 23.06%            | 24.85%             | 44.34%            | 83.68%            | 38.87%            | 11.63%            |

Table IA.76: VAR coefficient estimates. IRL data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.127<br>[0.312]  | 0.002<br>[0.158]   | -0.225<br>[0.128] | -0.134<br>[0.185] | 0.193<br>[0.284]  | -0.196<br>[0.301] |
| $\Delta\tau_t$ | 0.118<br>[0.498]  | 0.235<br>[0.252]   | 0.091<br>[0.204]  | 0.271<br>[0.295]  | -0.155<br>[0.453] | 0.394<br>[0.479]  |
| $\Delta y_t$   | -0.138<br>[0.630] | 0.162<br>[0.320]   | -0.108<br>[0.258] | 0.574<br>[0.374]  | -0.646<br>[0.573] | 0.826<br>[0.606]  |
| $fp_t$         | -0.290<br>[0.376] | -0.012<br>[0.191]  | 0.177<br>[0.154]  | 0.682<br>[0.223]  | 0.405<br>[0.342]  | -0.427<br>[0.362] |
| $fp_{t-1}$     | 0.255<br>[0.303]  | -0.007<br>[0.154]  | -0.04<br>[0.124]  | -0.219<br>[0.179] | 0.306<br>[0.275]  | -0.321<br>[0.291] |
| $R^2$          | 5.43%             | 17.22%             | 27.60%            | 69.86%            | 42.87%            | 45.47%            |

Table IA.77: VAR coefficient estimates. IRL data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.026<br>[0.238]  | -0.282<br>[0.158]  | -0.171<br>[0.159] | -0.288<br>[0.139] | 0.212<br>[0.171]  | -0.489<br>[0.266] |
| $\Delta\tau_t$ | -0.630<br>[0.637] | -0.046<br>[0.422]  | -0.080<br>[0.424] | 0.106<br>[0.371]  | -0.217<br>[0.457] | 0.166<br>[0.711]  |
| $\Delta y_t$   | -0.892<br>[0.610] | -0.010<br>[0.404]  | 0.260<br>[0.406]  | -0.285<br>[0.356] | 0.507<br>[0.438]  | -0.505<br>[0.681] |
| $fp_t$         | 2.063<br>[0.544]  | -0.631<br>[0.361]  | -0.729<br>[0.362] | 0.962<br>[0.317]  | -0.617<br>[0.391] | -0.028<br>[0.607] |
| $fp_{t-1}$     | -1.405<br>[0.703] | 0.339<br>[0.467]   | 0.633<br>[0.469]  | -0.074<br>[0.410] | 0.507<br>[0.505]  | -0.156<br>[0.786] |
| $R^2$          | 65.00%            | 40.79%             | 32.26%            | 68.75%            | 24.76%            | 22.65%            |

Table IA.78: VAR coefficient estimates. JPN data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | -0.075<br>[0.166] | -0.066<br>[0.052]  | -0.010<br>[0.036] | -0.145<br>[0.068] | 0.144<br>[0.068]  | -0.197<br>[0.094] |
| $\Delta\tau_t$ | 0.555<br>[0.875]  | 0.476<br>[0.275]   | 0.249<br>[0.188]  | 0.594<br>[0.362]  | -0.291<br>[0.359] | 0.742<br>[0.496]  |
| $\Delta y_t$   | 1.256<br>[1.167]  | 0.573<br>[0.367]   | 0.257<br>[0.251]  | 0.538<br>[0.482]  | -0.253<br>[0.478] | 0.803<br>[0.662]  |
| $fp_t$         | -1.072<br>[0.541] | -0.323<br>[0.17]   | -0.146<br>[0.116] | 0.479<br>[0.224]  | 0.489<br>[0.222]  | -0.769<br>[0.307] |
| $fp_{t-1}$     | 1.266<br>[0.555]  | 0.3<br>[0.175]     | 0.17<br>[0.119]   | 0.534<br>[0.229]  | -0.514<br>[0.228] | 0.769<br>[0.315]  |
| $R^2$          | 27.36%            | 28.91%             | 23.59%            | 96.82%            | 19.07%            | 22.33%            |

Table IA.79: VAR coefficient estimates. NLD data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | -0.150<br>[0.230] | -0.207<br>[0.082]  | -0.155<br>[0.051] | -0.225<br>[0.067] | 0.111<br>[0.078]  | -0.318<br>[0.107] |
| $\Delta\tau_t$ | -0.769<br>[0.825] | 0.12<br>[0.294]    | 0.385<br>[0.184]  | 0.036<br>[0.240]  | 0.064<br>[0.280]  | 0.055<br>[0.384]  |
| $\Delta y_t$   | 0.386<br>[1.328]  | -0.210<br>[0.473]  | 0.009<br>[0.296]  | 0.025<br>[0.386]  | -0.242<br>[0.450] | 0.033<br>[0.619]  |
| $fp_t$         | 0.594<br>[1.096]  | 0.085<br>[0.391]   | -0.340<br>[0.245] | 0.842<br>[0.319]  | 0.304<br>[0.371]  | -0.221<br>[0.510] |
| $fp_{t-1}$     | -0.022<br>[0.825] | -0.053<br>[0.294]  | 0.239<br>[0.184]  | -0.187<br>[0.240] | 0.211<br>[0.279]  | -0.265<br>[0.384] |
| $R^2$          | 10.85%            | 23.24%             | 40.34%            | 69.38%            | 50.21%            | 51.48%            |

Table IA.80: VAR coefficient estimates. PRT data.

OLS standard errors are reported in square brackets.

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | -0.124<br>[0.255] | -0.034<br>[0.152]  | -0.135<br>[0.137] | -0.137<br>[0.128] | 0.243<br>[0.207]  | -0.270<br>[0.278] |
| $\Delta\tau_t$ | -0.696<br>[0.601] | 0.239<br>[0.359]   | 0.208<br>[0.323]  | -0.093<br>[0.301] | 0.451<br>[0.488]  | -0.200<br>[0.656] |
| $\Delta y_t$   | -0.224<br>[0.674] | -0.318<br>[0.403]  | -0.102<br>[0.362] | -0.092<br>[0.338] | -0.138<br>[0.547] | -0.183<br>[0.736] |
| $fp_t$         | 1.149<br>[0.529]  | -0.554<br>[0.316]  | -0.329<br>[0.284] | 0.896<br>[0.265]  | -0.373<br>[0.429] | -0.192<br>[0.578] |
| $fp_{t-1}$     | -1.164<br>[0.552] | 0.483<br>[0.330]   | 0.381<br>[0.296]  | -0.048<br>[0.277] | 0.621<br>[0.448]  | -0.121<br>[0.603] |
| $R^2$          | 19.38%            | 19.42%             | 11.27%            | 75.02%            | 17.35%            | 13.62%            |

### IA.8.2 Variance decomposition of $fp_t$

Variance decomposition of  $fp_t$  based on the system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1})$  of different countries are reported below.

Throughout this section, quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

Table IA.81: Variance decomposition. AUT.

| horizon  | return             | surplus                | future fp              | spending ratio         |
|----------|--------------------|------------------------|------------------------|------------------------|
| 1        | 0.8<br>[0.4, 1.1]  | 57.1<br>[22.4, 96.1]   | 46.6<br>[7.7, 81.4]    | 31.3<br>[−27.0, 55.8]  |
| 3        | 2.3<br>[1.0, 4.2]  | 134.0<br>[54.5, 187.8] | −31.8<br>[−85.3, 47.2] | 28.6<br>[−56.5, 57.2]  |
| 10       | 1.8<br>[0.6, 8.6]  | 105.9<br>[60.6, 157.7] | −3.2<br>[−54.9, 40.2]  | 25.9<br>[−165.6, 56.5] |
| $\infty$ | 1.8<br>[0.7, 15.0] | 102.8<br>[89.5, 103.9] | 0.0<br>[0.0, 0.0]      | 25.0<br>[−217.1, 58.3] |

Table IA.82: Variance decomposition. BEL.

| horizon  | return              | surplus                 | future fp            | spending ratio        |
|----------|---------------------|-------------------------|----------------------|-----------------------|
| 1        | −0.1<br>[−0.1, 0.0] | 31.5<br>[11.4, 53.7]    | 73.1<br>[50.9, 93.2] | 64.5<br>[22.6, 114.2] |
| 3        | −0.2<br>[−0.4, 0.0] | 66.3<br>[23.1, 113.9]   | 38.4<br>[−9.1, 81.5] | 67.7<br>[20.8, 145.7] |
| 10       | −0.3<br>[−0.7, 0.0] | 101.1<br>[45.0, 116.9]  | 3.8<br>[−11.9, 59.8] | 68.5<br>[14.5, 190.0] |
| $\infty$ | −0.3<br>[−1.2, 0.0] | 104.9<br>[104.5, 105.7] | 0.0<br>[0.0, 0.0]    | 68.5<br>[12.8, 213.1] |

Table IA.83: Variance decomposition. CAN.

| horizon  | return             | fiscal adjustment     | future fp             | spending ratio        |
|----------|--------------------|-----------------------|-----------------------|-----------------------|
| 1        | 1.5<br>[0.6, 2.4]  | 27.1<br>[9.0, 45.8]   | 74.6<br>[55.5, 93.0]  | 87.7<br>[65.7, 136.1] |
| 3        | 2.7<br>[0.4, 5.1]  | 69.4<br>[26.7, 111.1] | 31.0<br>[−12.1, 74.3] | 81.0<br>[57.8, 138.4] |
| 10       | 3.7<br>[0.2, 8.4]  | 97.8<br>[50.9, 104.0] | 1.6<br>[−4.3, 47.0]   | 78.1<br>[51.1, 163.8] |
| $\infty$ | 3.8<br>[0.0, 11.5] | 99.4<br>[91.6, 103.1] | 0.0<br>[0.0, 0.0]     | 77.9<br>[50.3, 170.2] |

Table IA.84: Variance decomposition. CHE.

| horizon  | return             | fiscal adjustment      | future fp              | spending ratio        |
|----------|--------------------|------------------------|------------------------|-----------------------|
| 1        | 1.0<br>[−0.4, 2.4] | 57.6<br>[25.8, 88.4]   | 45.9<br>[15.6, 77.3]   | 60.3<br>[3.6, 115.8]  |
| 3        | 3.5<br>[0.1, 7.5]  | 127.1<br>[81.8, 168.8] | −26.1<br>[−68.7, 19.8] | 77.5<br>[31.0, 130.6] |
| 10       | 2.6<br>[−0.1, 6.4] | 104.6<br>[84.9, 131.5] | −2.7<br>[−29.7, 16.5]  | 78.5<br>[34.4, 140.1] |
| $\infty$ | 2.6<br>[−0.1, 6.4] | 102.0<br>[98.1, 104.7] | 0.0<br>[0.0, 0.0]      | 78.5<br>[34.5, 142.7] |

Table IA.85: Variance decomposition. DEU.

| horizon  | return             | surplus                | future fp              | spending ratio        |
|----------|--------------------|------------------------|------------------------|-----------------------|
| 1        | 0.8<br>[−0.1, 1.6] | 56.9<br>[25.8, 89.7]   | 46.9<br>[14.2, 78.0]   | 60.5<br>[40.3, 101.7] |
| 3        | 1.5<br>[−0.8, 4.5] | 141.3<br>[69.1, 187.0] | −38.2<br>[−84.6, 33.7] | 74.6<br>[53.5, 136.2] |
| 10       | 0.8<br>[−1.4, 4.5] | 109.5<br>[68.0, 152.5] | −5.7<br>[−49.1, 34.7]  | 75.8<br>[52.9, 172.0] |
| $\infty$ | 0.8<br>[−1.2, 4.8] | 103.8<br>[99.5, 106.0] | 0.0<br>[0.0, 0.0]      | 75.0<br>[53.2, 181.4] |

Table IA.86: Variance decomposition. ESP.

| horizon  | return              | surplus                 | future fp             | spending ratio         |
|----------|---------------------|-------------------------|-----------------------|------------------------|
| 1        | −0.0<br>[−0.1, 0.1] | 18.3<br>[−0.6, 40.9]    | 86.2<br>[63.6, 105.2] | 90.2<br>[−74.6, 302.7] |
| 3        | 0.0<br>[−0.4, 0.4]  | 61.9<br>[13.2, 123.3]   | 42.6<br>[−18.6, 91.3] | 83.2<br>[38.8, 257.7]  |
| 10       | −0.1<br>[−1.7, 1.3] | 105.8<br>[42.0, 160.5]  | −1.2<br>[−55.0, 62.3] | 81.6<br>[17.6, 294.1]  |
| $\infty$ | −0.1<br>[−4.0, 3.4] | 104.7<br>[101.2, 108.6] | 0.0<br>[0.0, 0.0]     | 81.8<br>[−16.2, 429.5] |

Table IA.87: Variance decomposition. FIN.

| horizon  | return              | surplus              | future fp            | spending ratio        |
|----------|---------------------|----------------------|----------------------|-----------------------|
| 1        | 3.3<br>[2.3, 4.2]   | 20.5<br>[2.4, 38.9]  | 80.8<br>[62.4, 99.0] | 73.0<br>[40.5, 312.2] |
| 3        | 9.3<br>[6.5, 12.4]  | 54.0<br>[7.1, 102.9] | 41.2<br>[−8.0, 87.8] | 91.7<br>[51.9, 409.9] |
| 10       | 15.3<br>[6.5, 29.8] | 86.1<br>[9.0, 106.2] | 3.2<br>[−13.4, 66.6] | 98.0<br>[44.1, 563.3] |
| $\infty$ | 15.8<br>[7.2, 91.8] | 88.8<br>[12.8, 97.4] | 0.0<br>[0.0, 0.0]    | 98.3<br>[44.4, 621.3] |

Table IA.88: Variance decomposition. FRA.

| horizon  | return             | surplus                | future fp             | spending ratio         |
|----------|--------------------|------------------------|-----------------------|------------------------|
| 1        | 0.2<br>[0.0, 0.5]  | 29.1<br>[6.3, 55.0]    | 75.2<br>[49.2, 98.3]  | 5.6<br>[−55.5, 26.5]   |
| 3        | 0.8<br>[0.0, 1.8]  | 75.9<br>[15.9, 142.3]  | 27.8<br>[−38.8, 88.2] | 18.7<br>[−32.1, 45.4]  |
| 10       | 1.2<br>[−0.1, 3.6] | 103.2<br>[31.4, 132.7] | 0.2<br>[−30.1, 71.7]  | 26.4<br>[−30.6, 94.8]  |
| $\infty$ | 1.2<br>[−0.1, 9.5] | 103.4<br>[95.2, 104.6] | 0.0<br>[0.0, 0.0]     | 26.3<br>[−31.0, 126.8] |

Table IA.89: Variance decomposition. GRC.

| horizon  | return              | surplus                | future fp             | spending ratio           |
|----------|---------------------|------------------------|-----------------------|--------------------------|
| 1        | 0.4<br>[−0.9, 1.7]  | 9.8<br>[−11.5, 33.8]   | 94.3<br>[69.9, 115.8] | 46.7<br>[−263.8, 500.8]  |
| 3        | 1.6<br>[−0.8, 4.2]  | 34.1<br>[−8.5, 79.3]   | 68.9<br>[22.9, 111.6] | 83.1<br>[−132.7, 367.7]  |
| 10       | 2.8<br>[−2.7, 9.3]  | 90.9<br>[7.7, 154.1]   | 10.9<br>[−51.4, 92.1] | 108.7<br>[−101.6, 393.3] |
| $\infty$ | 2.7<br>[−4.3, 28.4] | 101.8<br>[75.1, 108.9] | 0.0<br>[0.0, 0.0]     | 112.7<br>[−81.0, 450.9]  |

Table IA.90: Variance decomposition. IRL.

| horizon  | return              | surplus                | future fp             | spending ratio         |
|----------|---------------------|------------------------|-----------------------|------------------------|
| 1        | 0.2<br>[−0.6, 1.0]  | 30.5<br>[6.0, 55.2]    | 73.9<br>[49.2, 98.5]  | 117.2<br>[64.0, 257.3] |
| 3        | −0.1<br>[−2.3, 2.2] | 92.4<br>[29.5, 147.7]  | 12.2<br>[−42.0, 73.6] | 108.6<br>[68.5, 241.4] |
| 10       | −0.3<br>[−3.8, 4.5] | 104.8<br>[55.0, 124.3] | 0.1<br>[−16.9, 45.6]  | 106.8<br>[59.2, 302.7] |
| $\infty$ | −0.3<br>[−3.9, 6.6] | 104.9<br>[97.9, 108.5] | 0.0<br>[0.0, 0.0]     | 106.8<br>[60.0, 315.9] |

Table IA.91: Variance decomposition. ITA.

| horizon  | return              | surplus                | future fp            | spending ratio          |
|----------|---------------------|------------------------|----------------------|-------------------------|
| 1        | 1.3<br>[0.6, 2.0]   | 36.3<br>[9.0, 65.7]    | 67.0<br>[37.5, 94.8] | -3.0<br>[-161.8, 33.8]  |
| 3        | 2.2<br>[0.1, 4.7]   | 96.1<br>[30.2, 163.1]  | 6.2<br>[-61.0, 72.3] | 32.4<br>[-82.5, 73.2]   |
| 10       | 1.6<br>[-1.7, 6.8]  | 102.1<br>[40.5, 136.3] | 0.9<br>[-32.8, 63.1] | 42.4<br>[-92.4, 109.5]  |
| $\infty$ | 1.5<br>[-2.9, 12.9] | 103.0<br>[91.4, 107.5] | 0.0<br>[0.0, 0.0]    | 43.8<br>[-126.4, 122.4] |

Table IA.92: Variance decomposition. JPN.

| horizon  | return               | fiscal adjustment     | future fp             | spending ratio            |
|----------|----------------------|-----------------------|-----------------------|---------------------------|
| 1        | 1.9<br>[0.5, 3.4]    | 1.9<br>[-5.7, 9.6]    | 98.6<br>[90.7, 105.7] | 276.4<br>[-853.3, 1369.0] |
| 3        | 4.8<br>[1.4, 8.7]    | 10.6<br>[-5.5, 26.3]  | 87.1<br>[68.9, 102.0] | 126.1<br>[-19.6, 612.9]   |
| 10       | 11.5<br>[0.2, 20.6]  | 42.6<br>[20.9, 73.8]  | 48.3<br>[16.7, 68.3]  | 79.2<br>[13.3, 153.4]     |
| $\infty$ | 19.6<br>[-1.3, 35.2] | 82.8<br>[67.2, 103.7] | 0.0<br>[0.0, 0.0]     | 70.6<br>[10.3, 114.7]     |

Table IA.93: Variance decomposition. NLD.

| horizon  | return              | surplus                 | future fp             | spending ratio        |
|----------|---------------------|-------------------------|-----------------------|-----------------------|
| 1        | -0.1<br>[-0.4, 0.2] | 46.7<br>[24.2, 70.1]    | 57.9<br>[34.5, 80.4]  | 86.8<br>[52.6, 153.6] |
| 3        | -0.3<br>[-1.0, 0.4] | 113.5<br>[65.8, 156.4]  | -8.7<br>[-51.2, 38.6] | 83.4<br>[50.1, 149.4] |
| 10       | -0.3<br>[-0.8, 0.6] | 104.2<br>[79.4, 115.4]  | 0.6<br>[-10.2, 24.7]  | 80.0<br>[44.9, 172.6] |
| $\infty$ | -0.3<br>[-0.8, 0.7] | 104.8<br>[103.9, 105.4] | 0.0<br>[0.0, 0.0]     | 79.9<br>[45.1, 177.3] |

Table IA.94: Variance decomposition. PRT.

| horizon  | return               | surplus                | future fp             | spending ratio         |
|----------|----------------------|------------------------|-----------------------|------------------------|
| 1        | 0.2<br>[-0.6, 1.0]   | 21.1<br>[-5.0, 52.6]   | 83.2<br>[51.1, 109.5] | 3.4<br>[-448.7, 461.9] |
| 3        | 0.1<br>[-1.4, 1.7]   | 46.7<br>[4.8, 92.6]    | 57.8<br>[11.5, 99.9]  | 53.0<br>[-61.9, 123.6] |
| 10       | -0.6<br>[-4.8, 2.7]  | 86.9<br>[22.0, 110.4]  | 18.3<br>[-5.4, 84.1]  | 70.3<br>[-37.8, 179.3] |
| $\infty$ | -0.9<br>[-22.9, 4.9] | 105.5<br>[99.5, 127.4] | 0.0<br>[0.0, 0.0]     | 73.5<br>[-38.4, 253.8] |

## IA.9 Other state variables

Table IA.95: VAR coefficient estimates for a system that includes the log tax-GDP ratio,  $\tau y_t$ . US data, 1947–2022.

OLS standard errors are reported in square brackets. The last two columns show imputed coefficients for spending growth and for  $fa_{t+1} = \Delta\tau_{t+1} - \beta\Delta x_{t+1}$ .

|                | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\tau y_{t+1}$    | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|----------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| $r_t$          | 0.221<br>[0.123]  | -0.205<br>[0.101]  | 0.033<br>[0.050]  | -0.164<br>[0.074] | -0.239<br>[0.088] | 0.288<br>[0.185]  | -0.492<br>[0.232] |
| $\Delta\tau_t$ | -0.147<br>[0.119] | 0.164<br>[0.097]   | -0.002<br>[0.049] | -0.161<br>[0.072] | 0.166<br>[0.085]  | 0.650<br>[0.178]  | -0.483<br>[0.224] |
| $\Delta y_t$   | 0.221<br>[0.318]  | 1.313<br>[0.260]   | 0.105<br>[0.130]  | 0.619<br>[0.192]  | 1.208<br>[0.228]  | -0.544<br>[0.476] | 1.855<br>[0.599]  |
| $fp_t$         | 0.272<br>[0.183]  | -0.424<br>[0.150]  | -0.074<br>[0.075] | 0.804<br>[0.111]  | -0.350<br>[0.132] | 0.165<br>[0.275]  | -0.589<br>[0.346] |
| $\tau y_t$     | 0.218<br>[0.103]  | -0.268<br>[0.084]  | -0.074<br>[0.042] | 0.080<br>[0.062]  | 0.806<br>[0.074]  | -0.501<br>[0.154] | 0.241<br>[0.193]  |
| $fp_{t-1}$     | -0.082<br>[0.186] | 0.135<br>[0.152]   | 0.138<br>[0.076]  | -0.166<br>[0.112] | -0.004<br>[0.134] | 0.634<br>[0.279]  | -0.498<br>[0.351] |
| $R^2$          | 19.69%            | 57.10%             | 12.91%            | 70.35%            | 74.41%            | 31.37%            | 34.99%            |

Table IA.96: VAR coefficient estimates for a system that includes bond return forecasting variables based on the yield curve. US data, 1947–2022

OLS standard errors are reported in square brackets.

|                           | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $yr_{1,t+1}$      | $spr_{1\rightarrow 10,t+1}$ | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|---------------------------|-------------------|--------------------|-------------------|-------------------|-------------------|-----------------------------|-------------------|-------------------|
| $r_t$                     | −0.019<br>[0.140] | −0.209<br>[0.129]  | −0.040<br>[0.061] | −0.202<br>[0.090] | 0.005<br>[0.041]  | 0.020<br>[0.020]            | 0.397<br>[0.234]  | −0.605<br>[0.284] |
| $\Delta\tau_t$            | −0.033<br>[0.108] | 0.048<br>[0.099]   | −0.003<br>[0.047] | −0.125<br>[0.070] | 0.010<br>[0.032]  | −0.002<br>[0.016]           | 0.424<br>[0.180]  | −0.375<br>[0.219] |
| $\Delta y_t$              | −0.505<br>[0.309] | 1.742<br>[0.284]   | 0.149<br>[0.135]  | 0.428<br>[0.199]  | −0.038<br>[0.091] | −0.132<br>[0.045]           | 0.463<br>[0.516]  | 1.280<br>[0.627]  |
| $fp_t$                    | 0.473<br>[0.169]  | −0.576<br>[0.156]  | −0.108<br>[0.074] | 0.863<br>[0.109]  | 0.166<br>[0.050]  | 0.017<br>[0.025]            | −0.165<br>[0.283] | −0.412<br>[0.343] |
| $yr_{1,t}$                | 1.195<br>[0.299]  | −0.400<br>[0.276]  | 0.035<br>[0.131]  | 0.265<br>[0.193]  | 0.710<br>[0.089]  | 0.041<br>[0.044]            | −1.203<br>[0.500] | 0.799<br>[0.608]  |
| $spr_{1\rightarrow 10,t}$ | 1.592<br>[0.780]  | −0.219<br>[0.718]  | 0.673<br>[0.340]  | 0.263<br>[0.504]  | 0.293<br>[0.231]  | 0.535<br>[0.114]            | −1.018<br>[1.303] | 0.796<br>[1.584]  |
| $fp_{t-1}$                | −0.177<br>[0.184] | 0.198<br>[0.169]   | 0.186<br>[0.080]  | −0.195<br>[0.119] | −0.108<br>[0.054] | −0.006<br>[0.027]           | 0.786<br>[0.307]  | −0.586<br>[0.373] |
| $R^2$                     | 30.85%            | 52.70%             | 13.99%            | 70.60%            | 60.43%            | 48.11%                      | 26.67%            | 35.17%            |

Table IA.97: VAR coefficient estimates that includes bond return forecasting variables based on the yield curve and the log tax-GDP ratio. US data, 1947–2022

OLS standard errors are reported in square brackets.

|                           | $r_{t+1}$         | $\Delta\tau_{t+1}$ | $\Delta y_{t+1}$  | $fp_{t+1}$        | $\tau y_{t+1}$    | $yr_{1,t+1}$      | $spr_{1\rightarrow 10,t+1}$ | $\Delta x_{t+1}$  | $fa_{t+1}$        |
|---------------------------|-------------------|--------------------|-------------------|-------------------|-------------------|-------------------|-----------------------------|-------------------|-------------------|
| $r_t$                     | −0.025<br>[0.140] | −0.186<br>[0.123]  | −0.033<br>[0.060] | −0.206<br>[0.090] | −0.153<br>[0.106] | 0.003<br>[0.041]  | 0.020<br>[0.020]            | 0.434<br>[0.226]  | −0.618<br>[0.286] |
| $\Delta\tau_t$            | −0.060<br>[0.116] | 0.154<br>[0.102]   | 0.028<br>[0.050]  | −0.146<br>[0.075] | 0.126<br>[0.088]  | 0.002<br>[0.034]  | −0.001<br>[0.017]           | 0.594<br>[0.187]  | −0.438<br>[0.236] |
| $\Delta y_t$              | −0.396<br>[0.354] | 1.312<br>[0.310]   | 0.023<br>[0.152]  | 0.514<br>[0.228]  | 1.289<br>[0.268]  | −0.006<br>[0.105] | −0.135<br>[0.052]           | −0.227<br>[0.572] | 1.539<br>[0.722]  |
| $fp_t$                    | 0.433<br>[0.180]  | −0.419<br>[0.158]  | −0.062<br>[0.077] | 0.831<br>[0.116]  | −0.356<br>[0.137] | 0.154<br>[0.053]  | 0.018<br>[0.026]            | 0.088<br>[0.291]  | −0.506<br>[0.368] |
| $\tau y_t$                | 0.070<br>[0.111]  | −0.275<br>[0.098]  | −0.081<br>[0.048] | 0.055<br>[0.072]  | 0.806<br>[0.084]  | 0.021<br>[0.033]  | −0.002<br>[0.016]           | −0.442<br>[0.180] | 0.165<br>[0.228]  |
| $yr_{1,t}$                | 1.094<br>[0.339]  | −0.003<br>[0.297]  | 0.152<br>[0.145]  | 0.186<br>[0.219]  | −0.155<br>[0.257] | 0.680<br>[0.100]  | 0.043<br>[0.050]            | −0.565<br>[0.548] | 0.561<br>[0.693]  |
| $spr_{1\rightarrow 10,t}$ | 1.604<br>[0.778]  | −0.262<br>[0.683]  | 0.660<br>[0.334]  | 0.272<br>[0.502]  | −0.922<br>[0.590] | 0.296<br>[0.230]  | 0.534<br>[0.114]            | −1.087<br>[1.258] | 0.822<br>[1.590]  |
| $fp_{t-1}$                | −0.156<br>[0.186] | 0.115<br>[0.163]   | 0.161<br>[0.080]  | −0.179<br>[0.120] | −0.046<br>[0.141] | −0.101<br>[0.055] | −0.006<br>[0.027]           | 0.653<br>[0.301]  | −0.536<br>[0.380] |
| $R^2$                     | 31.26%            | 57.19%             | 17.20%            | 70.88%            | 75.14%            | 60.62%            | 48.11%                      | 32.72%            | 35.68%            |

Table IA.98: Variance decomposition of fiscal position  $fp_t$ , US 1947-2022, based on system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1}, yr_{1,t}, spr_{1 \rightarrow 10,t})$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return             | fiscal adjustment       | future sv            | spending ratio        |
|----------|--------------------|-------------------------|----------------------|-----------------------|
| 1        | 0.0<br>[0.0, 0.0]  | 24.2<br>[11.3, 36.8]    | 77.1<br>[64.5, 90.0] | 65.4<br>[36.9, 87.5]  |
| 3        | 0.1<br>[0.0, 0.1]  | 71.6<br>[35.8, 103.0]   | 29.7<br>[-1.8, 65.5] | 68.3<br>[38.9, 98.7]  |
| 10       | 0.1<br>[-0.1, 0.2] | 100.1<br>[70.0, 106.6]  | 1.1<br>[-5.2, 31.1]  | 81.6<br>[40.5, 127.2] |
| $\infty$ | 0.1<br>[-0.2, 0.4] | 101.3<br>[100.9, 101.5] | 0.0<br>[-0.0, 0.0]   | 82.4<br>[31.9, 142.4] |

Table IA.99: Variance decomposition of fiscal position  $fp_t$ , US 1947-2022, based on system  $(r_t, \Delta\tau_t, \Delta y_t, fp_t, fp_{t-1}, \tau y_t, yr_{1,t}, spr_{1 \rightarrow 10,t})$

Quantities in square brackets indicate the 95% confidence intervals due to a bootstrap exercise. In this bootstrap procedure we i) draw a new VAR(1) coefficient matrix using the covariance matrix of the estimated coefficients around the point estimates; ii) given this VAR matrix and the data, generate the news series and do the variance decomposition; iii) repeat i) and ii) 2,000 times and report the 95% quantiles.

| horizon  | return             | fiscal adjustment       | future sv            | spending ratio         |
|----------|--------------------|-------------------------|----------------------|------------------------|
| 1        | 0.0<br>[0.0, 0.0]  | 24.3<br>[11.1, 36.6]    | 77.0<br>[64.7, 90.2] | 66.4<br>[42.8, 87.9]   |
| 3        | 0.1<br>[0.0, 0.1]  | 73.2<br>[39.7, 104.0]   | 28.1<br>[-2.8, 61.6] | 74.5<br>[56.3, 97.2]   |
| 10       | 0.0<br>[-0.1, 0.2] | 101.2<br>[78.0, 111.0]  | 0.1<br>[-9.6, 23.5]  | 103.1<br>[91.1, 129.8] |
| $\infty$ | 0.0<br>[-0.1, 0.2] | 101.3<br>[101.1, 101.5] | 0.0<br>[-0.0, 0.0]   | 100.7<br>[88.6, 135.6] |

## References

- Hall, George J., and Thomas J. Sargent.** 2021. “Debt and Taxes in Eight US Wars and Two Insurrections.” *The Handbook of Historical Economics*, 825–880.
- Koeda, Junko, and Yosuke Kimura.** 2025. “Government debt maturity and the term structure in Japan.” *The Japanese Economic Review*, 1–26.